

# Predictions of Diffractive Cross Sections in Proton-Proton Collisions



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arXiv.org > hep-ph > arXiv:1205.1446

High Energy Physics - Phenomenology

## MBR Monte Carlo Simulation in PYTHIA8

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*(Submitted on 7 May 2012)*

# CONTENTS

- Introduction
- Cross Sections
- (Event Generation)
- (Implementation in PYTHIA8)
- Conclusions

For details on the phenomenology of the predictions see:

**DIFFRACTION 2010**

**"Diffractive and total *pp* cross sections at the LHC and beyond" (KG)**

<http://link.aip.org/link/doi/10.1063/1.3601406>

This talk: an implementation of these cross sections in PYTHIA8.

# INTRODUCTION

- ❑ The **RENORM (renormalization model)** soft  $pp$  cross sections previously used in MBR (Minimum Bias Rockefeller) simulation **are adapted to PYTHIA8**.
  - **MBR was successful at Fermilab in fixed target and collider experiments.**
- ❑ RENORM predictions are based on a parton-model approach in which **diffraction is derived from inclusive PDFs and color factors**.
- ❑ Diffractive cross sections and final states are both predicted:
  - Cross sections vs gap width or vs forward momentum loss of proton(s):
    - ✓ **Absolute normalization!**
  - Hadronization of dissociated proton:
    - A (non-perturbative) **“quark string”** is introduced and tuned to reproduce the MBR multiplicity and  $p_T$  distributions.
    - $dN/d\eta$ ,  $p_T$ , and particle ID: new in this PYTHIA8 implementation (the original MBR simulation produced only  $\pi^\pm$  and  $\pi^0$ ).
    - Unique unitarization based on a saturated “glue-ball” exchange.
- ❑ Total Cross section  **$\sim \ln^2 s$**  based on a **glue-ball-like saturated-exchange**.
  - Immune to eikonalization-model dependences.

# STUDIES OF DIFFRACTION IN QCD

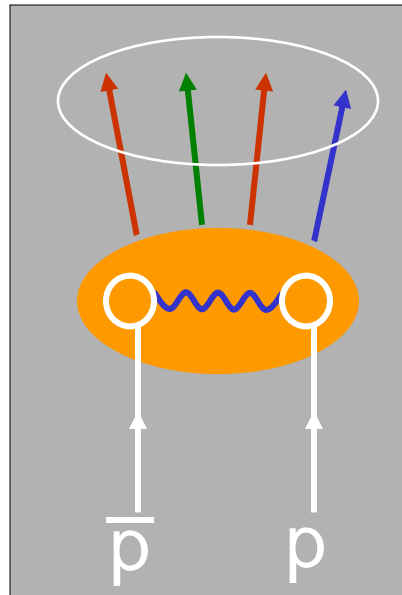
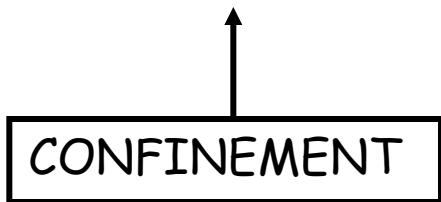
## Non-diffractive

- ❖ color-exchange  $\rightarrow$  gaps exponentially suppressed

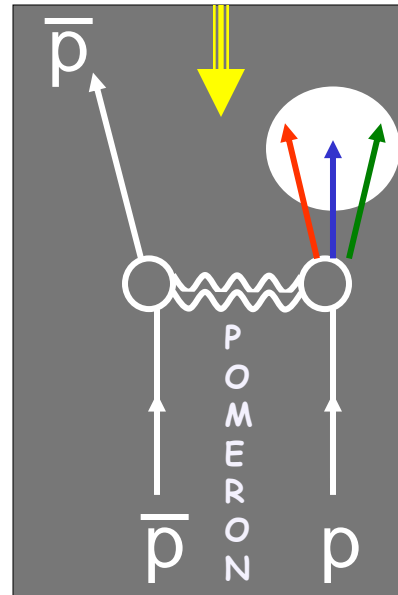
## Diffractive

- ❖ Colorless vacuum exchange  $\rightarrow$  large-gap signature

Incident hadrons acquire color and break apart



rapidity gap

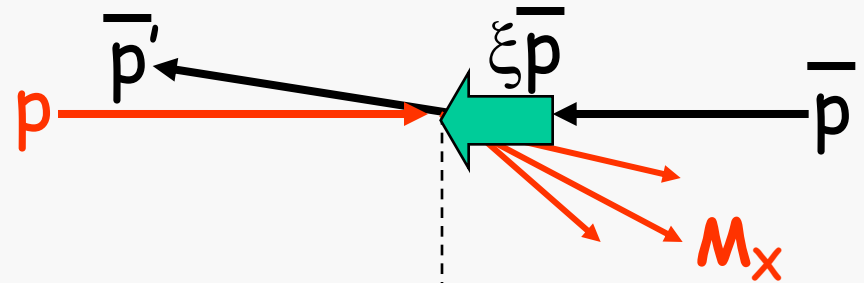
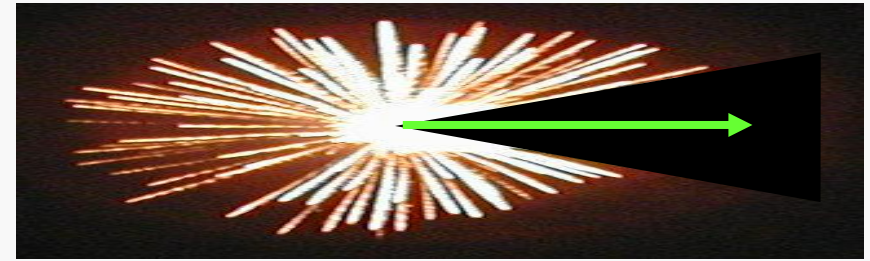
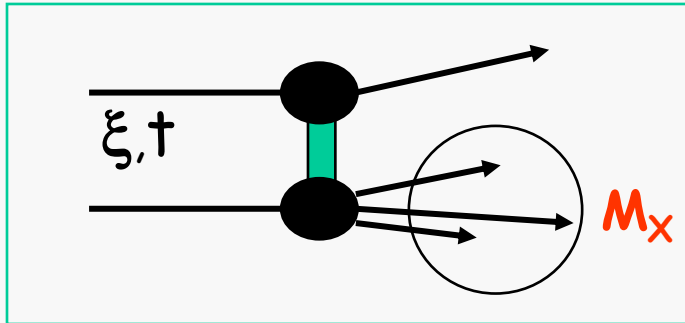


Incident hadrons retain their quantum numbers remaining colorless

Goal: probe the QCD nature of the diffractive exchange

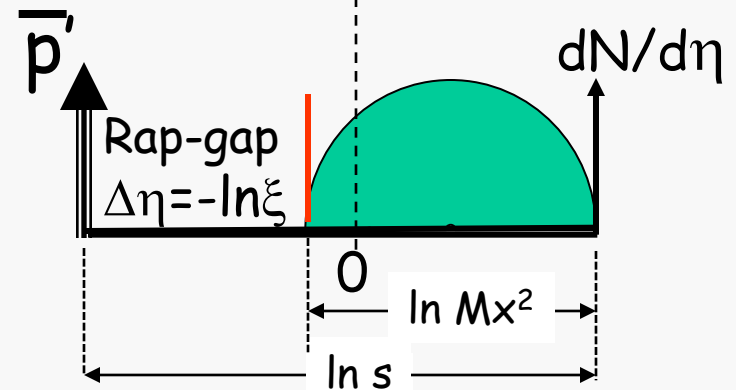
# DEFINITIONS

## SINGLE DIFFRACTION



$$1 - x_L \equiv \xi = \frac{M_x^2}{s}$$

$$\xi^{\text{CAL}} = \frac{\sum_{i=1}^{\text{all}} E_T^{i\text{-tower}} e^{-\eta_i}}{\sqrt{s}}$$



**since no radiation  $\rightarrow$**   
no price paid for increasing  
diffractive gap size

$$\left( \frac{d\sigma}{d\Delta\eta} \right)_{t=0} \approx \text{constant} \Rightarrow \frac{d\sigma}{d\xi} \propto \frac{1}{\xi} \Rightarrow \frac{d\sigma}{dM^2} \propto \frac{1}{M^2}$$

# DIFFRACTION AT CDF

Elastic scattering



$\sigma_T = \text{Im } f_{el}(t=0)$

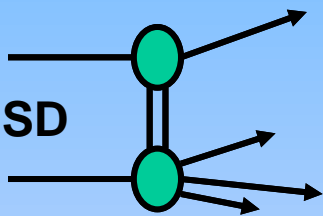


OPTICAL THEOREM

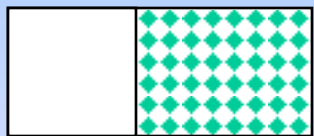
Total cross section



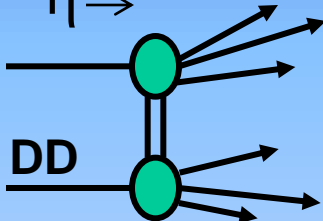
SD



Single Diffraction or Single Dissociation



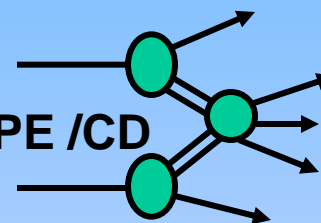
DD



Double Diffraction or Double Dissociation



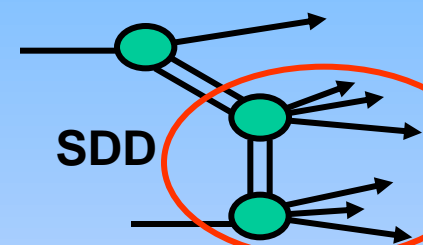
DPE / CD



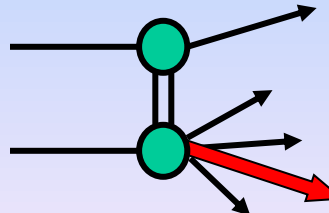
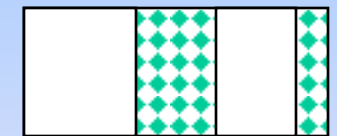
Double Pom. Exchange or Central Dissociation



SDD

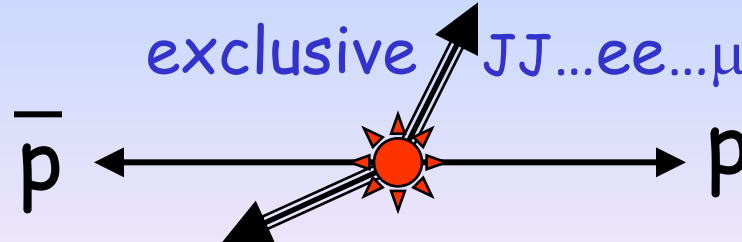


Single + Double Diffraction (SDD)



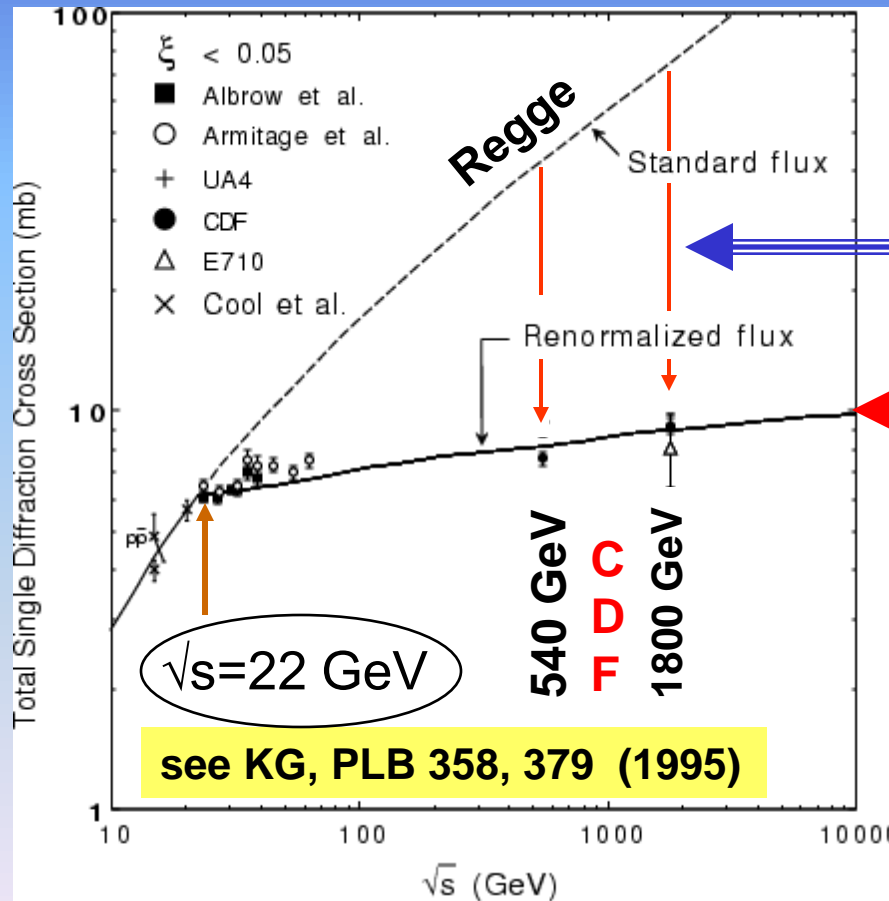
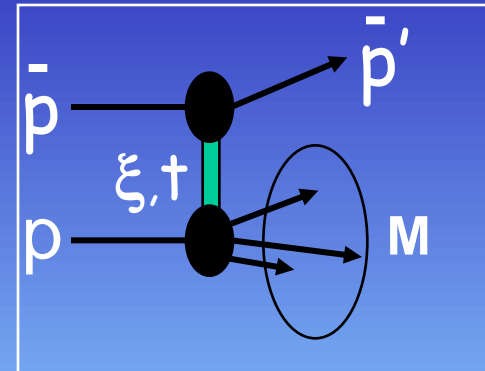
JJ, b, J/ψ, W

exclusive JJ...ee...μμ...γγ



# FACTORIZATION BREAKING IN SOFT DIFFRACTION

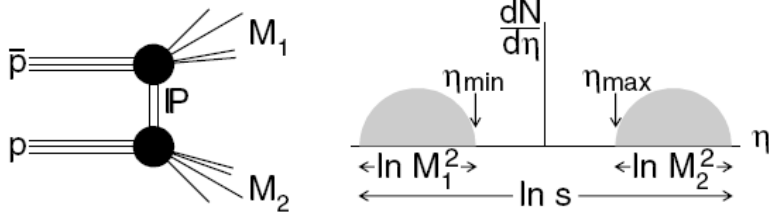
→ diffractive x-section suppressed relative to Regge prediction as  $\sqrt{s}$  increases



Factor of  $\sim 8$  ( $\sim 5$ )  
 suppression at  
 $\sqrt{s} = 1800$  (540) GeV

RENORMALIZATION

# DD at CDF

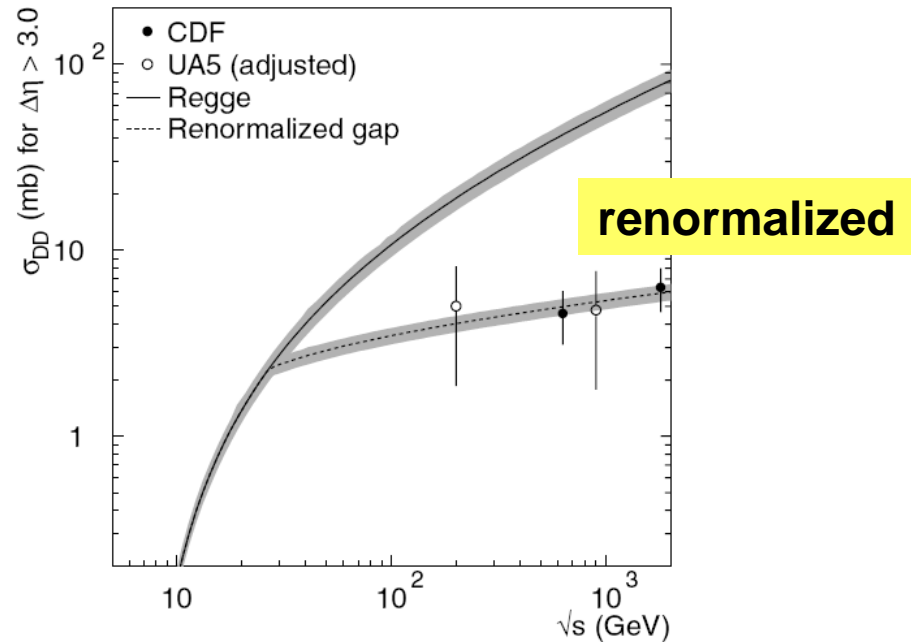
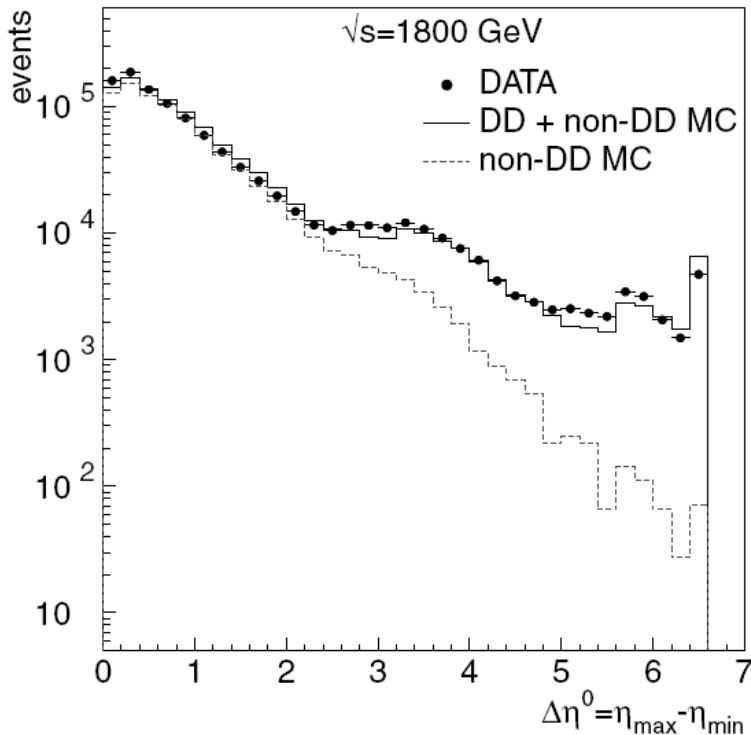


$$\frac{d^3\sigma_{DD}}{dt dM_1^2 dM_2^2} = \frac{d^2\sigma_{SD}}{dt dM_1^2} \frac{d^2\sigma_{SD}}{dt dM_2^2} / \frac{d\sigma_{el}}{dt}$$

$$= \frac{[\kappa \beta_1(0) \beta_2(0)]^2}{16\pi} \frac{s^{2\epsilon} e^{b_{DD}t}}{(M_1^2 M_2^2)^{1+2\epsilon}}$$

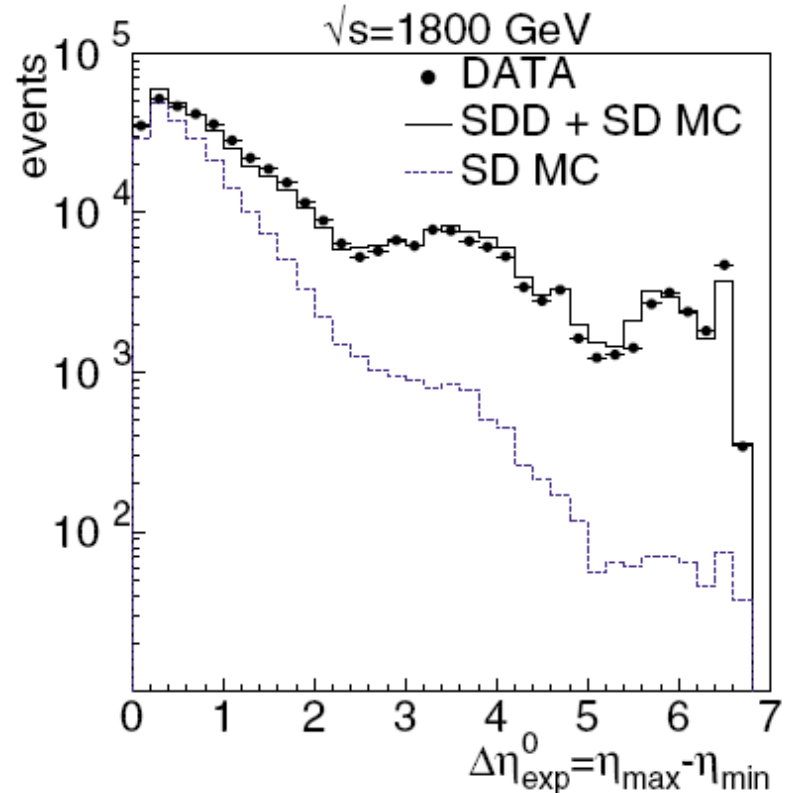
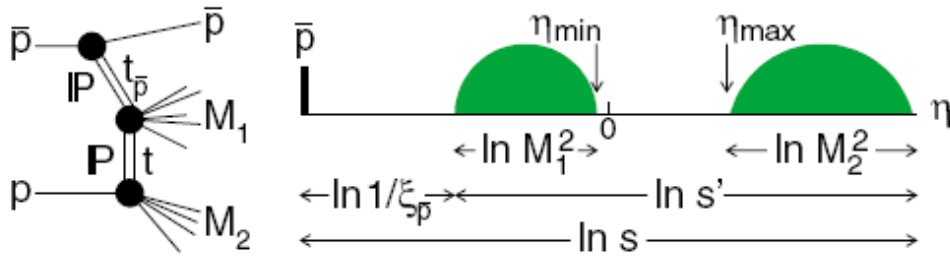
$$\frac{d^3\sigma_{DD}}{dt d\Delta\eta d\eta_c} = \left[ \frac{\kappa \beta^2(0)}{16\pi} e^{2[\alpha(t)-1]\Delta\eta} \right] \left[ \kappa \beta^2(0) \left( \frac{s'}{s_0} \right)^\epsilon \right]$$

gap probability                      x-section





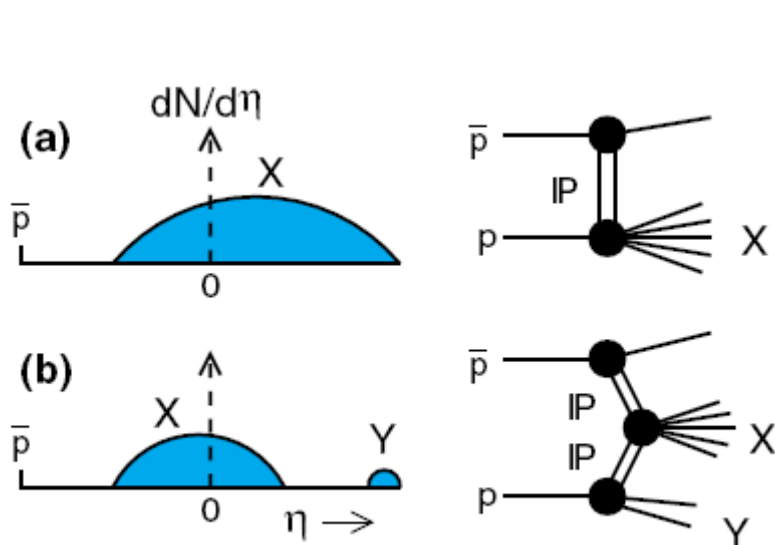
# SDD at CDF



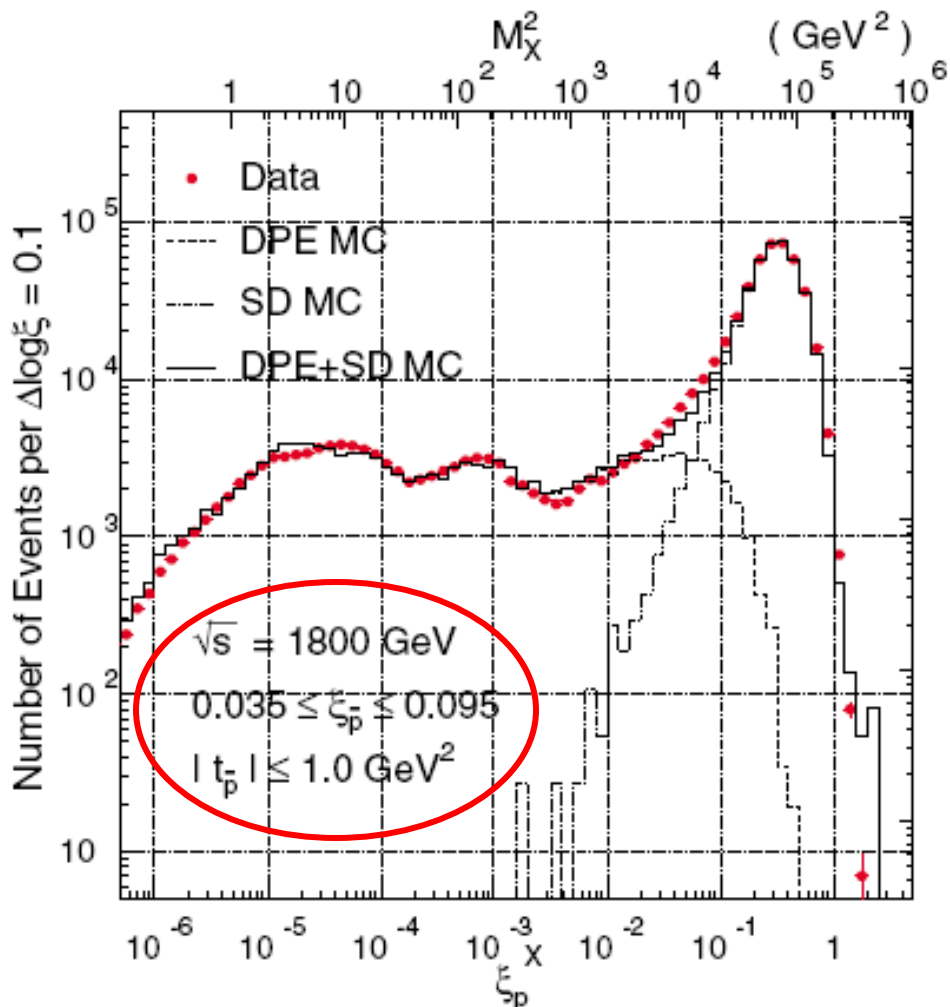
■ Excellent agreement between data and MBR (MinBiasRockefeller) MC

$$\frac{d^5\sigma}{dt_{\bar{p}} dt d\xi_{\bar{p}} d\Delta\eta d\eta_c} = \left[ \frac{\beta(t)}{4\sqrt{\pi}} e^{[\alpha(t_{\bar{p}})-1]\ln(1/\xi)} \right]^2 \times \kappa \left\{ \kappa \left[ \frac{\beta(0)}{4\sqrt{\pi}} e^{[\alpha(t)-1]\Delta\eta} \right]^2 \kappa \left[ \beta^2(0) \left( \frac{s''}{s_0} \right)^\epsilon \right] \right\}$$

# CD (DPE) at CDF



- Excellent agreement between data and MBR
- ➔ low and high masses are correctly implemented

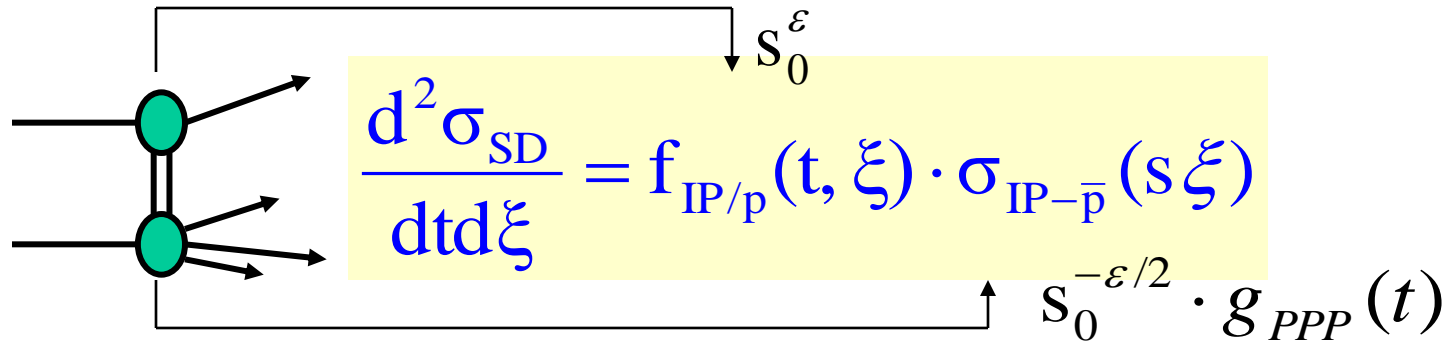


# Scale $s_0$ and triple-pom coupling

Slide #16  
Ddfr. 2012

Pom. flux: interpret as gap probability  
→ set to unity: determines  $g_{PPP}$  and  $s_0$

KG, PLB 358 (1995) 379



- Two free parameters:  $s_0$  and  $g_{PPP}$
- Obtain product  $g_{PPP} \cdot s_0^{\epsilon/2}$  from  $\sigma_{SD}$
- Renormalized Pomeron flux determines  $s_0$
- Get unique solution for  $g_{PPP}$

$$g_{PPP} = 0.69 \text{ mb}^{-1/2} = 1.1 \text{ GeV}^{-1}$$

$$s_0 = 3.7 \pm 1.5 \text{ GeV}^2$$

# Reduce the uncertainty in $s_0$

## Saturation glueball?

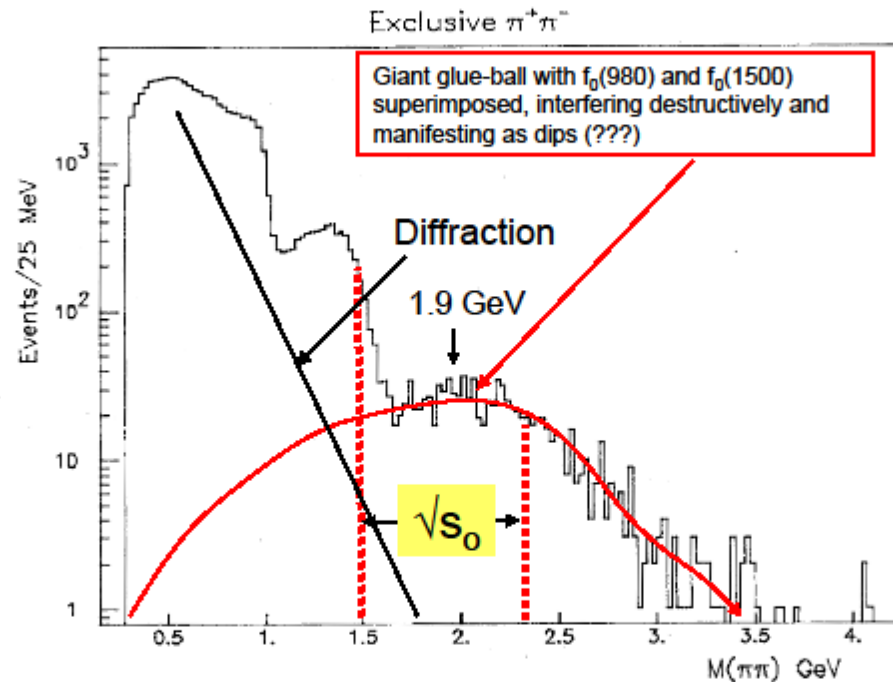
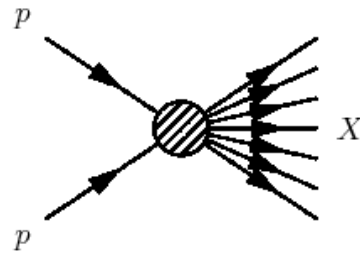
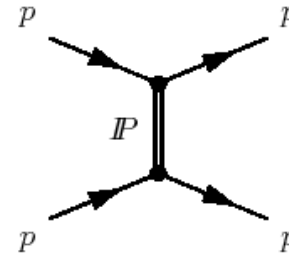


Figure 8:  $M_{\pi^+\pi^-}$  spectrum in *DPE* at the ISR (Axial Field Spectrometer, R807 [97, 98]). Figure from Ref. [98]. **See M.G.Albrow, T.D. Goughlin, J.R. Forshaw, hep-ph>arXiv:1006.1289**

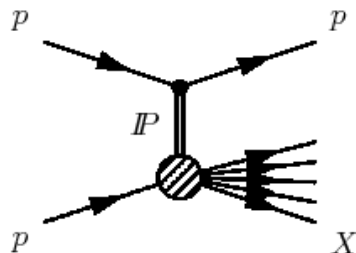
# Cross Sections



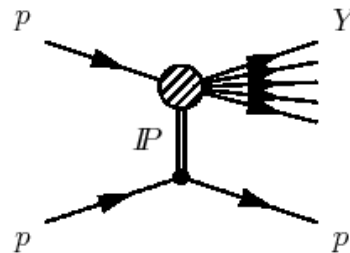
(a) tot



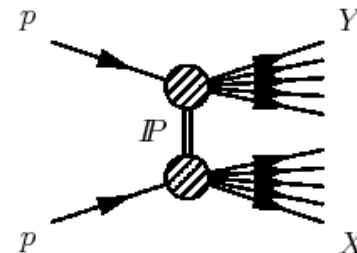
(b) el



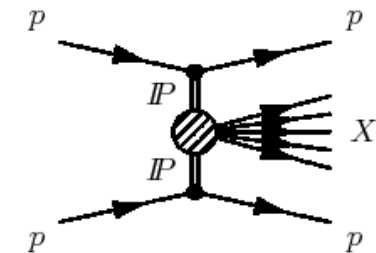
(c) SD



(d) SD



(e) DD



(f) CD

- SD → single diffraction (single dissociation)
- DD → double diffraction (double diffraction)
- CD → central dissociation (double pomeron exchange)

# Total, elastic, and inelastic x-sections

$$\sigma_{\text{ND}} = (\sigma_{\text{tot}} - \sigma_{\text{el}}) - (2\sigma_{\text{SD}} + \sigma_{\text{DD}} + \sigma_{\text{CD}})$$

R. J. M. Covolan, K. Goulios, J. Montanha, Phys. Lett. B **389**, 176 (1996)

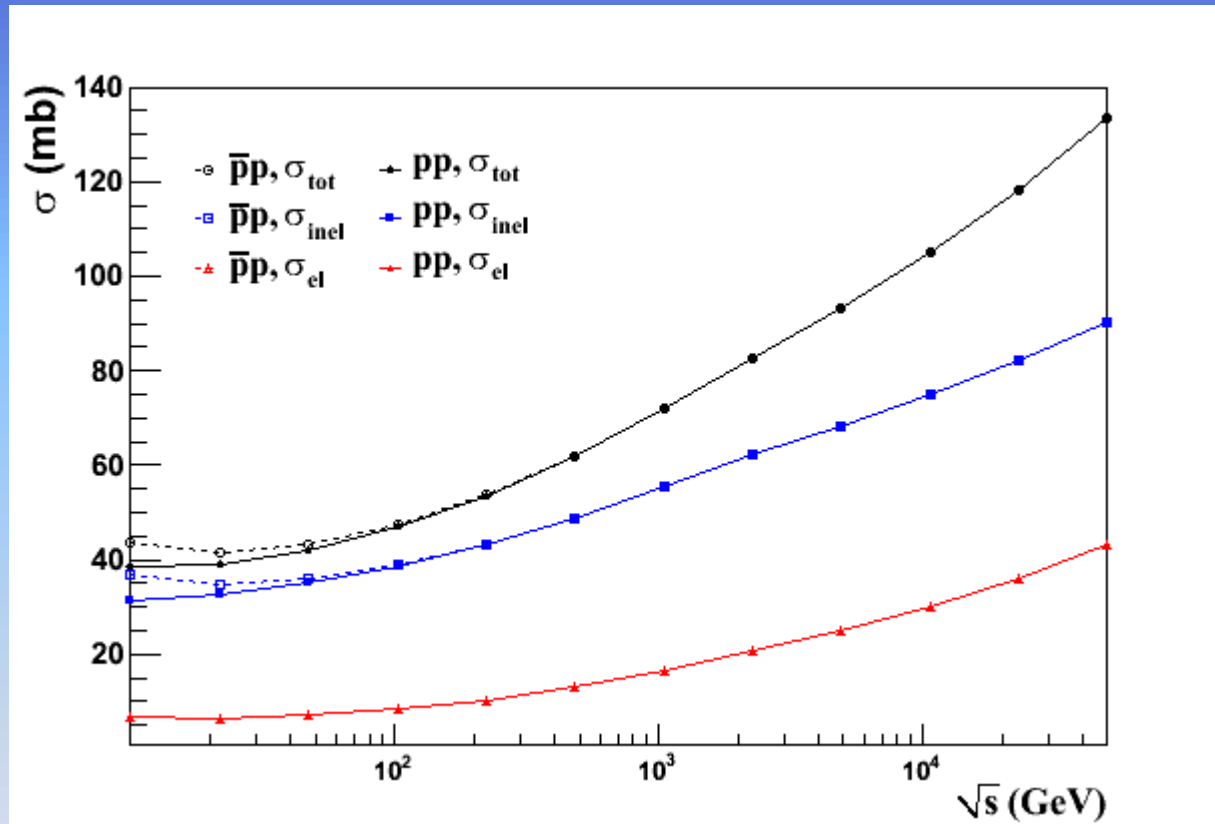
$$\sigma_{\text{tot}}^{p^\pm p} = \begin{cases} 16.79s^{0.104} + 60.81s^{-0.32} \mp 31.68s^{-0.54} & \text{for } \sqrt{s} < 1.8 \\ \sigma_{\text{tot}}^{\text{CDF}} + \frac{\pi}{s_0} \left[ \left( \ln \frac{s}{s_F} \right)^2 - \left( \ln \frac{s^{\text{CDF}}}{s_F} \right)^2 \right] & \text{for } \sqrt{s} \geq 1.8 \end{cases}$$

K. Goulios, *Diffraction, Saturation and pp Cross Sections at the LHC*, arXiv:1105.4916.

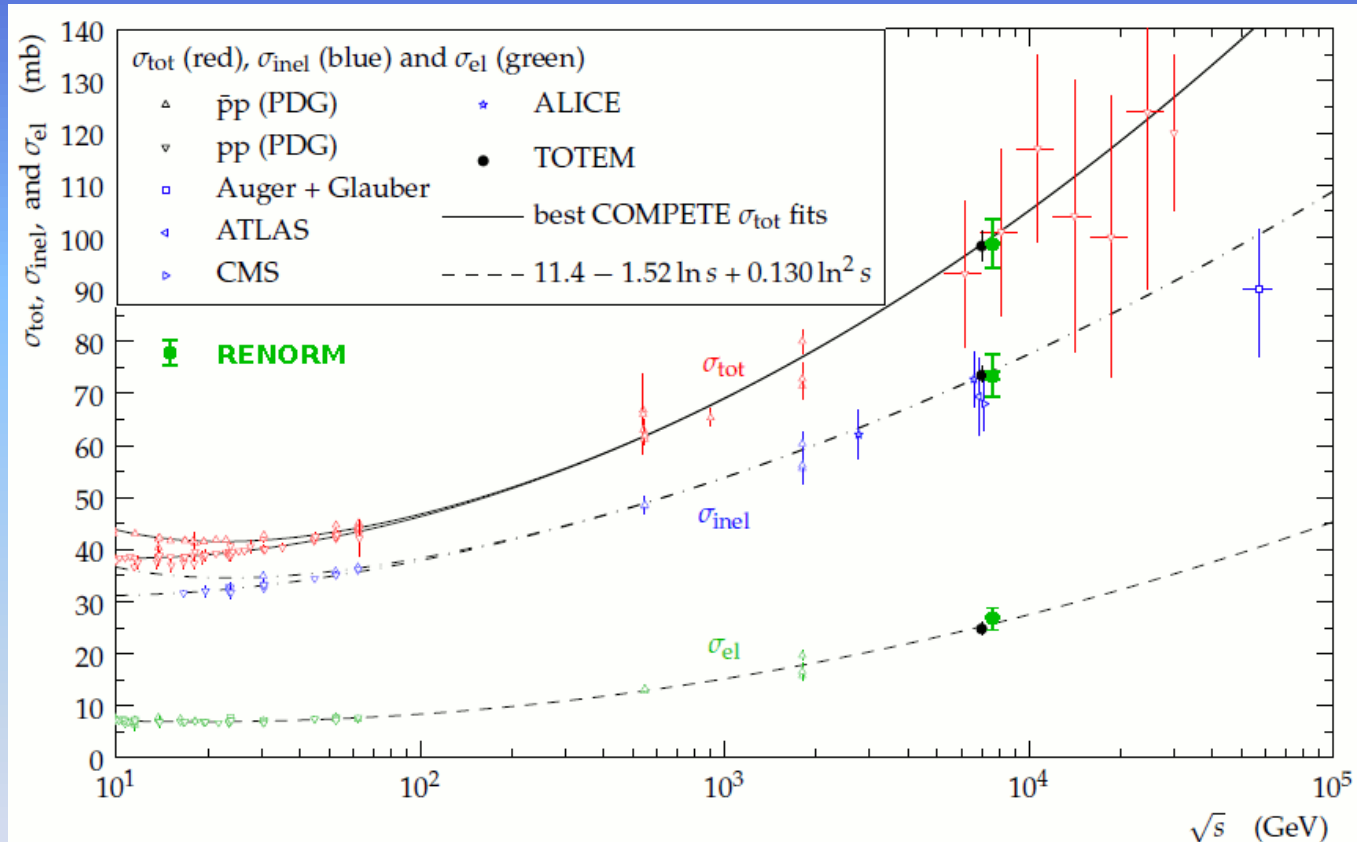
$$\sqrt{s^{\text{CDF}}} = 1.8 \text{ TeV}, \sigma_{\text{tot}}^{\text{CDF}} = 80.03 \pm 2.24 \text{ mb}$$

$$\sqrt{s_F} = 22 \text{ GeV} \quad s_0 = 3.7 \pm 1.5 \text{ GeV}^2$$

# Total, elastic, and inelastic x-sections versus $\sqrt{s}$

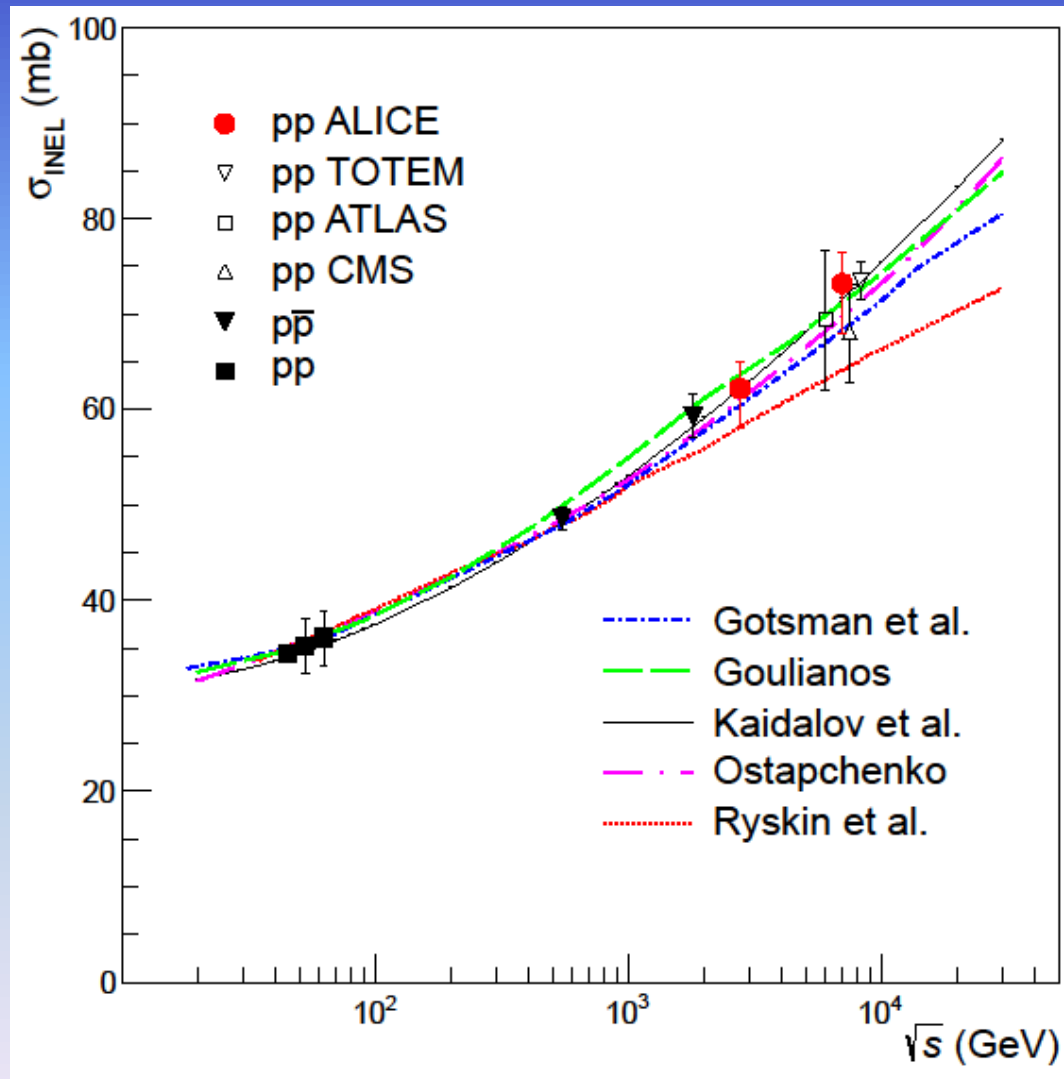


# TOTEM vs PYTHIA8-MBR





# ALICE tot-inel vs PYTHIA8-MBR





# Diffractive x-sections

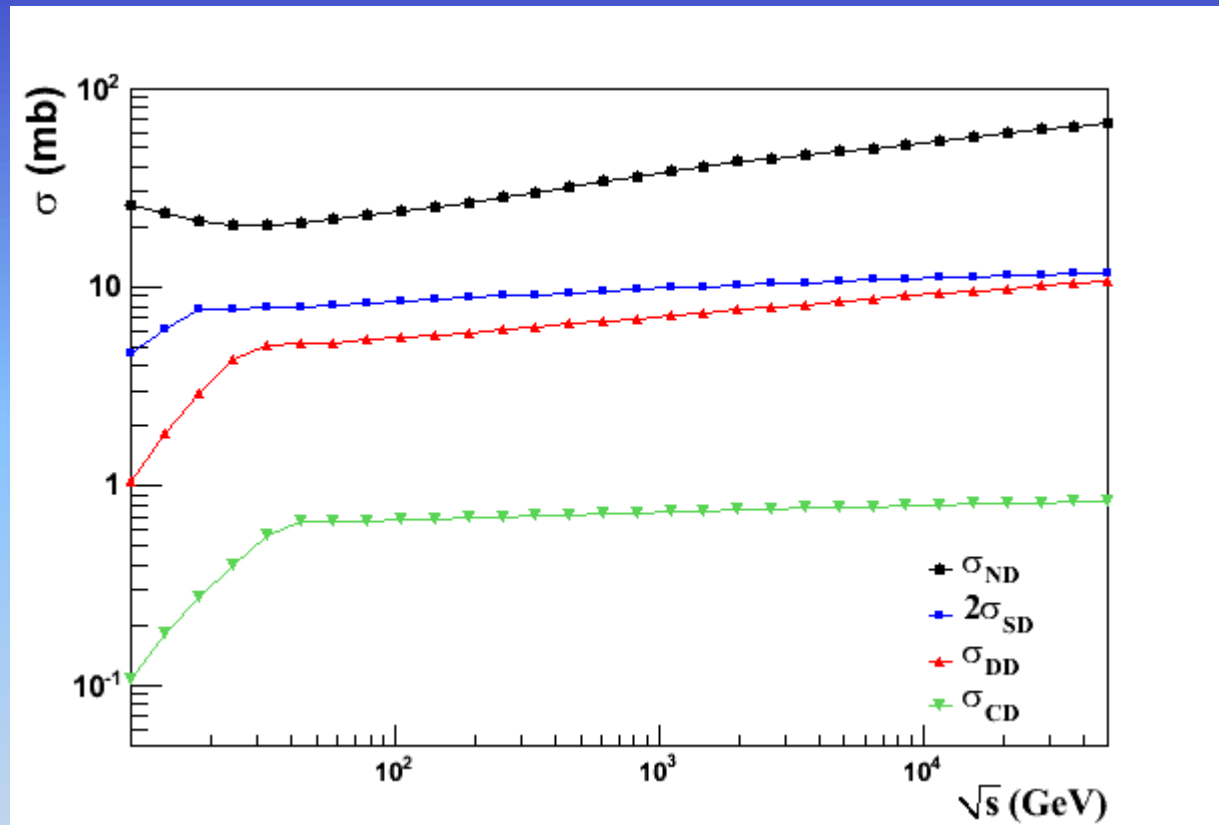
$$\begin{aligned} \frac{d^2\sigma_{SD}}{dt d\Delta y} &= \frac{1}{N_{\text{gap}}(s)} \left[ \frac{\beta^2(t)}{16\pi} e^{2[\alpha(t)-1]\Delta y} \right] \cdot \left\{ \kappa \beta^2(0) \left( \frac{s'}{s_0} \right)^\epsilon \right\}, \\ \frac{d^3\sigma_{DD}}{dt d\Delta y dy_0} &= \frac{1}{N_{\text{gap}}(s)} \left[ \frac{\kappa \beta^2(0)}{16\pi} e^{2[\alpha(t)-1]\Delta y} \right] \cdot \left\{ \kappa \beta^2(0) \left( \frac{s'}{s_0} \right)^\epsilon \right\}, \\ \frac{d^4\sigma_{DPE}}{dt_1 dt_2 d\Delta y dy_c} &= \frac{1}{N_{\text{gap}}(s)} \left[ \prod_i \left[ \frac{\beta^2(t_i)}{16\pi} e^{2[\alpha(t_i)-1]\Delta y_i} \right] \right] \cdot \kappa \left\{ \kappa \beta^2(0) \left( \frac{s'}{s_0} \right)^\epsilon \right\} \end{aligned}$$

$$\beta^2(t) = \beta^2(0) F^2(t)$$

$$F^2(t) = \left[ \frac{4m_p^2 - 2.8t}{4m_p^2 - t} \left( \frac{1}{1 - \frac{t}{0.71}} \right)^2 \right]^2 \approx a_1 e^{b_1 t} + a_2 e^{b_2 t}$$

$$\alpha_1=0.9, \alpha_2=0.1, b_1=4.6 \text{ GeV}^{-2}, b_2=0.6 \text{ GeV}^{-2}, s'=s e^{-\Delta y}, \kappa=0.17, \kappa\beta^2(0)=\sigma_0, s_0=1 \text{ GeV}^2, \sigma_0=2.82 \text{ mb or } 7.25 \text{ GeV}^{-2}$$

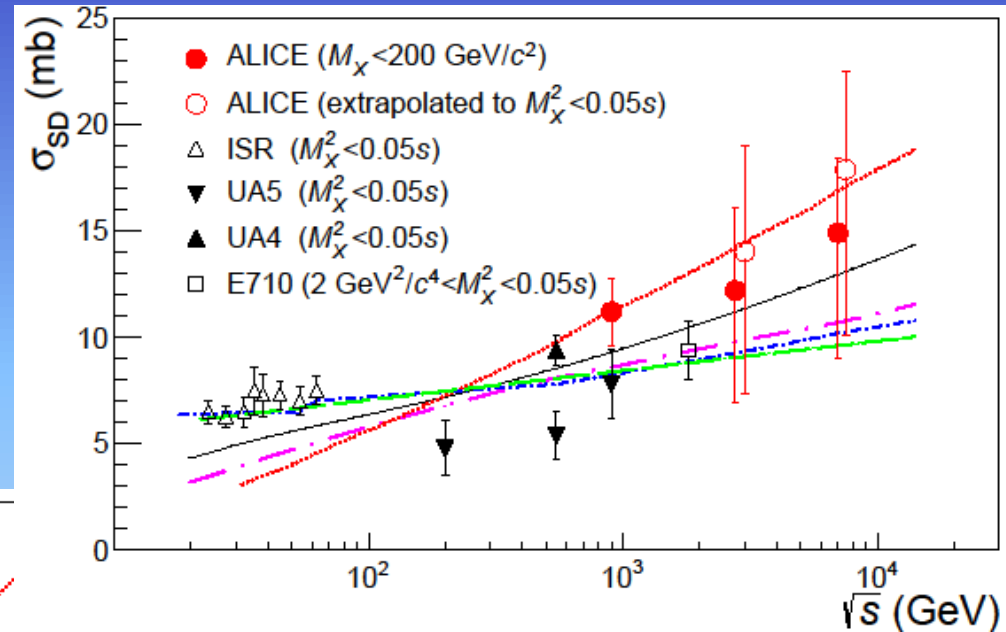
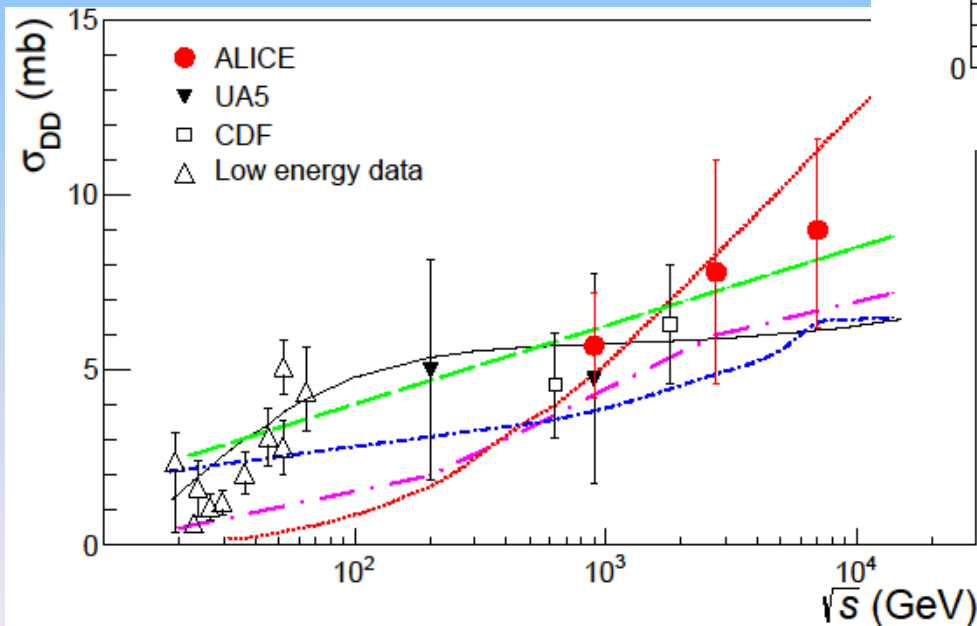
# Diffractive x-sections of $\sqrt{s}$



- Suppress x-sections at small gaps by a factor  $S$  using the error function with  $\Delta y_S=2$  for SD and DD, and  $\Delta y=\Delta y_1+\Delta y_2=2$  for CD (DPE).

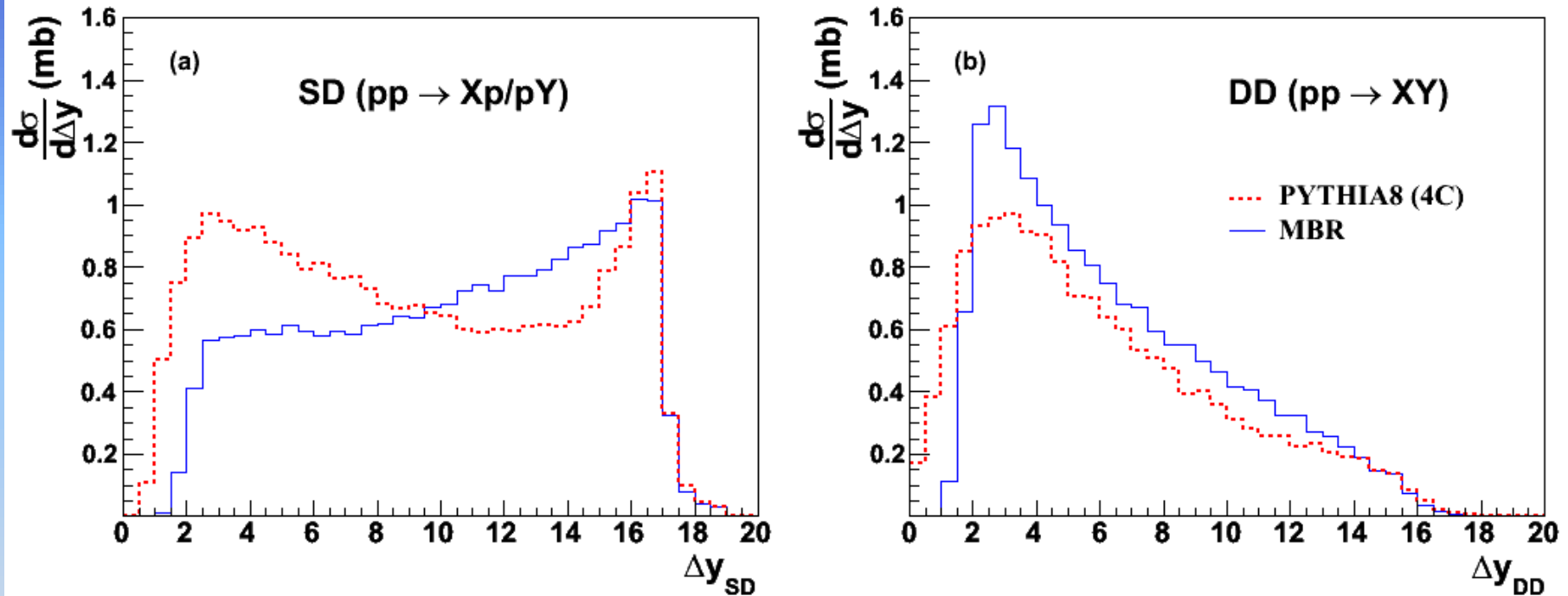
$$S = \frac{1}{2} \left[ 1 + \text{erf} \left( \frac{\Delta y - \Delta y_S}{\sigma_S} \right) \right]$$

# ALICE SD and DD vs PYTHIA8-MBR



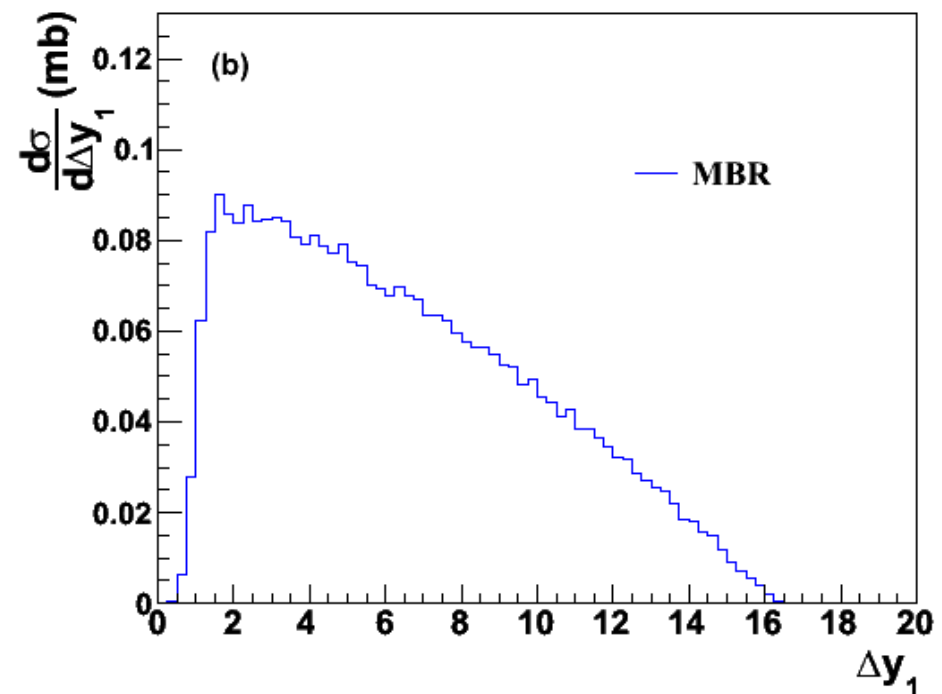
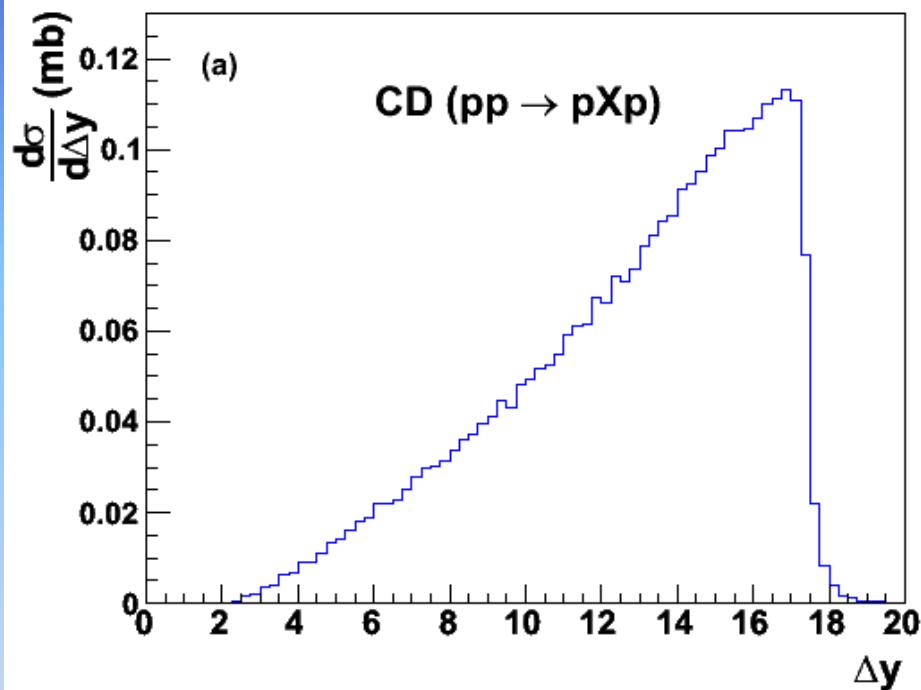
# SD and DD at 7 TeV

## MBR vs PYTHIA8-4C



- The differences between the PYTHIA8(4C) and MBR predictions are mainly due to the  $(1/M^2)^{1+\varepsilon}$  behavior, with  $\varepsilon=1.104$  in MBR vs 1,08 in PYTHIA8(4C).

# CD (DPE) x-sections at 7 TeV versus (a) $\Delta y = \Delta y_1 + \Delta y_2$ and (b) $\Delta y_1$



- ❑ Both figures are MBR predictions with a  $\Delta y=2$  cut-off in the error function.
- ❑ The normalization is absolute with no model uncertainty other than that due to the determination of the parameters in the formulas as determined from data

# SUMMARY ← introduction

- ❑ The ENORM (renormalization model) soft  $pp$  cross sections previously used in MBR (Minimum Bias Rockefeller) simulation are adapted to PYTHIA8.
  - MBR was successful at Fermilab in fixed target and collider experiments.
- ❑ RENORM predictions are based on a parton-model approach, in which diffraction is derived from inclusive PDFs and color factors.
- ❑ Diffractive cross sections and final states are both predicted:
  - Cross sections vs gap width or vs forward-momentum loss of proton(s):
    - ✓ Absolute normalization!
  - Hadronization of dissociated proton:
    - A (non-perturbative) “quark string” is introduced and tuned to reproduce the MBR multiplicity and  $p_T$  distributions.
    - $dN/d\eta$ ,  $p_T$ , and particle ID: new in this PYTHIA8 implementation (the original MBR simulation produced only  $\pi^\pm$  and  $\pi^0$ ).
    - Unique unitarization based on a saturated “glue-ball” exchange.
- ❑ Total Cross section  $\sim \ln^2 s$  based on a glue-ball-like saturated-exchange.
  - Immune to eikonalization-model dependences.

*Thank you for your attention*



# References in arXiv:1205.1446v2 [hep-ph]

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K. Goulios, *Diffraction in QCD*, arXiv:hep-ph/020314.
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- [11] K. Goulios, *Diffraction interactions of hadrons at high energies*, Phys. Rep. 101, 169 (1983).