

Diffractive and Total Cross Sections @ Tevatron and LHC

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The Rockefeller University

→ CDF results are presented on behalf of the CDF Collaboration ←



Contents

- Introduction
- Total Cross Sections
- Diffraction
- Exclusive Production

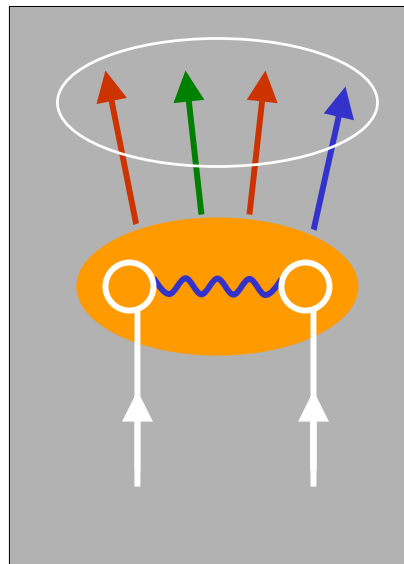
\bar{p} -p Interactions

Non-diffractive:
Color-exchange

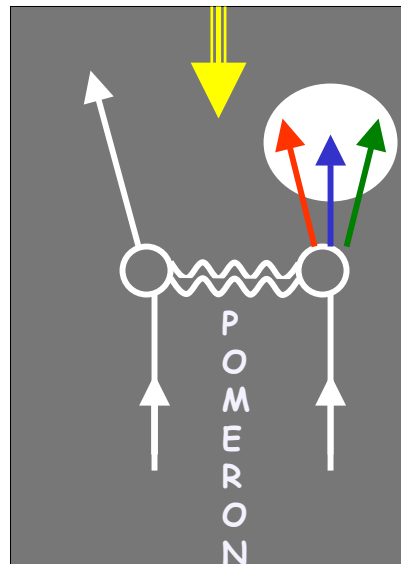
Diffractive:
Colorless exchange with
vacuum quantum numbers

rapidity gap

Incident hadrons
acquire color
and break apart



CONFINEMENT



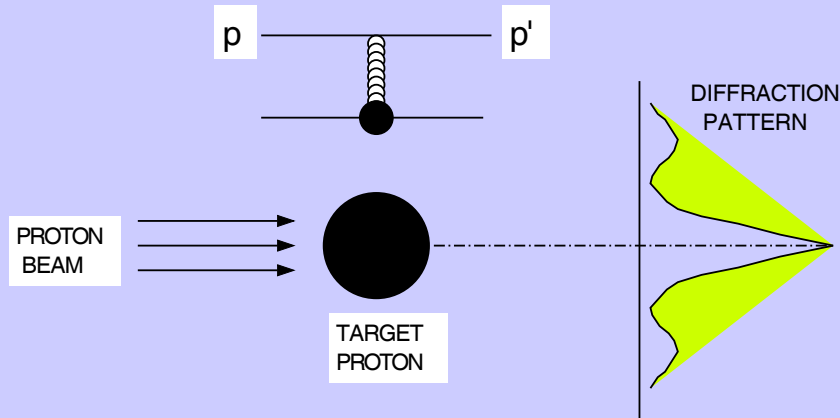
Incident hadrons retain
their quantum numbers
remaining colorless

pseudo-
DECONFINEMENT

Goal: understand the QCD nature of the diffractive exchange

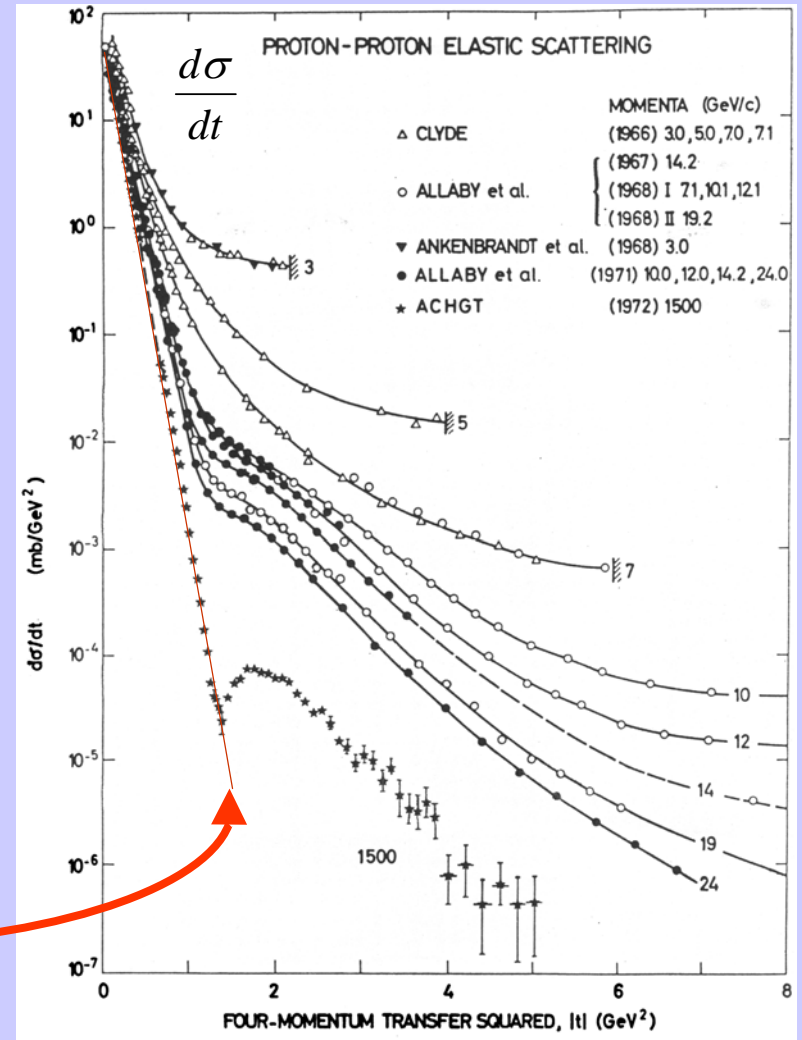
Elastic Scattering

PROTON-PROTON ELASTIC SCATTERING

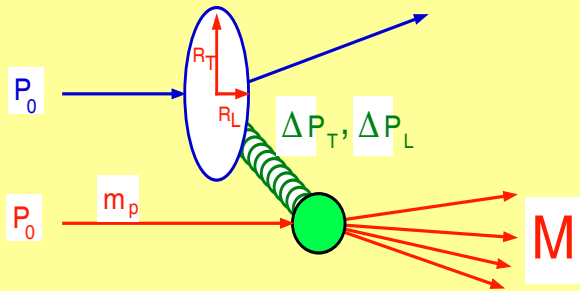


$$\frac{d\sigma}{dt} \sim e^{bt} \sim e^{-\frac{R^2}{4}(p\theta)^2}$$

$$R = \frac{1}{m_\pi} \Rightarrow b \approx 13 \left(\frac{\text{GeV}}{c} \right)^{-2}$$



Diffraction Dissociation



Momentum loss fraction

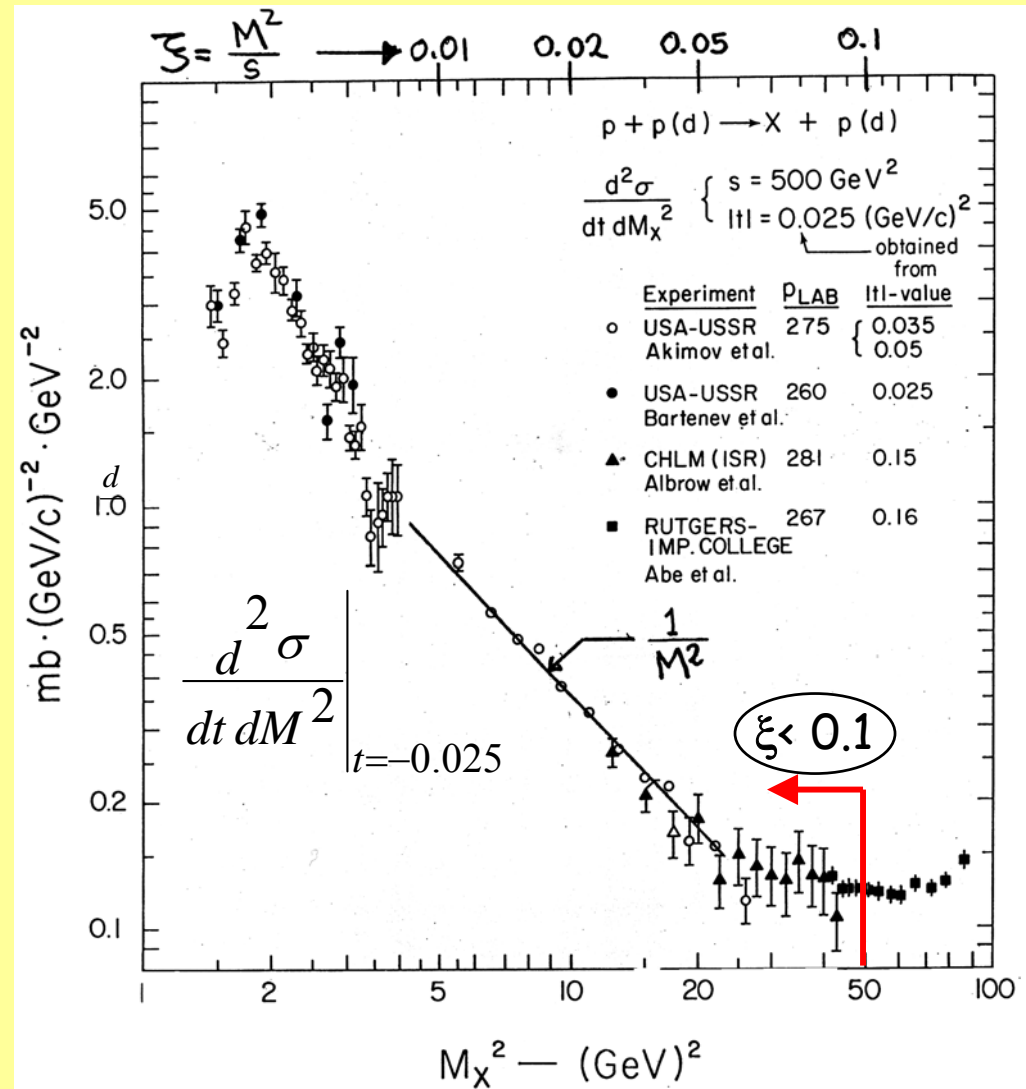
$$\xi = \frac{\Delta P_L}{P_L} = \frac{M_X^2}{S}$$

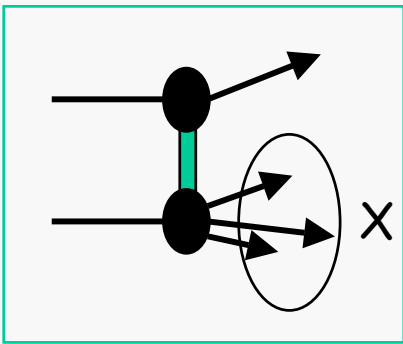
COHERENCE CONDITION

$$\xi < \frac{m_\pi}{m_p} \approx 0.1$$

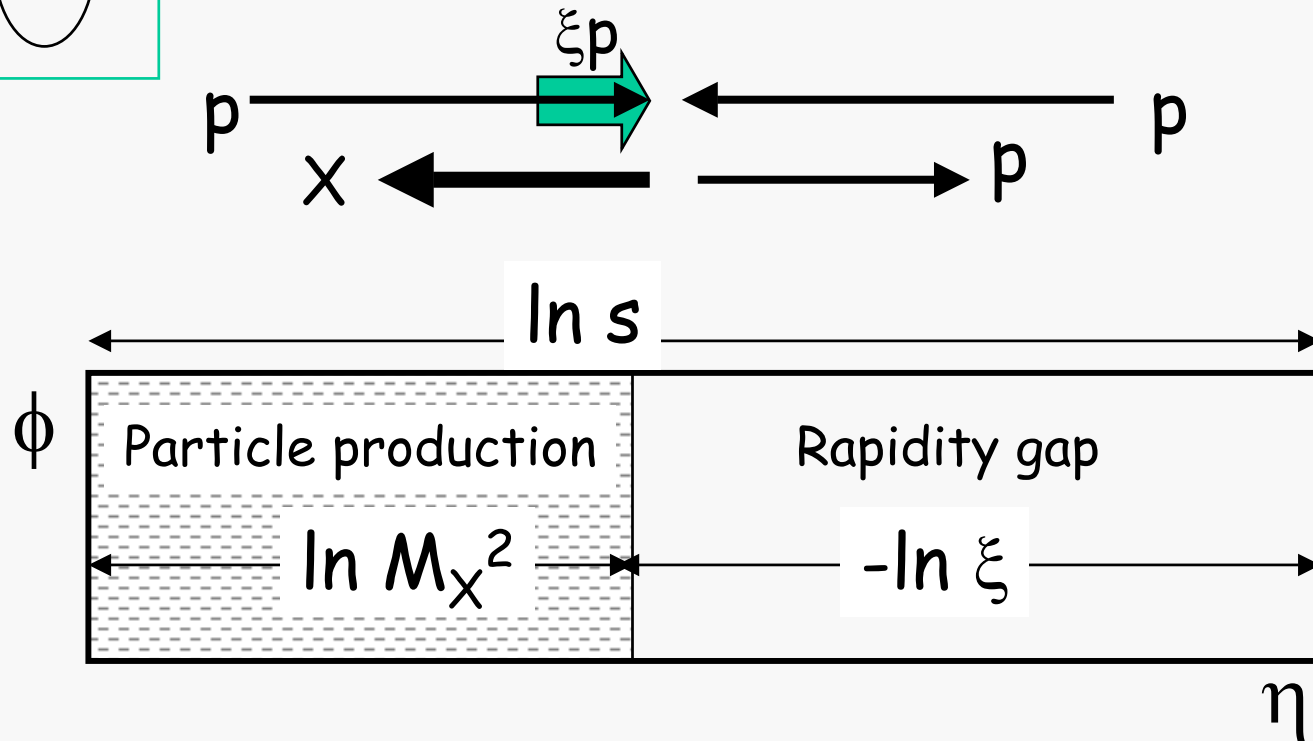
@ Tevatron $M_X \rightarrow 600 \text{ GeV}$
 @ LHC $\rightarrow 4.4 \text{ TeV}$

But why $\frac{d\sigma}{dM^2} \sim \frac{1}{M^2}$?





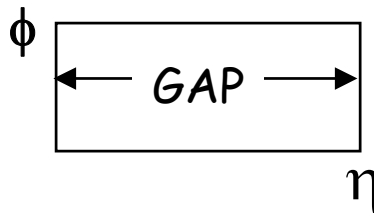
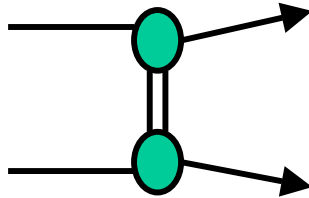
Rapidity Gaps



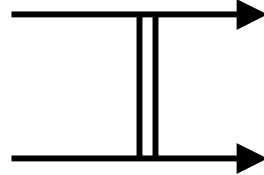
$$\left(\frac{d\sigma}{d\Delta\eta} \right)_{t=0} \approx \text{constant} \Rightarrow \frac{d\sigma}{dM^2} \sim \frac{1}{M^2} \Rightarrow \frac{d\sigma}{d\xi} \sim \frac{1}{\xi}$$

Diffractive $\bar{p}p$ Processes

Elastic scattering

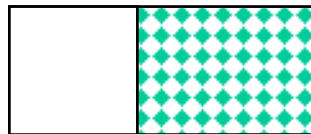
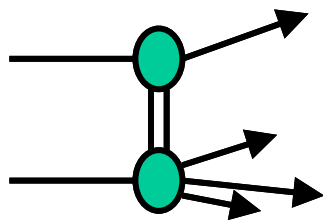
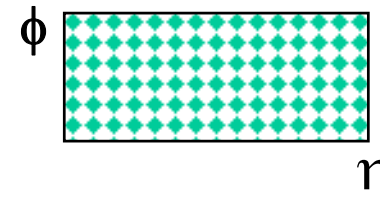
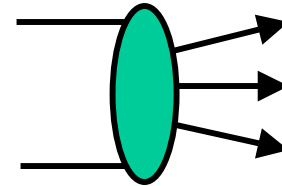


$\sigma_T = \text{Im } f_{el}(t=0)$

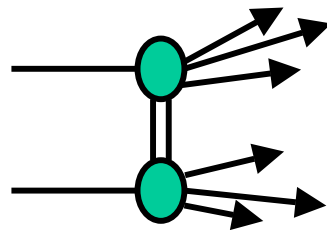


OPTICAL
THEOREM

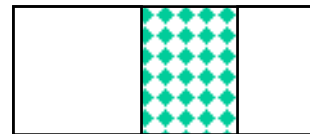
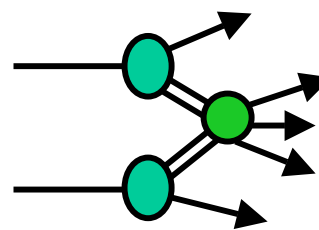
Total cross section



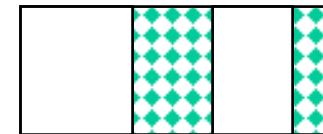
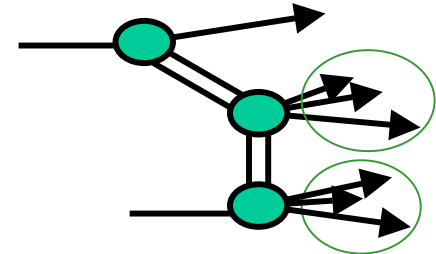
SD



DD

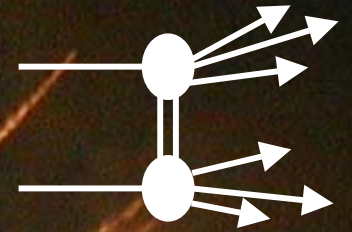


DPE



SDD=SD+DD

Rapidity Gaps in Fireworks



The Physics

- Elastic and Total Cross Sections:..... $pp \rightarrow pp$ and $pp \rightarrow X$
 - ✓ Fundamental Quantum Mechanics
 - Froissart Unitarity Bound..... $\sigma_T < C \ln^2 s$
 - Optical theorem..... $\sigma_T \sim \text{Im } f(t=0)$
 - Dispersion relations..... $\text{Re } f(t=0) \sim \text{Im } f(t=0)$
 - Is space-time discrete? → Measure the ρ -value at the LHC!

- Diffraction Dissociation:..... $pp \rightarrow pX$, $pp \rightarrow pXp$, $pp \rightarrow XGX$, $pp \rightarrow pXGX$
 - ✓ Non-perturbative QCD
 - Soft & hard diffraction
 - Factorization
 - Multi-gap diffraction
 - Diffraction in QCD:.....what is the Pomeron?
 - Dark energy?

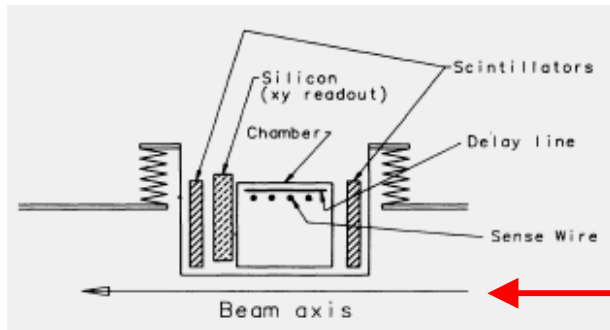
- Exclusive Production:..... $pp \rightarrow pp+A$ (jet+jet, $\gamma+\gamma$, ..., H^0)
 - ✓ Discovery channel
 - Diffractive Higgs production at the LHC (?)

Tevatron Experiments

Exp \ Info	Roman Pots	EI	σ_T	Soft diffraction	Hard diffraction
E710/811 (Scint. Counters)	p, pbar	x	x	sd	
CDF-0	p, pbar	x	x	sd	
CDF-I	pbar			sd,dd,dpe,sdd	JJ,b,J/ ψ ,W,JGJ
CDF-II	pbar			sd	JJ,W,Z,JGJ Exclusive JJ, $\gamma\gamma$,...
DO-I					JJ,W,Z,JGJ, ...
DO-II	p, pbar	x	x	sd,dpe,...	JJ,W,Z,JGJ, ... Exclusive ???

CDF Run 1-0 (1988-89)

Elastic, diffractive, and total cross section
@ 546 and 1800 GeV

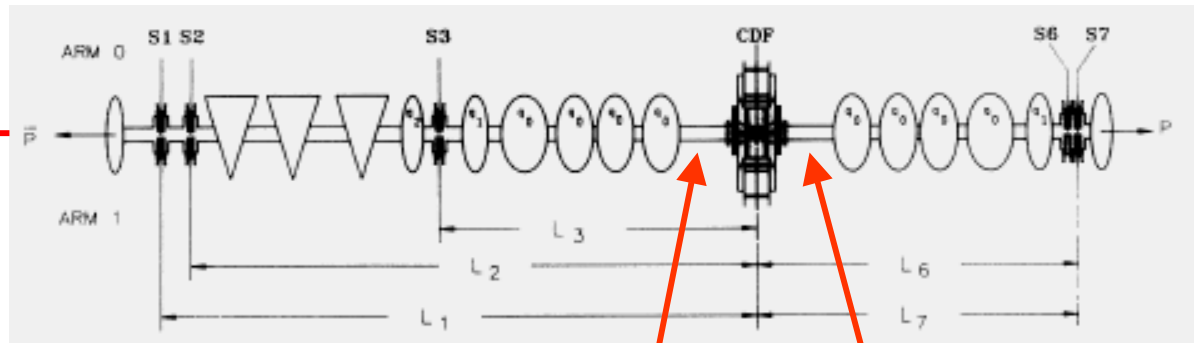


Roman Pot Detectors

- Scintillation trigger counters
- Wire chamber
- Double-sided silicon strip detector

Roman Pot Spectrometers

CDF-I

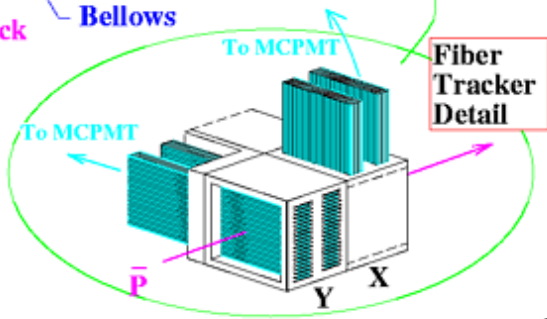
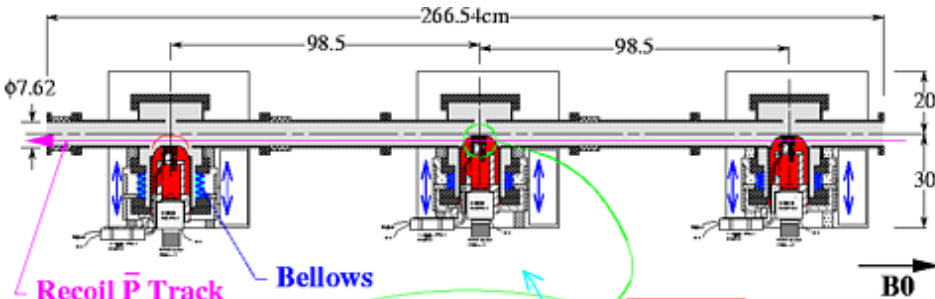


Roman Pots with Trackers
up to $|\eta| = 7$

CDF-I

Run-IC

Run-IA,B

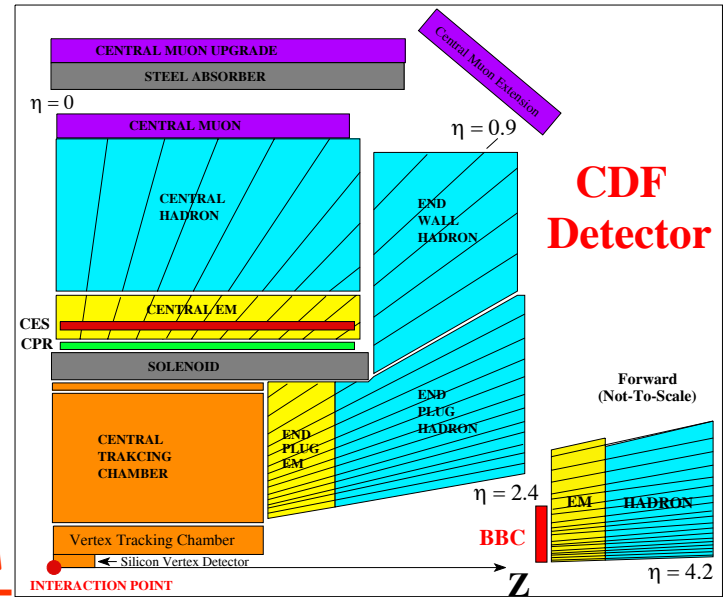


Scintillator fiber xy-tracker
270 μ pitch, 2 m lever arm

$x < 0.97$

$x = 1$

Acceptance: $0 < |t| < 1, 0.03 < \xi < 0.1$



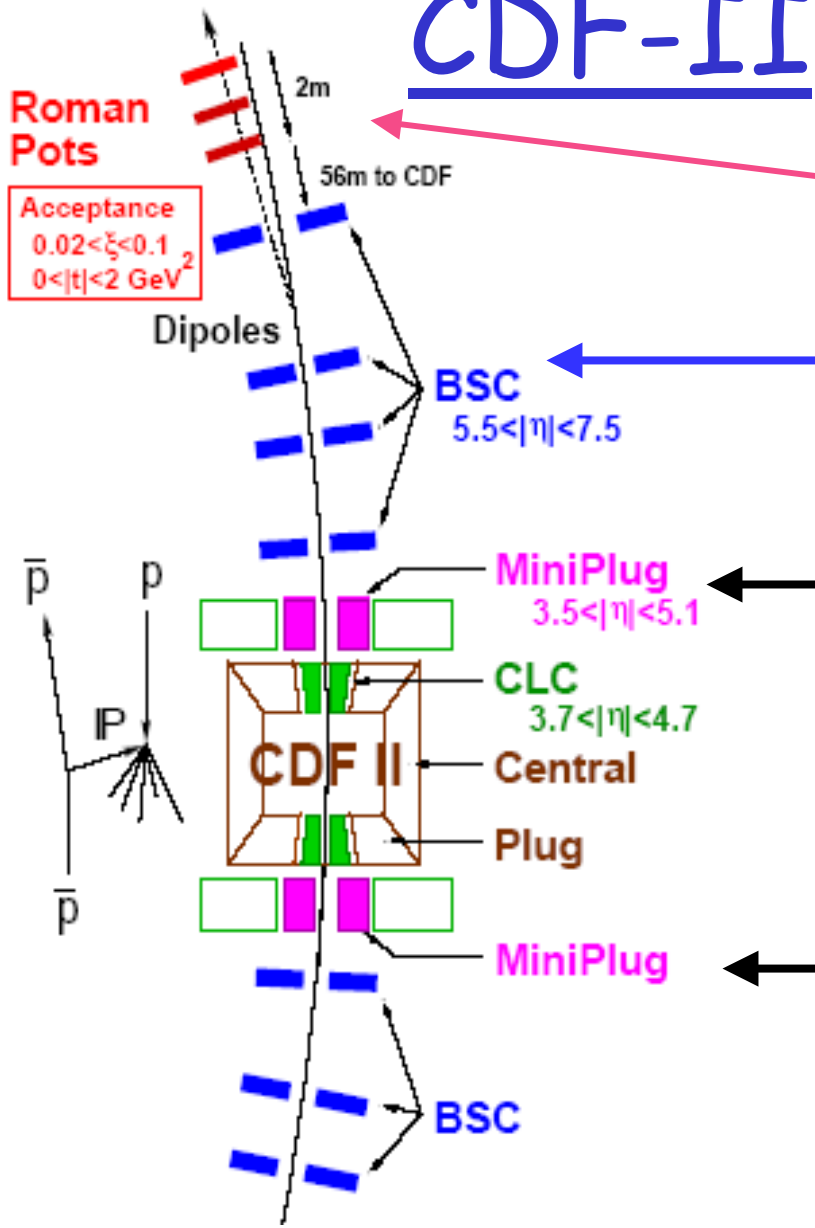
beam

Forward Detectors

BBC $3.2 < \eta < 5.9$

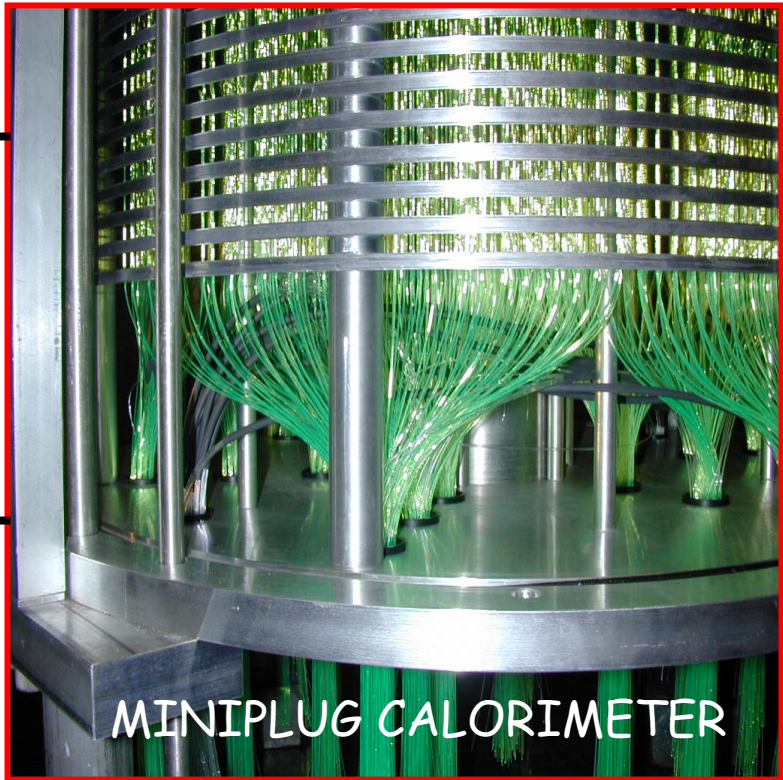
FCAL $2.4 < \eta < 4.2$

CDF-II

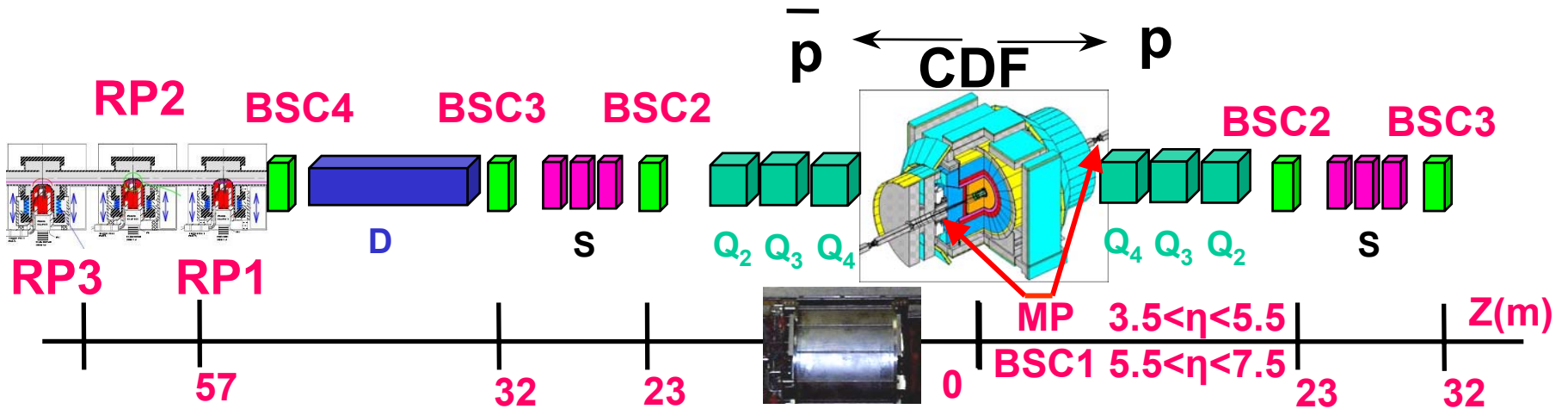


ROMAN POT DETECTORS

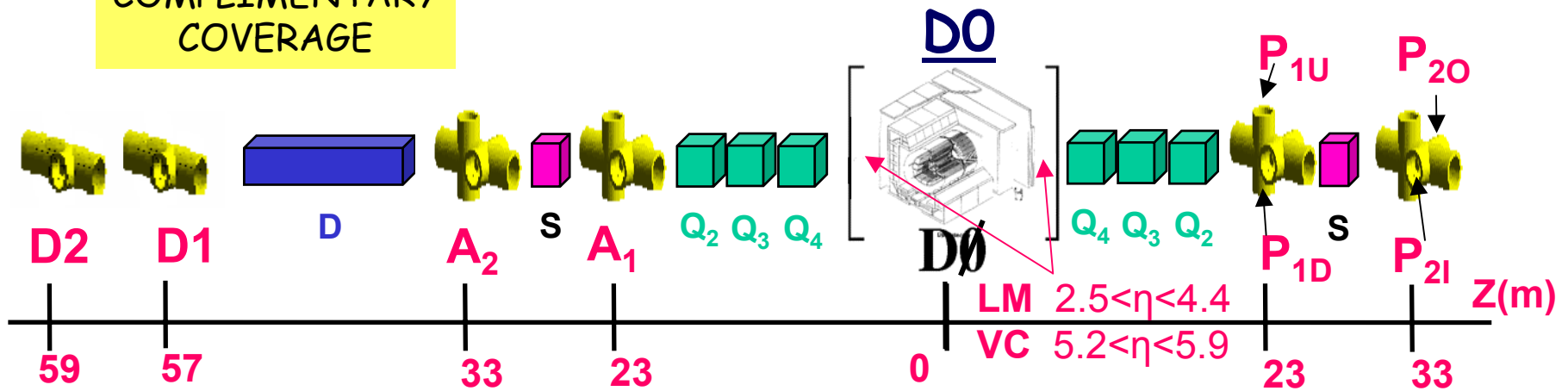
BEAM SHOWER COUNTERS:
Used to reject ND events



CDF & DØ - Run II



CDF & DØ:
COMPLIMENTARY
COVERAGE



From Barreto's talk in small-x

ELASTIC AND TOTAL CROSS SECTIONS

At Tevatron:
CDF and E710/811

→ use luminosity independent method

$$\sigma_T^2 \sim \frac{1}{L} \frac{1}{1+\rho^2} \left. \frac{dN_{el}}{dt} \right|_{t=0} \quad \& \quad \sigma_T \sim \frac{1}{L} (N_{el} + N_{inel})$$

optical theorem

$$\Rightarrow \quad \sigma_T = \frac{16\pi}{1+\rho^2} \left(\left. \frac{dN_{el}}{dt} \right|_{t=0} \right) \frac{1}{N_{el} + N_{inel}}$$

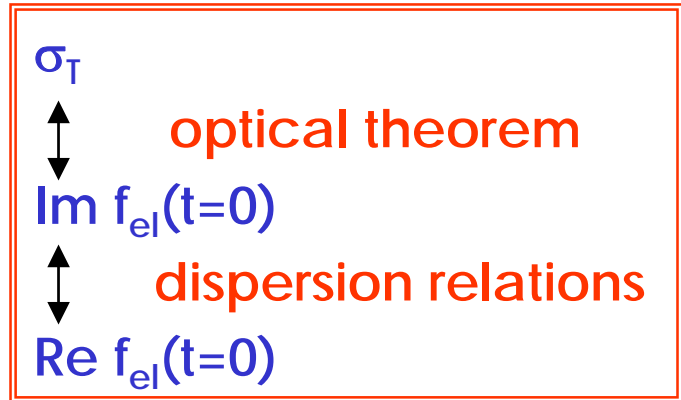
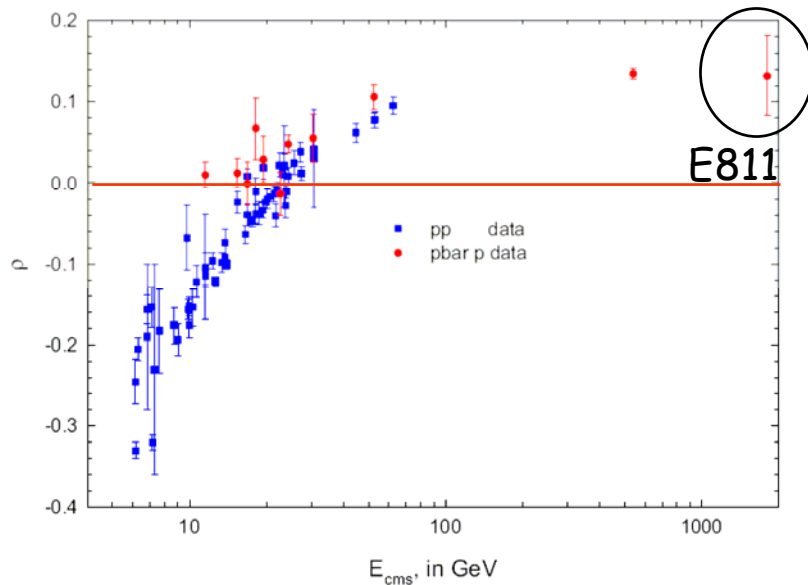
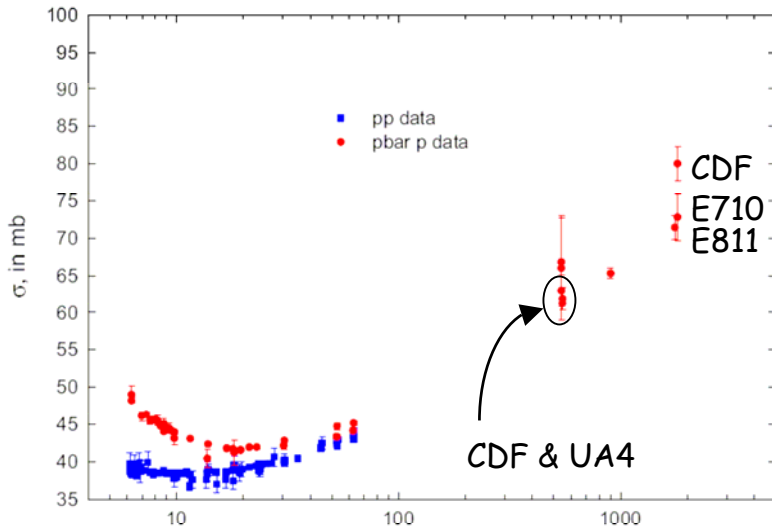
Alert:

- background N_{inel} yields small σ_T
- undetected N_{inel} yields large σ_T

σ_T and ρ -values from PDG

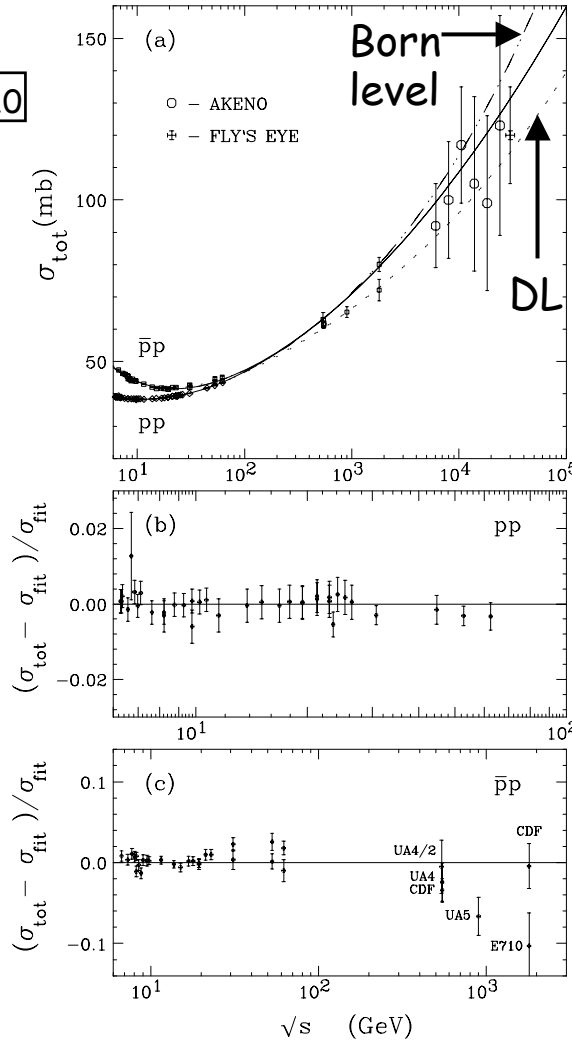
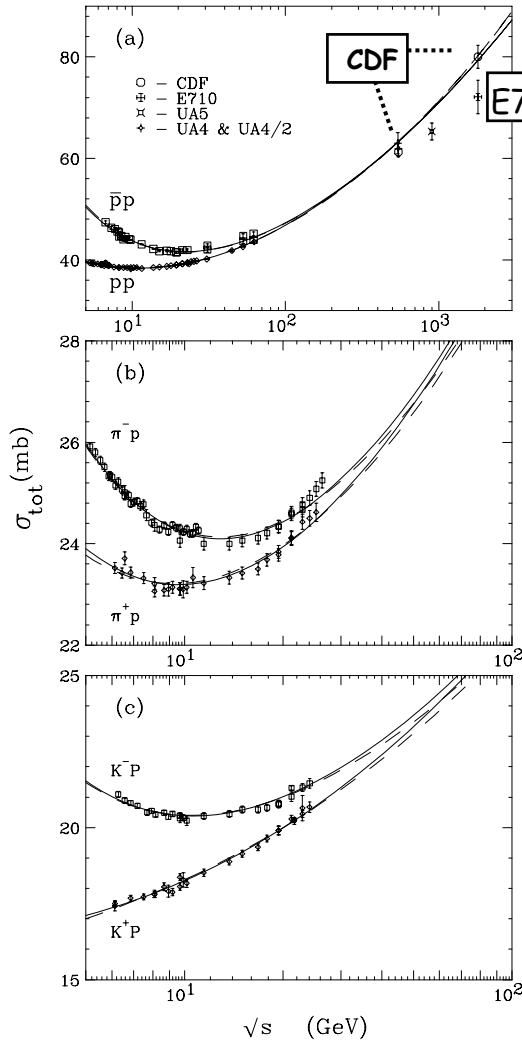
ρ = ratio of real/imaginary parts of elastic scattering amplitude at $t=0$

CDF and E710/811 disagree



N. Khuri and A. Martin:
measuring ρ at the LHC tests
discreteness of space-time

Total Cross Sections: Regge fit



CMG: Covelan, Montagna, and G
PLB 389 (1995) 176

Simultaneous Regge fit to
 pp , πp , and Kp σ -sections
using the eikonal approach
to ensure unitarity

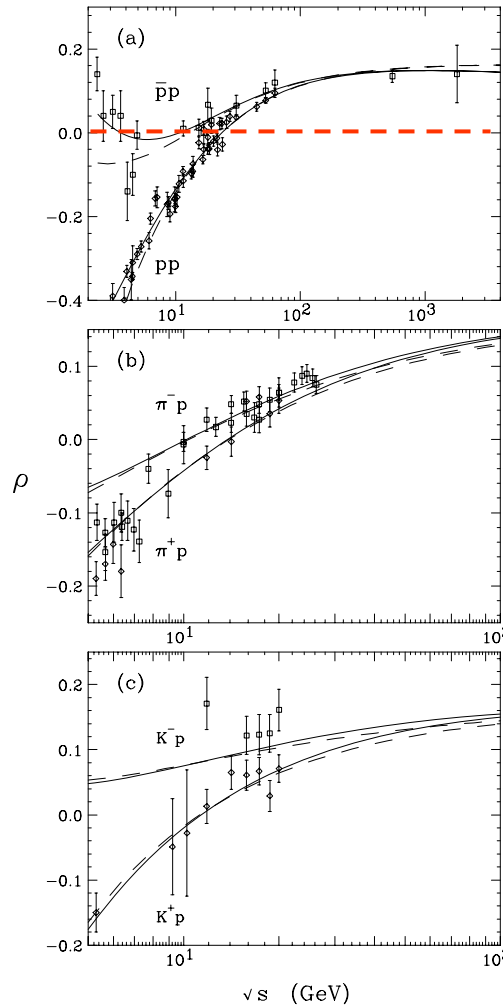
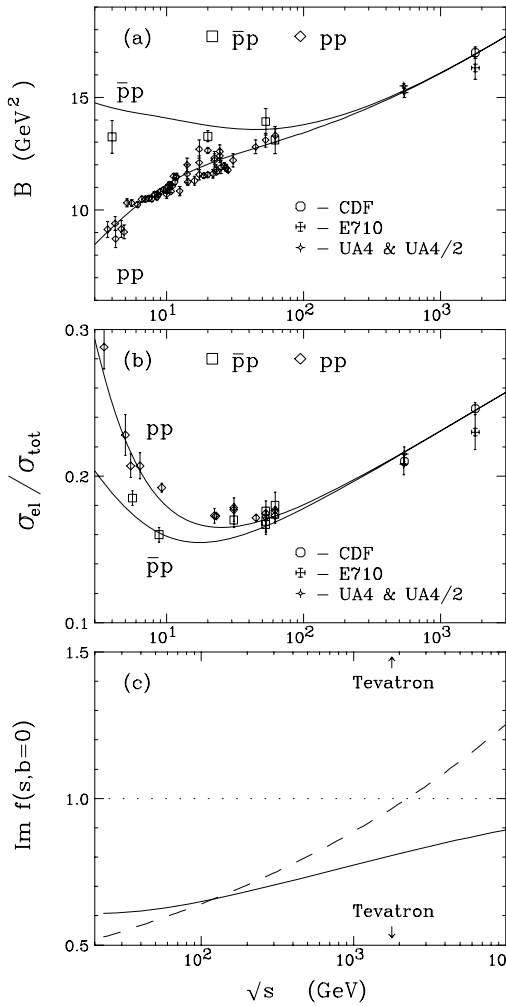
$$\sigma \rightarrow s^\epsilon$$

$$\epsilon = 1.104 \pm 0.002$$

$$\rightarrow \sigma_{LHC} = 115 \text{ mb}$$

@14 TeV

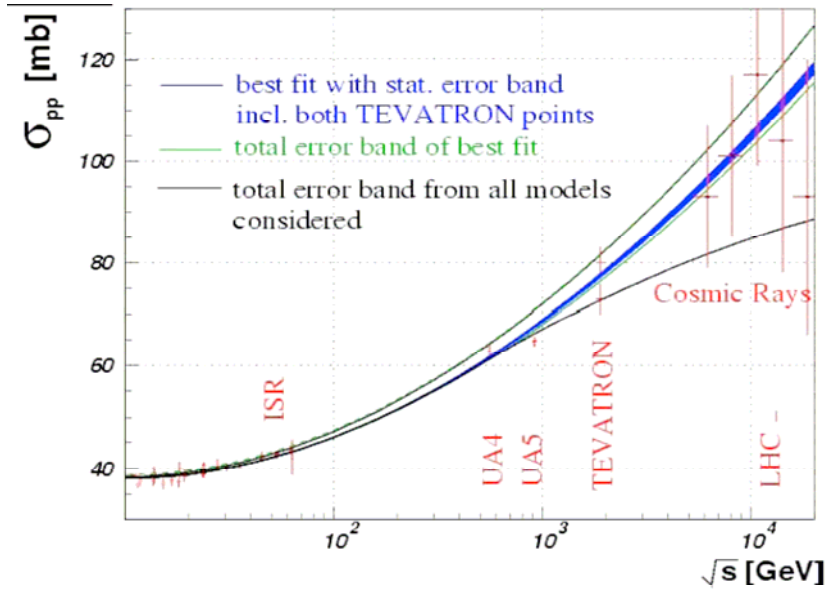
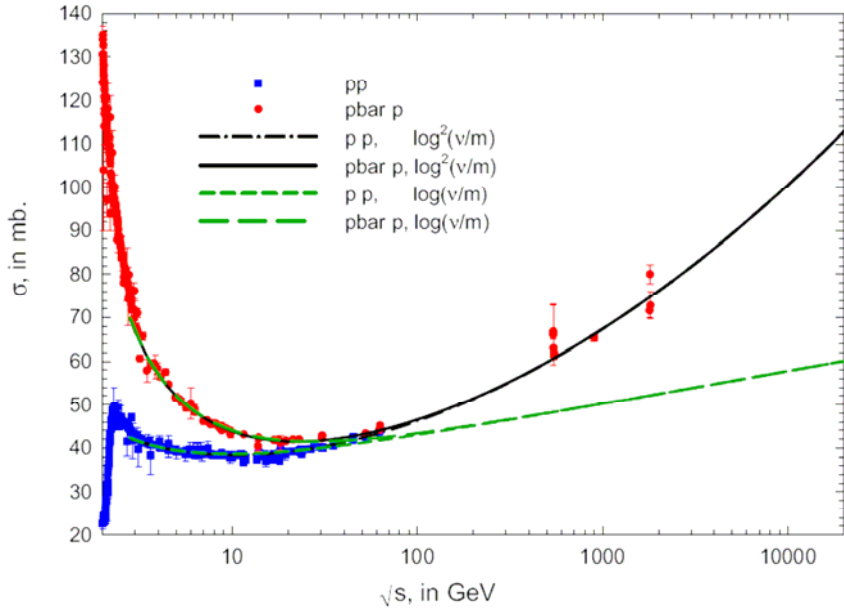
Elastic/Total and ρ -values: Regge fit



Covolan, Montagna, and G
PLB 389 (1995) 176

- Agreement with data on:
 - b -slopes
 - σ_{el}/σ_T
 - ρ -values
- Unitarity assured

Other Approaches



COMPETE Collaboration fits all available hadronic data and predicts

LHC: $\sigma_{tot} = 111.5 \pm 1.2 \begin{matrix} +4.1 \\ -2.1 \end{matrix} \text{ mb}$ [PRL 89 201801 (2002)]

eg, M. Block, arXiv:hep-ph/0601210 (2006)

→ fit data using analyticity constraints
M. Block and F. Halzen, Phys. Rev. D **72**, 036006

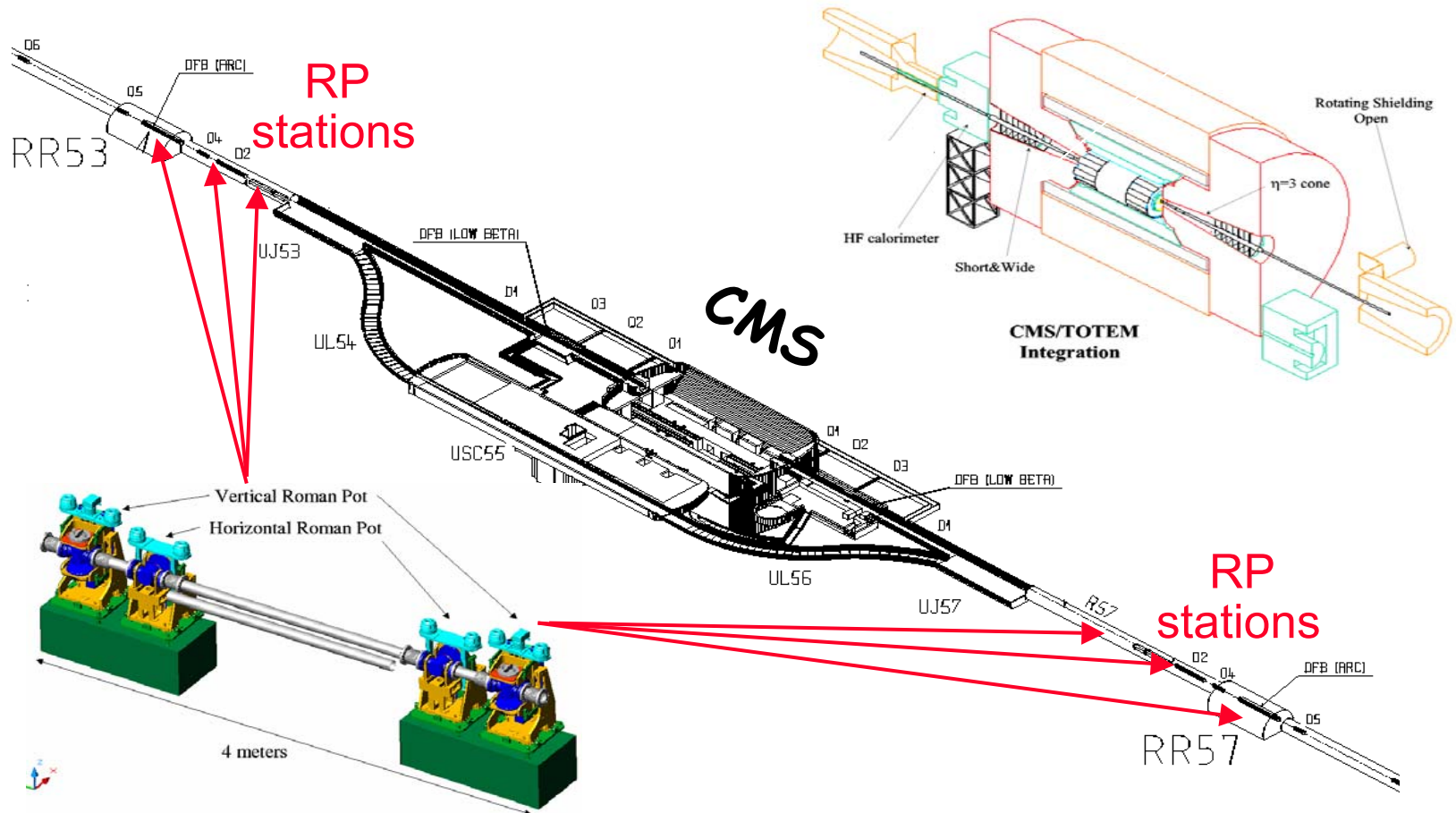
$\sigma_T(\text{LHC}) = 107.3 \pm 1.2 \text{ mb}$

Recall CMG Regge fit: 115 mb

TOTEM experiment @ LHC

Total Cross Section, Elastic Scattering, and Diffraction Dissociation

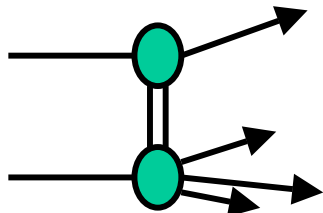
Aim at 1% accuracy on σ_T



DIFFRACTION

- Soft & hard diffraction
- Factorization / renormalization
- Multi-gap diffraction
- Diffraction in QCD
- Dark energy ???

A unitarity issue



Factorization \rightarrow

$$\frac{d^2 \sigma_{SD}}{dt d\xi} = f_{IP/p}(t, \xi) \cdot \sigma_{IP-\bar{p}}(M_X^2)$$

Pomeron flux \uparrow

$$\sigma_{SD} \sim S^{2\varepsilon}$$

❖ Regge theory

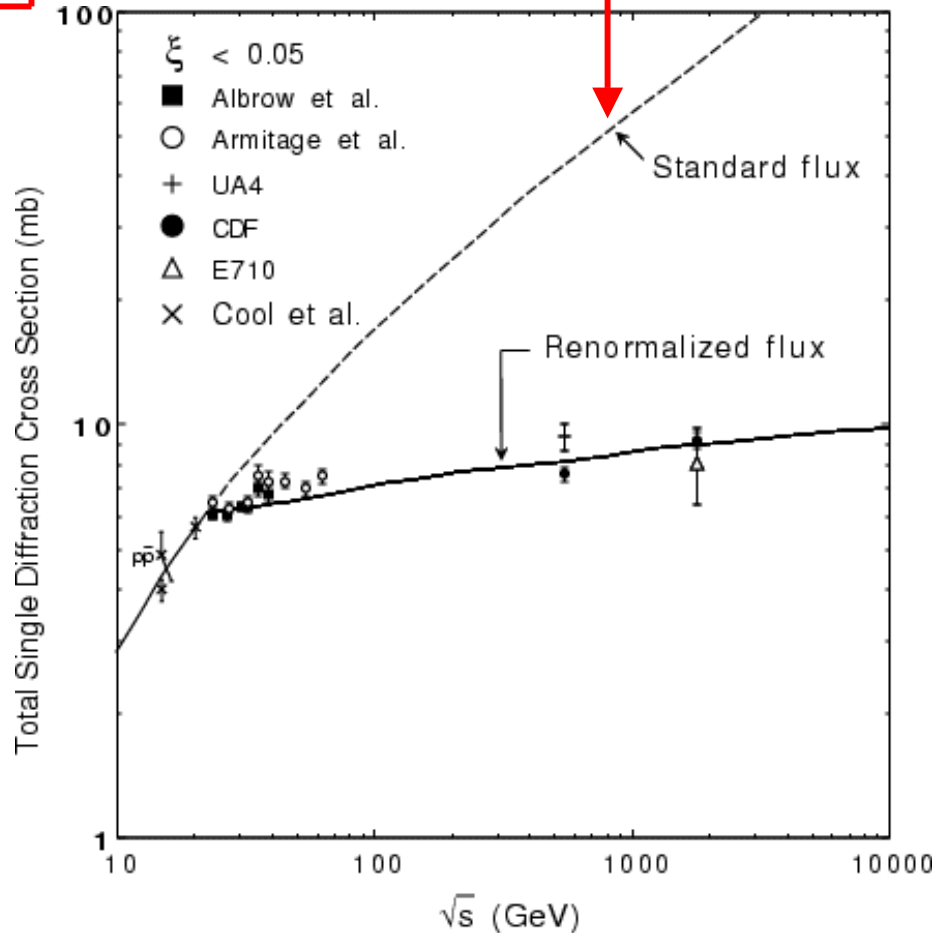
σ_{SD} exceeds σ_T at
 $\sqrt{s} \approx 2 \text{ TeV}$.

❖ Renormalization

Pomeron flux integral
 (re)normalized to unity

KG, PLB 358 (1995) 379

$$\int_{\xi_{\min}}^{0.1} \int_{t=-\infty}^0 f_{IP/p}(t, \xi) d\xi dt = 1$$



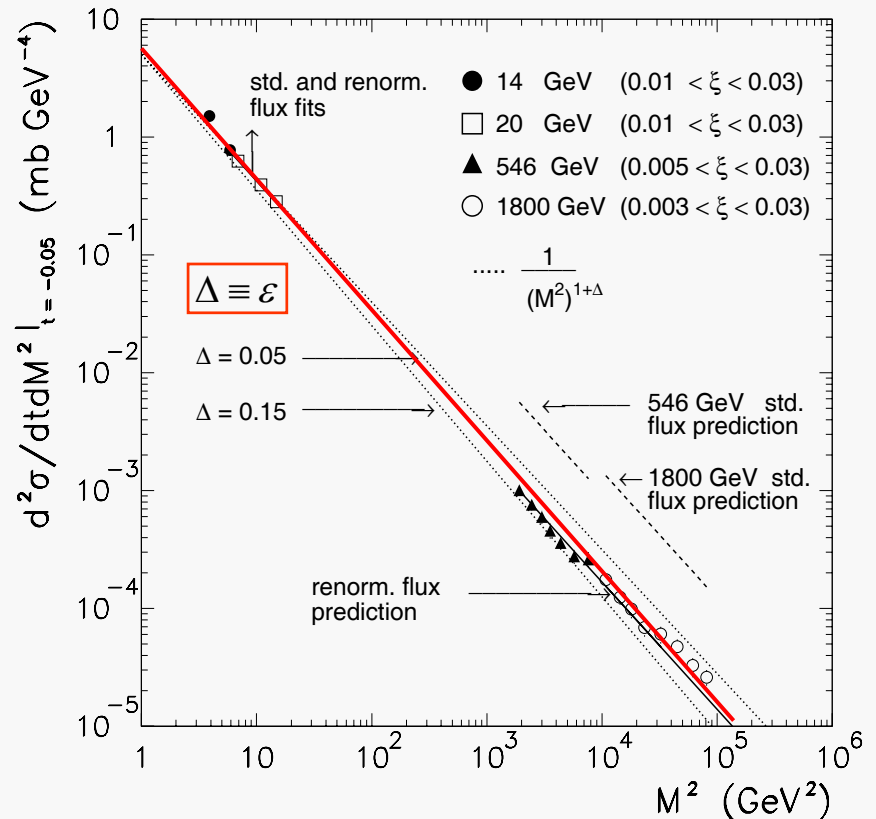
A Scaling Law in Diffraction

KG&JM, PRD 59 (1999) 114017

renormalization

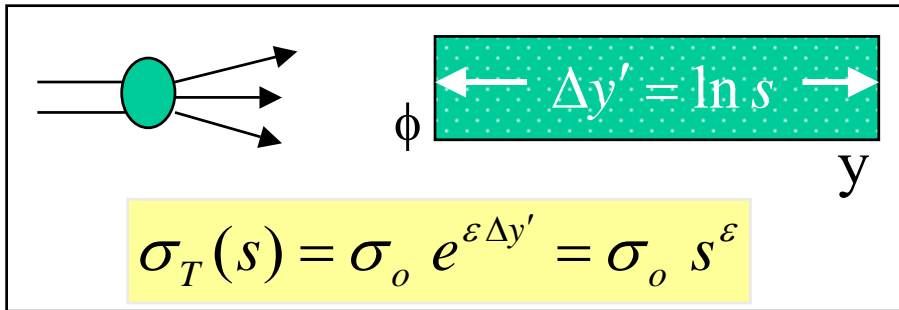
$$\frac{d\sigma}{dM^2} \propto \frac{s^{2\varepsilon} \rightarrow 1}{(M^2)^{1+\varepsilon}}$$

→ Independent of S over 6 orders of magnitude in M²!



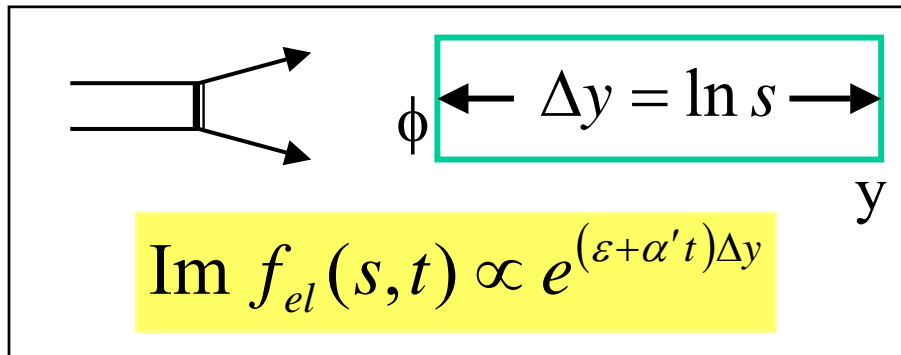
Factorization breaks down so as to ensure M²-scaling!

The QCD Connection

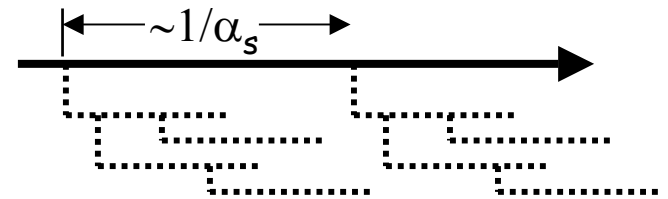


The exponential rise of $\sigma_T(\Delta y')$ is due to the increase of wee partons with $\Delta y'$

(E. Levin, An Introduction to Pomerons, Preprint DESY 98-120)



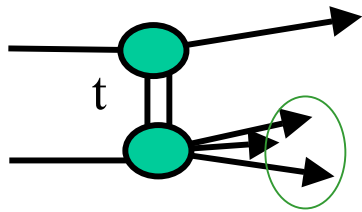
Total cross section:
power law increase versus s



Elastic cross section:
forward scattering amplitude

Single Diffraction in QCD

(KG, hep-ph/0205141)



$$\left. \frac{d\sigma}{dM^2} \right|_{\text{REGGE}} \propto \frac{s^{2\varepsilon}}{(M^2)^{1+\varepsilon}}$$

2 independent variables: $t, \Delta y$

$$\frac{d^2\sigma}{dt d\Delta y} = \underbrace{C \cdot F_p^2(t) \cdot \left\{ e^{(\varepsilon + \alpha' t) \Delta y} \right\}^2}_{\text{Gap probability}} \cdot \underbrace{\kappa \cdot \left\{ \sigma_0 e^{\varepsilon \Delta y'} \right\}}_{\text{color factor}}$$

Gap probability

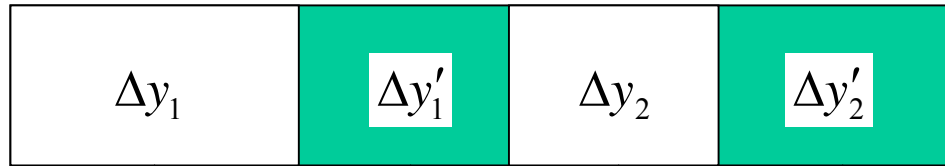
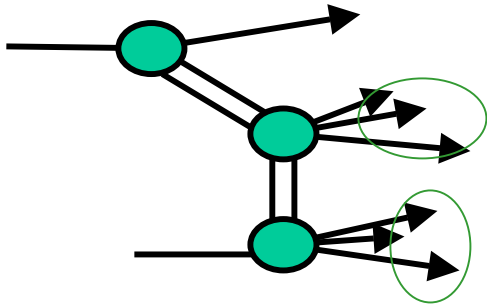
$$\sim e^{2\varepsilon \Delta y}$$

$$\int_{\Delta y_{\min}}^{\Delta y = \ln s} s^{2\varepsilon \Delta y} \approx s^{2\varepsilon}$$

Renormalization removes the s-dependence → SCALING

Multi-gap Renormalization

(KG, hep-ph/0205141)



5 independent variables

$$\left\{ \begin{array}{c} t_1 \\ \Delta y = \Delta y_1 + \Delta y_2 \\ t_2 \end{array} \right.$$

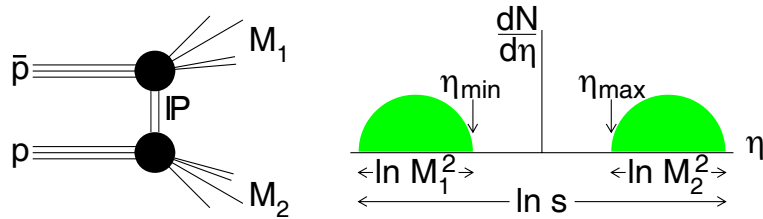
color factors

$$\frac{d^5 \sigma}{\prod_{i=1-5} dV_i} = \underbrace{C \times F_p^2(t_1) \prod_{i=1-2} \left\{ e^{(\varepsilon + \alpha' t_i) \Delta y_i} \right\}^2}_{\text{Gap probability} \sim e^{2\varepsilon \Delta y}} \times \underbrace{\kappa^2 \left\{ \sigma_o e^{\varepsilon(\Delta y'_1 + \Delta y'_2)} \right\}}_{\text{Sub-energy cross section (for regions with particles)}}$$

$$\int_{\Delta y_{\min}}^{\Delta y = \ln s} s^{2\varepsilon \Delta y} \approx s^{2\varepsilon}$$

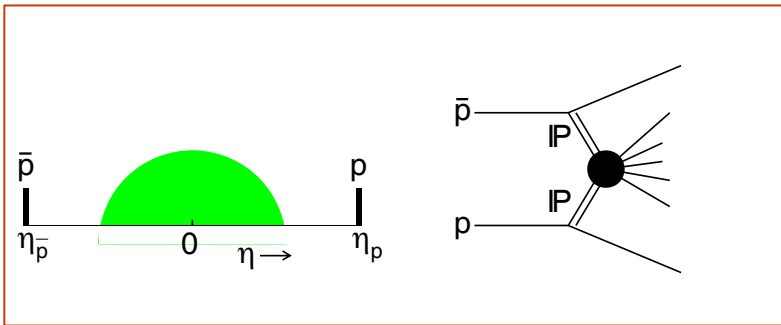
Same suppression as for single gap!

Central and Double Gaps @ CDF



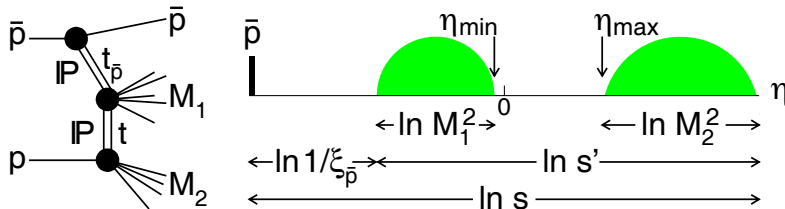
□ Double Diffraction Dissociation

➤ One central gap



□ Double Pomeron Exchange

➤ Two forward gaps

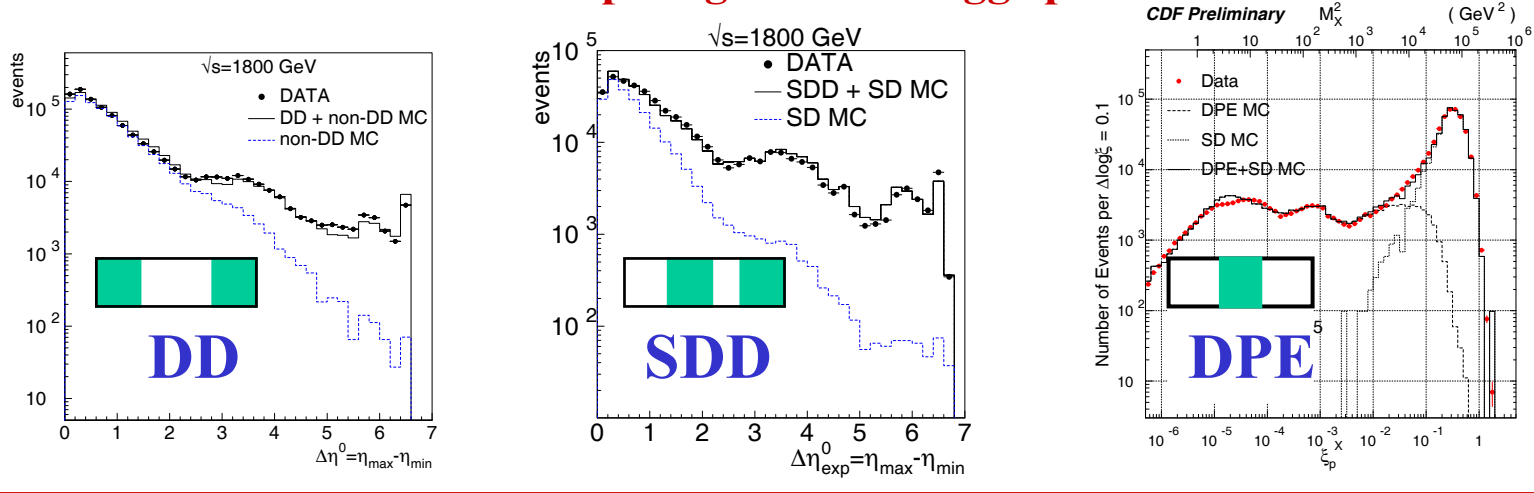


□ SDD: Single+Double Diffraction

➤ One forward + one central gap

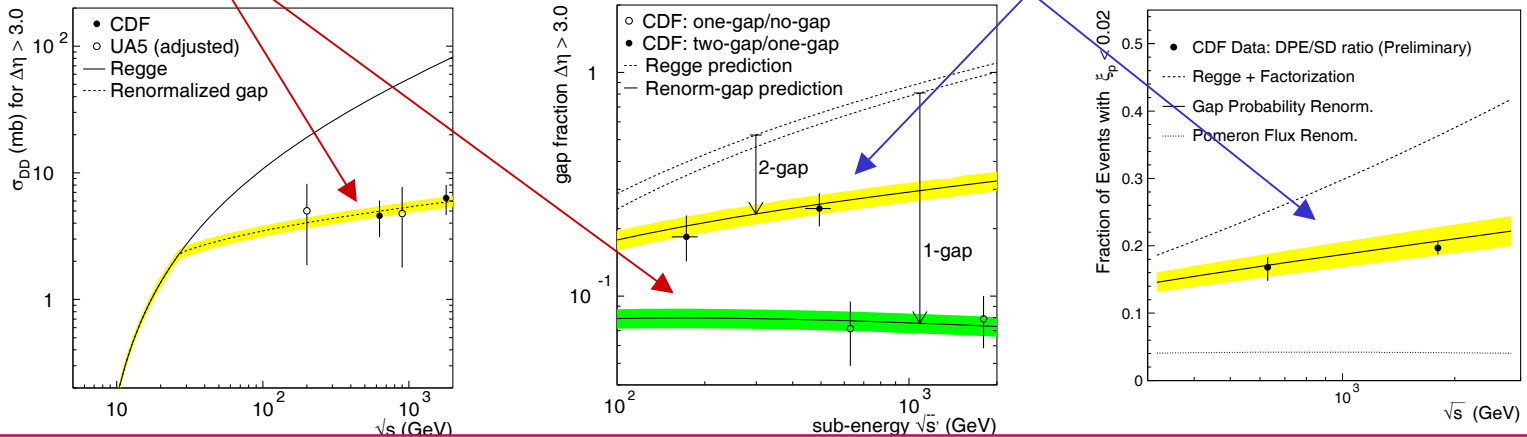
Central & Double-Gap CDF Results

Differential shapes agree with Regge predictions



➤ One-gap cross sections are suppressed

➤ Two-gap/one-gap ratios are $\approx \kappa = 0.17$



Dark Energy

Non-diffractive interactions

Rapidity gaps are formed by multiplicity fluctuations:

$$P(\Delta y) = e^{-\rho \Delta y}, \quad \rho = \frac{dN_{\text{particles}}}{dy}$$

$P(\Delta y)$ is exponentially suppressed

Diffractive interactions

Rapidity gaps at $t=0$ grow with Δy :

$$\Delta y \approx -\ln \xi = \ln s - \ln M^2$$
$$P(\Delta y)|_{t=0} \sim e^{2\varepsilon \Delta y}$$

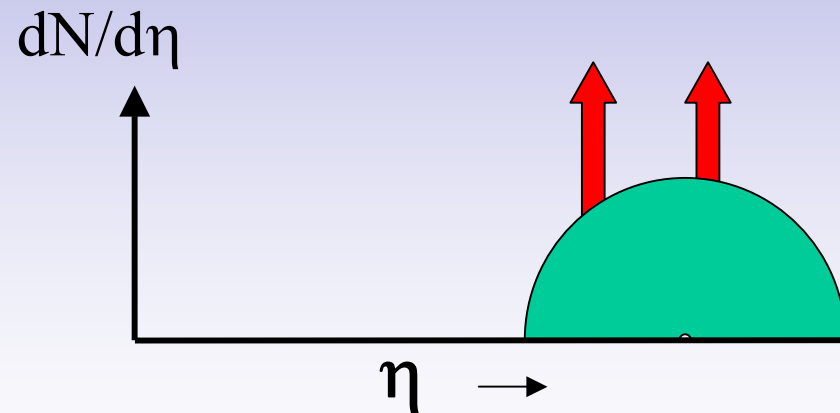
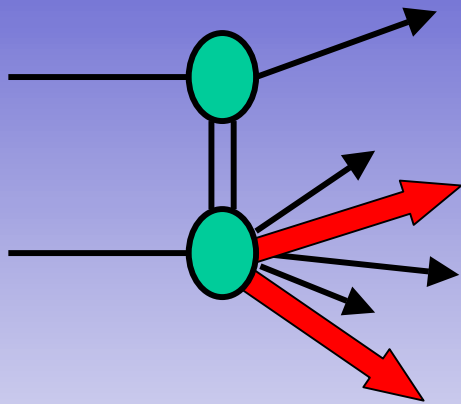
2ε : negative particle density!



Gravitational repulsion?

HARD DIFFRACTION

- Diffractive fractions
- Diffractive structure function
→ factorization breakdown
- Restoring factorization
- Hard diffraction in QCD



JJ, W, b, J/ψ

Diffractive Fractions @ CDF

$$\bar{p}p \rightarrow (\text{☀} + X) + \text{gap}$$

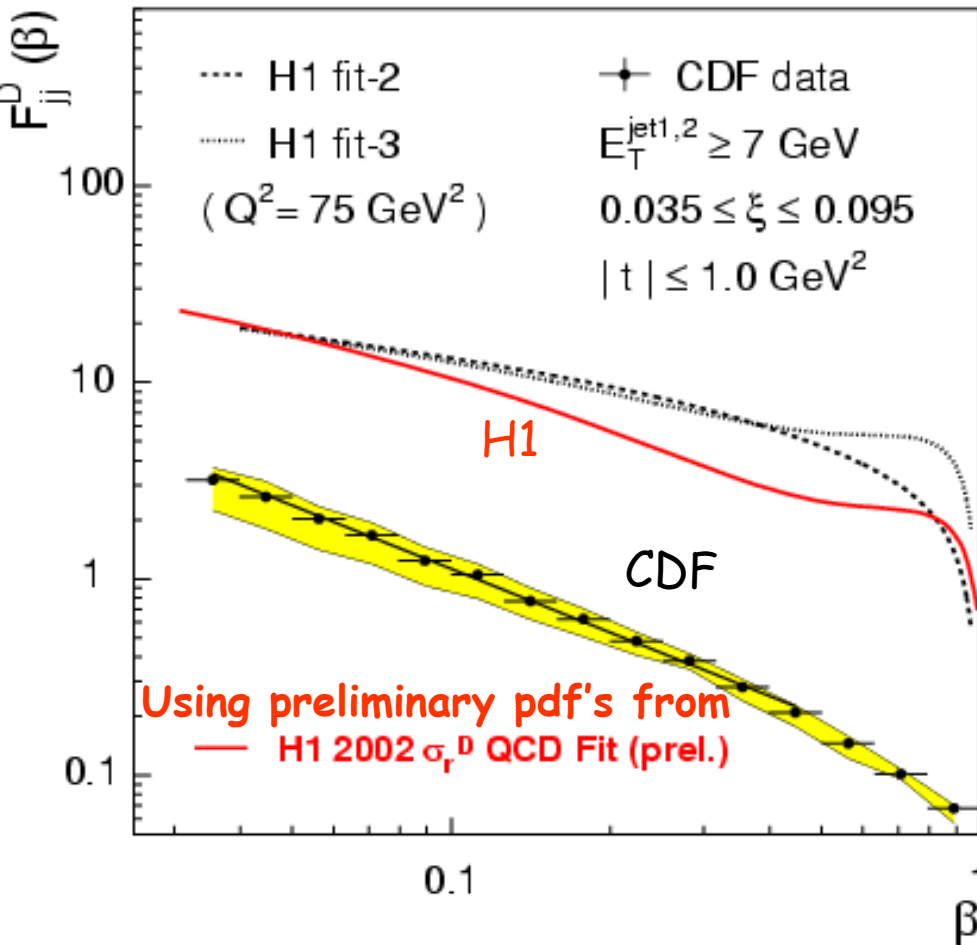
Fraction:
SD/ND ratio
at 1800 GeV

☀	Fraction(%)
W	1.15 (0.55)
JJ	0.75 (0.10)
b	0.62 (0.25)
J/ψ	1.45 (0.25)

All ratios ~ 1%
→ ~ uniform suppression
~ FACTORIZATION!

Diffractive Structure Function:

Breakdown of QCD Factorization

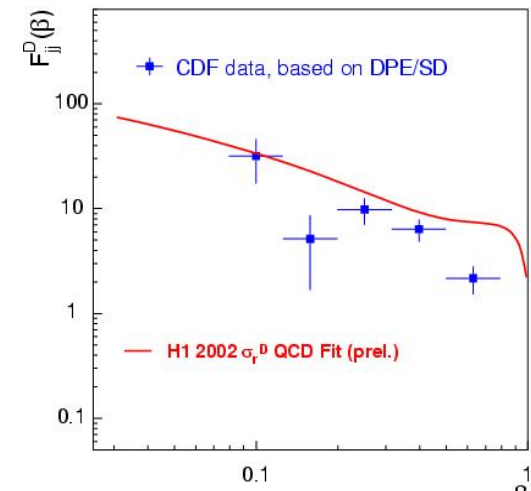
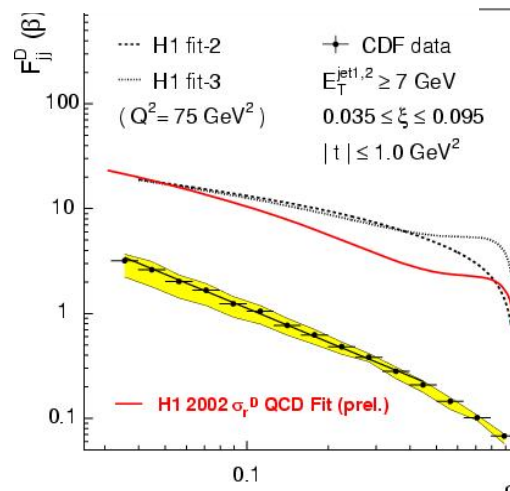
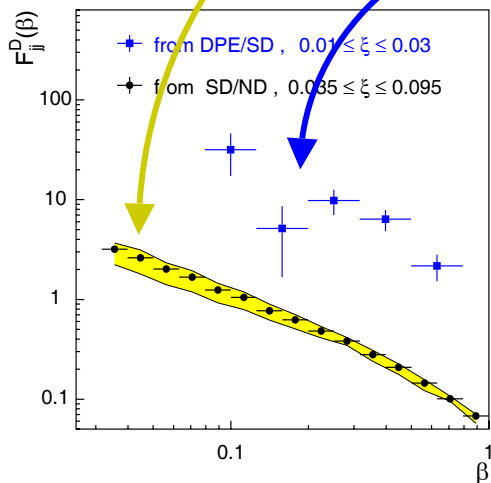
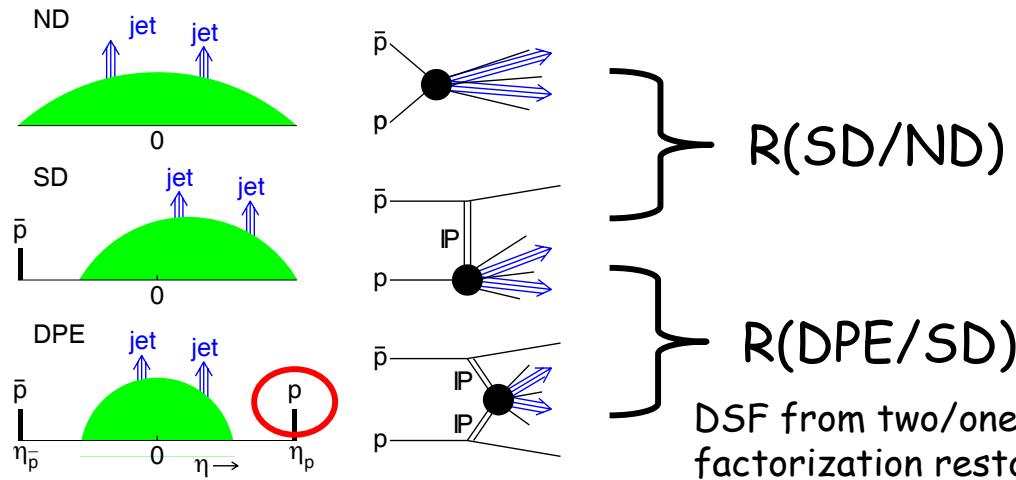


β = momentum fraction
of parton in Pomeron

The diffractive structure function at the Tevatron is suppressed by a factor of ~ 10 relative to expectation from pdf's measured by H1 at HERA

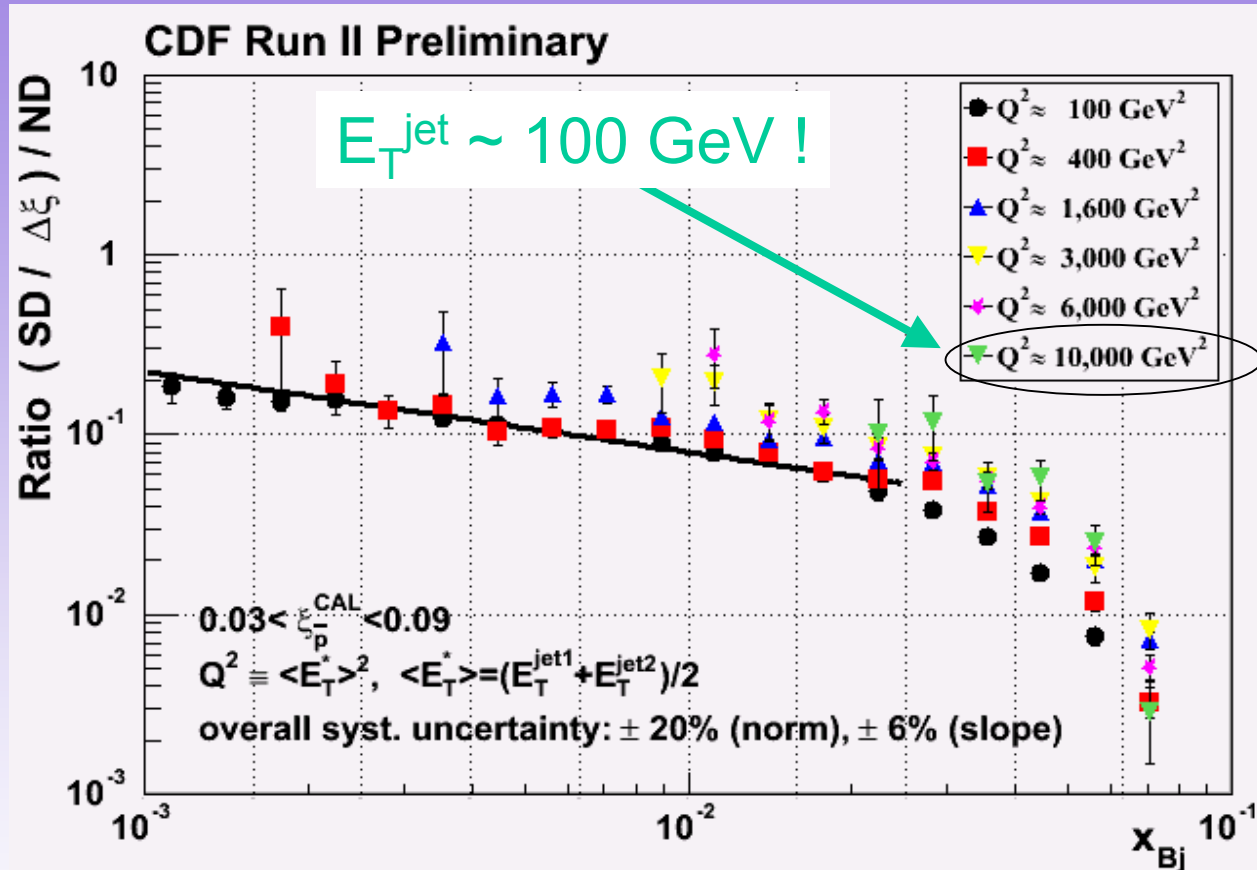
Similar suppression factor
as in soft diffraction
relative to Regge expectations!

Restoring QCD Factorization



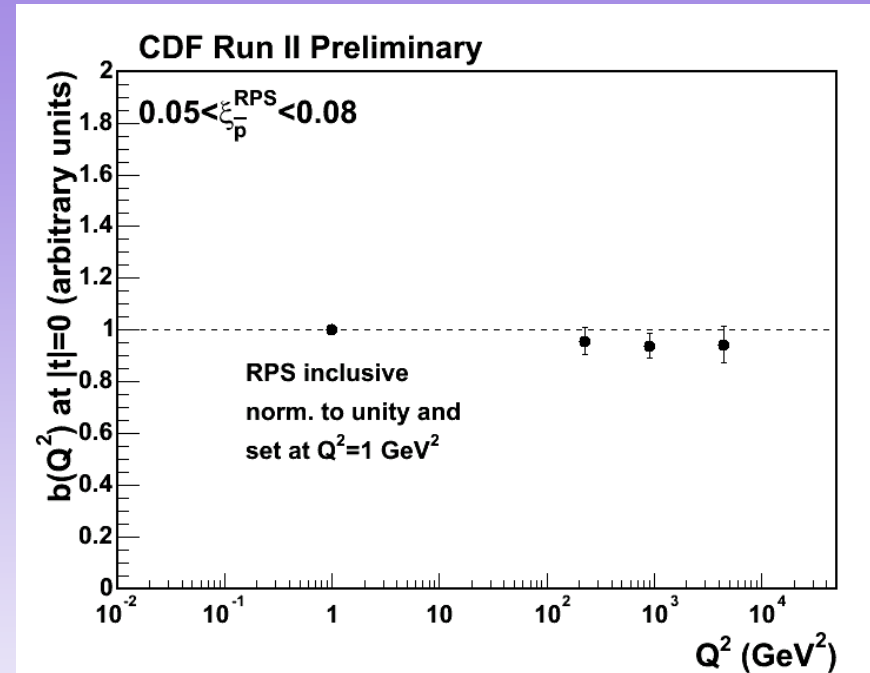
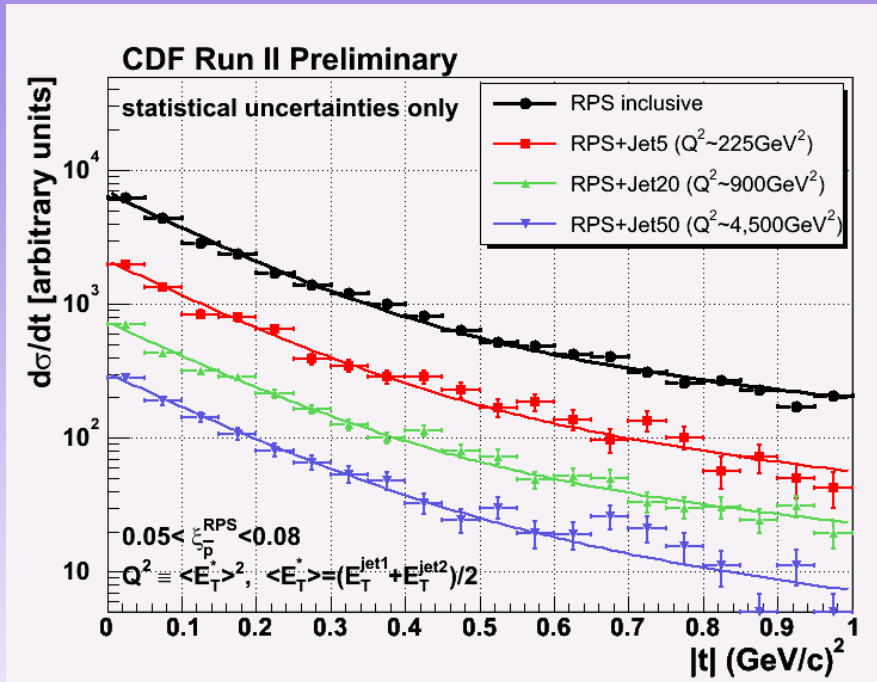
The diffractive structure function measured on the proton side in events with a leading antiproton is NOT suppressed relative to predictions based on DDIS

Diffraction Structure Function: Q² dependence



Small Q^2 dependence in region $100 < Q^2 < 10,000 \text{ GeV}^2$
 \Rightarrow Pomeron evolves as the proton!

Diffraction Structure Function: t- dependence



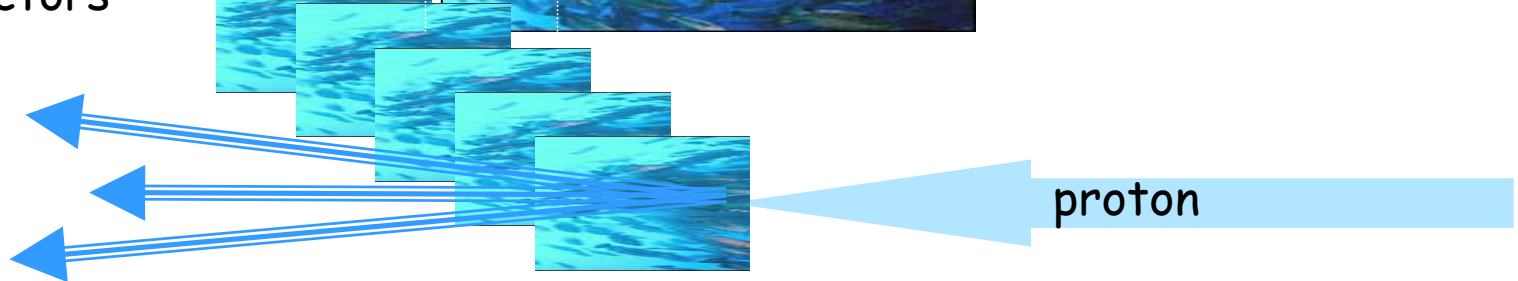
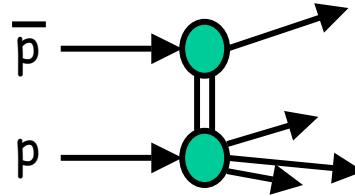
Fit $d\sigma/dt$ to a double exponential:

$$F = 0.9 \cdot e^{b_1 \cdot t} + 0.1 \cdot e^{b_2 \cdot t}$$

- No diffraction dips
- No Q^2 dependence in slope from inclusive to $Q^2 \sim 10^4 \text{ GeV}^2$

- Same slope over entire region of $0 < Q^2 < 4,500 \text{ GeV}^2$ across soft and hard diffraction!

Hard Diffraction in QCD

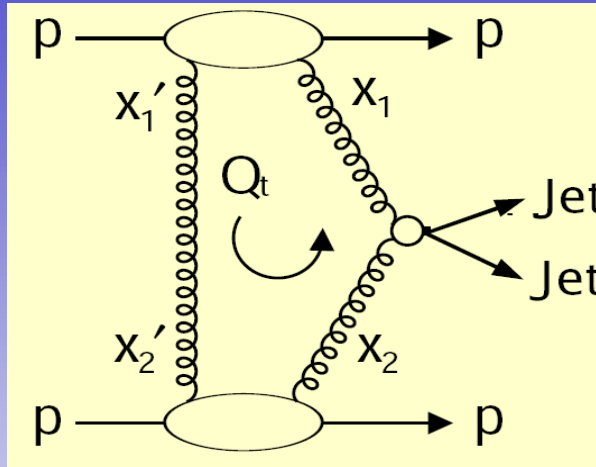


Derive diffractive
from inclusive PDFs
and color factors

EXCLUSIVE PRODUCTION

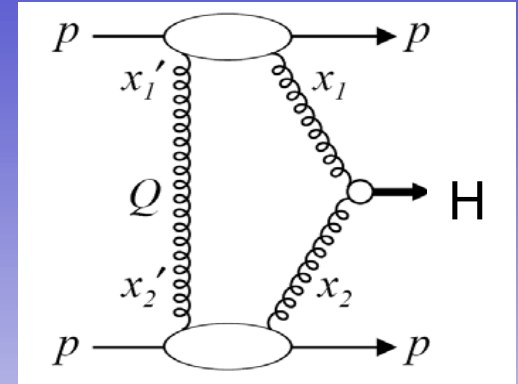
Measure exclusive jj & $\gamma\gamma$ → → →

Calibrate predictions for H production rates @ LHC



[Bialas, Landshoff,](#)
 Phys.Lett. B 256,540 (1991)
[Khoze, Martin, Ryskin,](#)
 Eur. Phys. J. C23, 311 (2002);
 C25,391 (2002);C26,229 (2002)
[C. Royon,](#) hep-ph/0308283
[B. Cox, A. Pilkington,](#)
 PRD 72, 094024 (2005)
 OTHER.....

Clean discovery channel

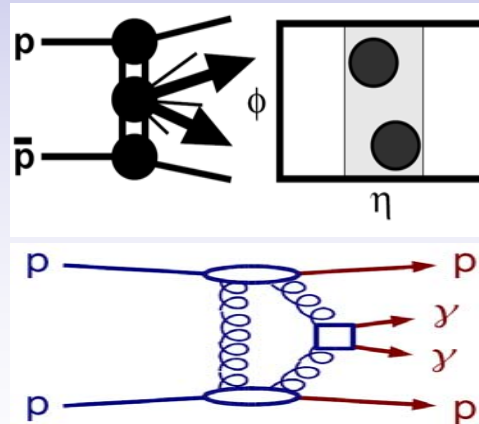


KMR: $\sigma_H(\text{LHC}) \sim 3 \text{ fb}$
 S/B ~ 1 if $\Delta M \sim 1 \text{ GeV}$

Search for exclusive dijets:
 Measure dijet mass fraction

$$R_{jj} = \frac{M_{jj}}{M_X(\text{all calorimeters})}$$

Look for signal as $M_{jj} \rightarrow 1$



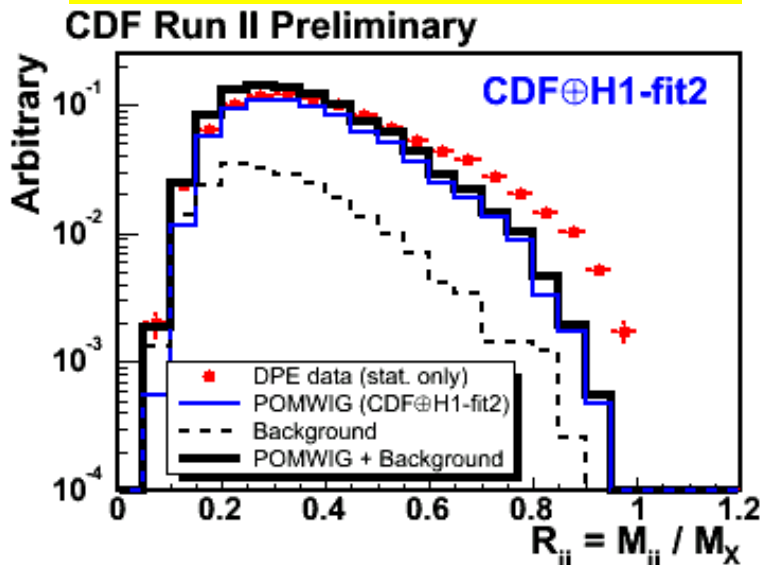
Search for exclusive $\gamma\gamma$

Search for events with two high E_T gammas and no other activity in the calorimeters or BSCs

Exclusive Dijet and $\gamma\gamma$ Search

S T M C H D

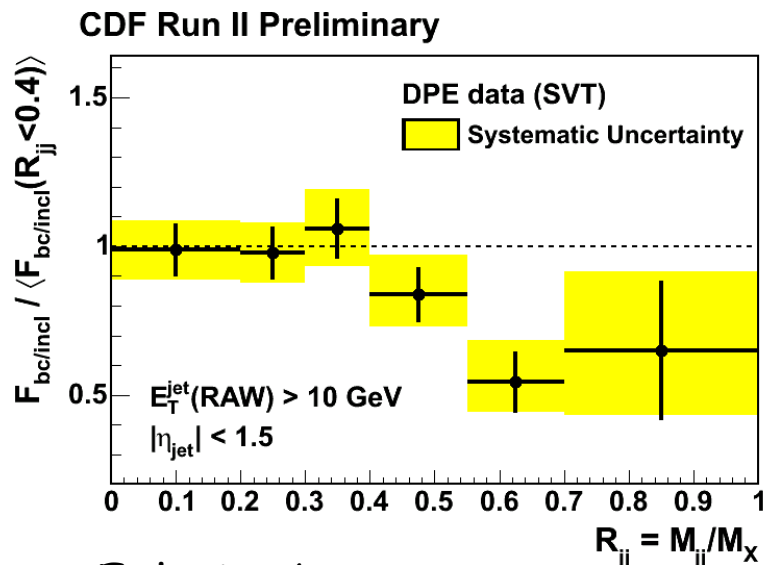
Dijet fraction - all jets



Excess over MC predictions
at large dijet mass fraction

Systematic uncertainties under study: tune in this summer for results

b-tagged dijet fraction



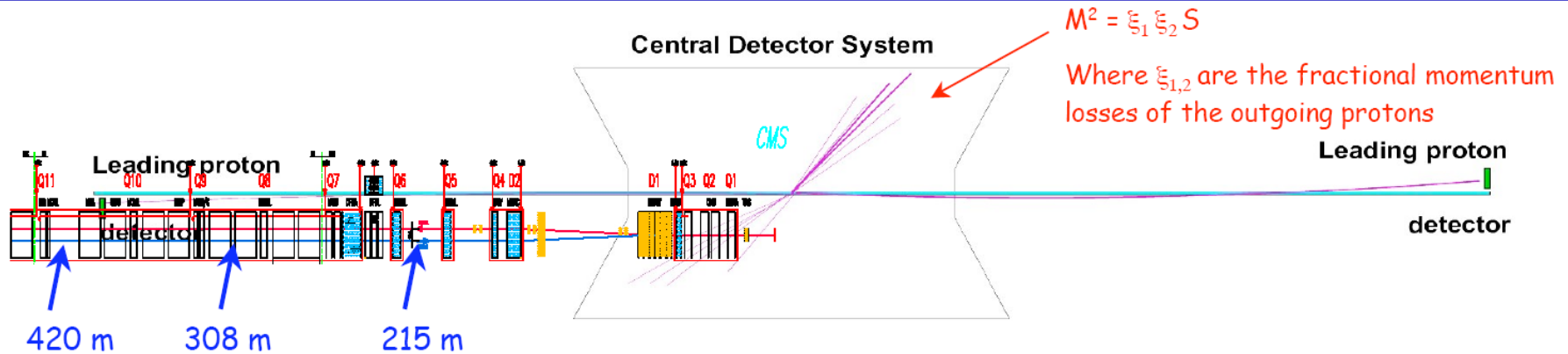
Exclusive b-jets are suppressed
by $J_z = 0$ selection rule

Exclusive $\gamma\gamma$

Based on 3 events observed: $\sigma_{\text{MEAS}} = 0.14_{-0.04}^{+0.14} (\text{stat}) \pm 0.03(\text{syst}) \text{ pb}$

Good agreement with KMR: $\sigma_{\text{KMR}} = 0.04 \pm 0.04 (\times 2 - 3) \text{ pb}$

Looking forward @ LHC



FP420 project

Measure protons at 420 m from the IP during normal high luminosity running to be used in conjunction with CMS and ATLAS

Feasibility study and R&D for Roman Pot detector development

- Physics aim : $pp \rightarrow p + X + p$ (Higgs, New physics, QCD studies)
- Status: Project funded by the UK

Summary

TEVATRON - what we have learnt

- M^2 - scaling
- Non-suppressed double-gap to single-gap ratios
- ➔ Pomeron: composite object made up from underlying pdf's subject to color constraints

LHC - what to do

- Elastic and total cross sections & ρ -value
- High mass ➔ 4 TeV and multi-gap diffraction
- Exclusive production (FP420 project)
 - ➔ Reduced bgnd for std Higgs to study properties
 - ➔ Discovery channel for certain Higgs scenarios