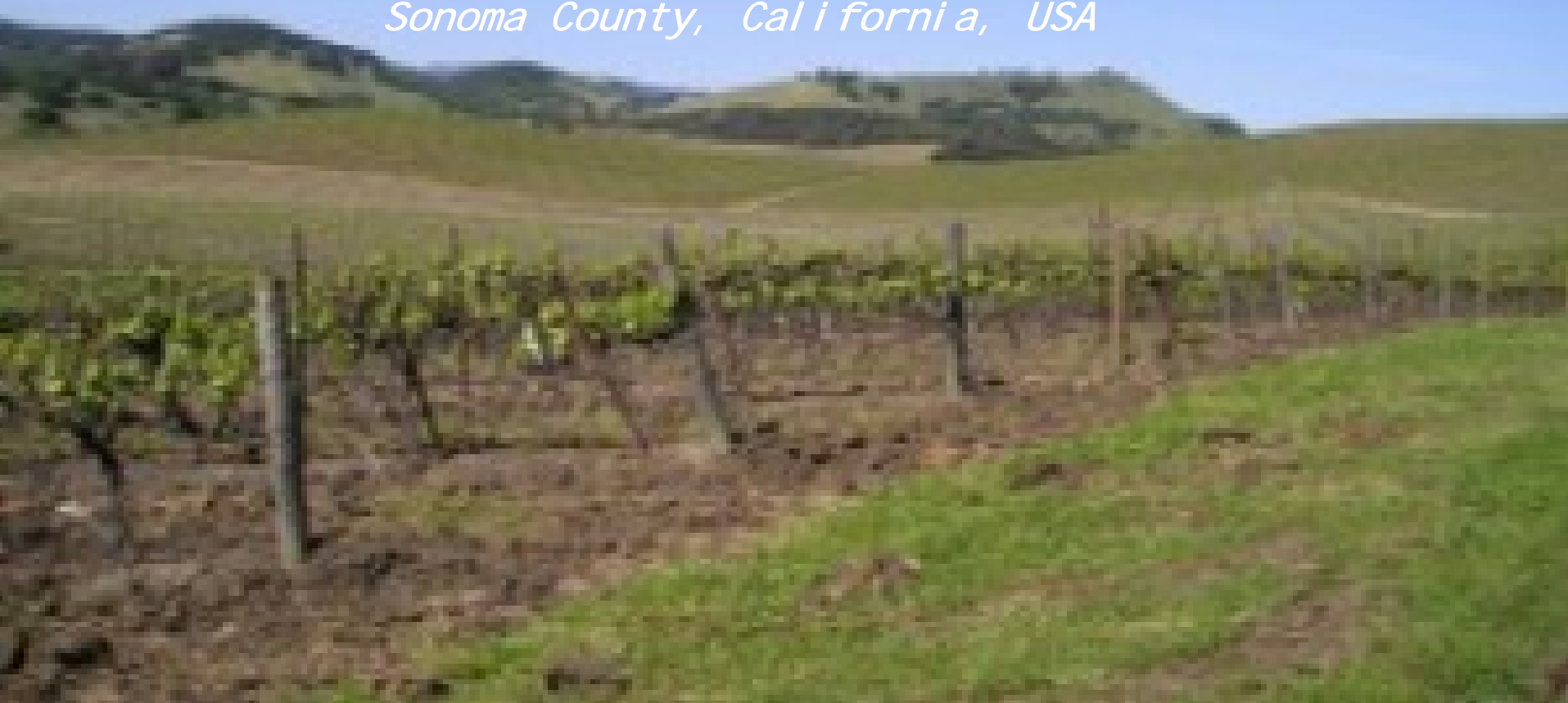


DIFFRACTION FROM THE DEEP SEA

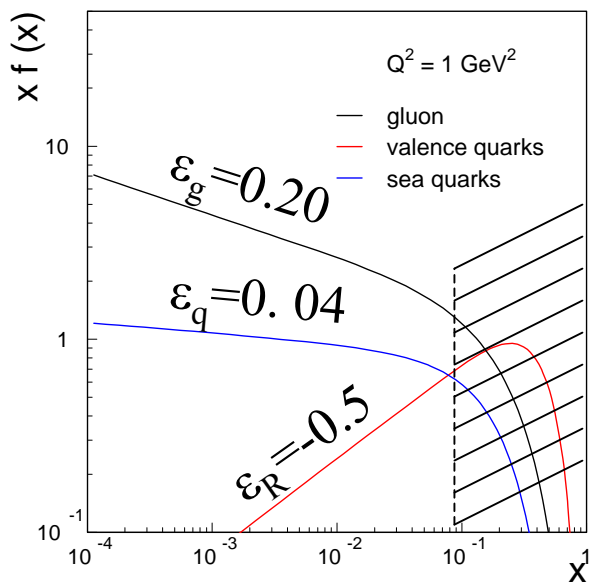
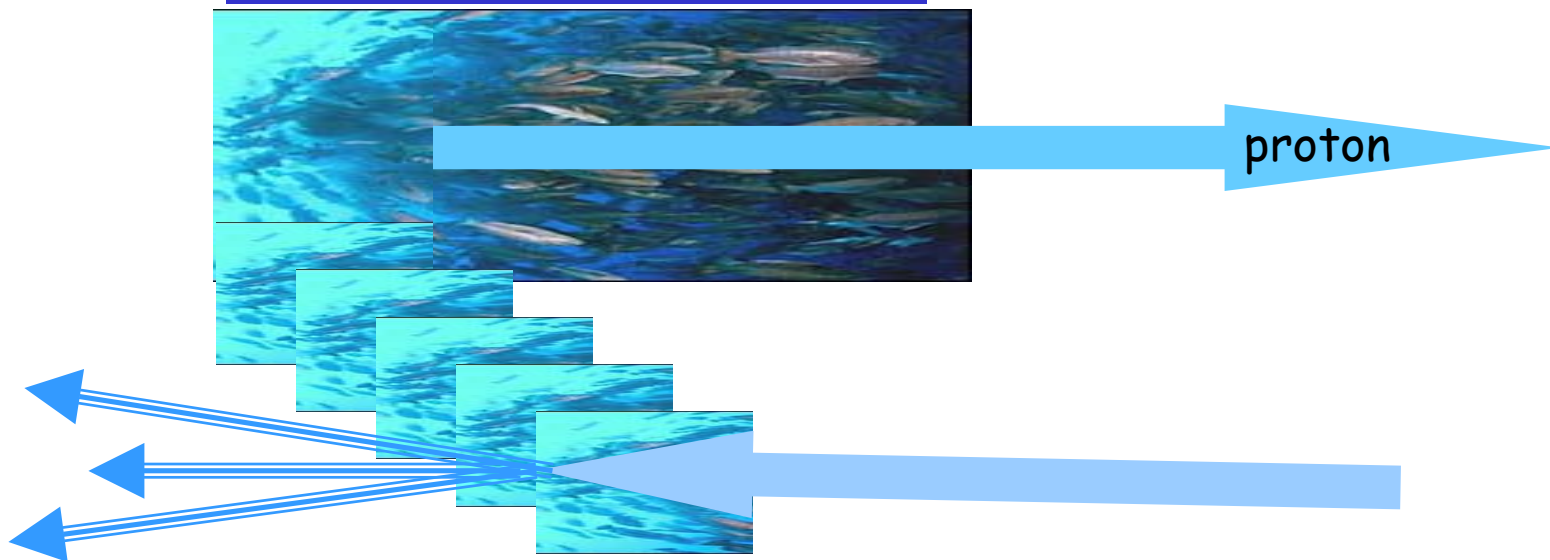
Konstantin Goulianos
The Rockefeller University

ISMD 2004

26 July – 1 August 2004
Sonoma County, California, USA

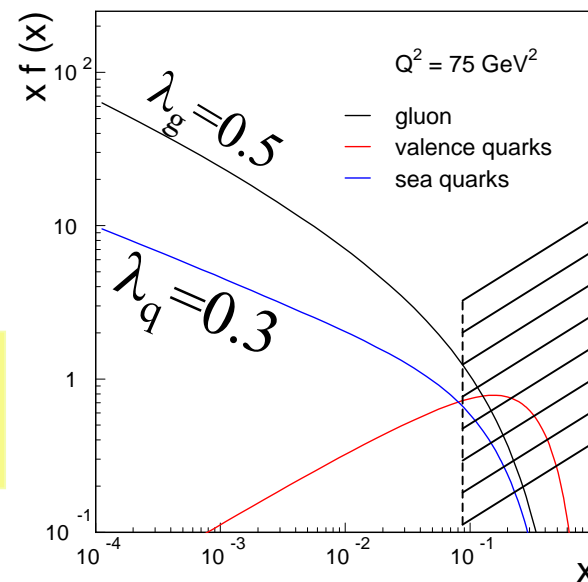


Introduction



in the deep sea

$$x \cdot f(x) = \frac{1}{x \epsilon \text{ (or } \lambda)}$$

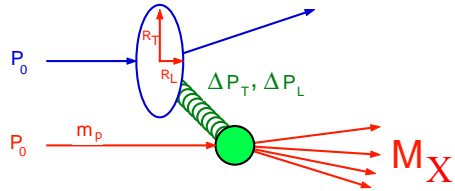


Four Decades of Diffraction

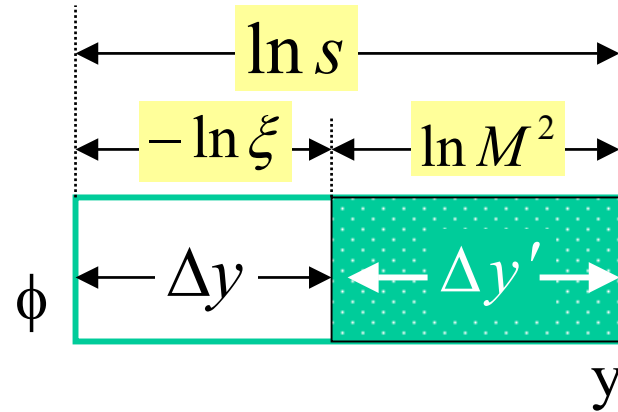
- ✚ 1960's Good and Walker
BNL: first observation
- ✚ 1970's Fermilab fixed target, ISR, SPS
Regge factorization works
KG, Phys. Rep. 101, 169 (1983)
- 1980's UA8: diff. dijets \Rightarrow hard diffraction
- 1990's Tevatron: Regge factorization breakdown
TeV, HERA: QCD factorization breakdown

Soft Diffraction

1/M² law



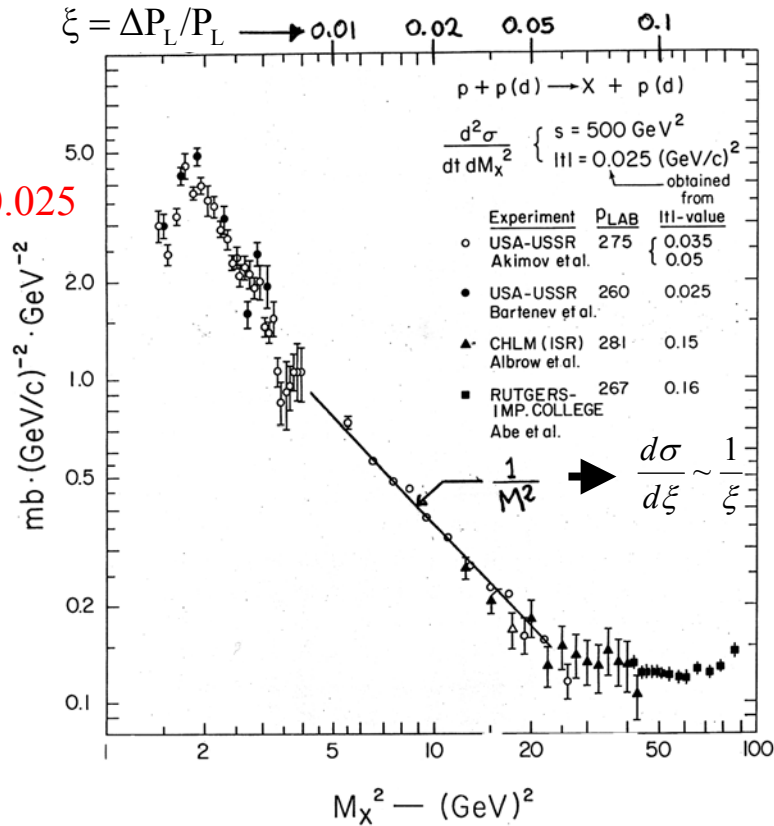
in QCD:



$$\xi = \frac{\Delta p_L}{p_L} = \frac{M^2}{s}$$

$$\frac{d\sigma}{dM^2} \sim \frac{1}{M^2} \Leftrightarrow \frac{d\sigma}{d\Delta y} \propto \text{constant}$$

POMERON: color singlet w/vacuum quantum numbers



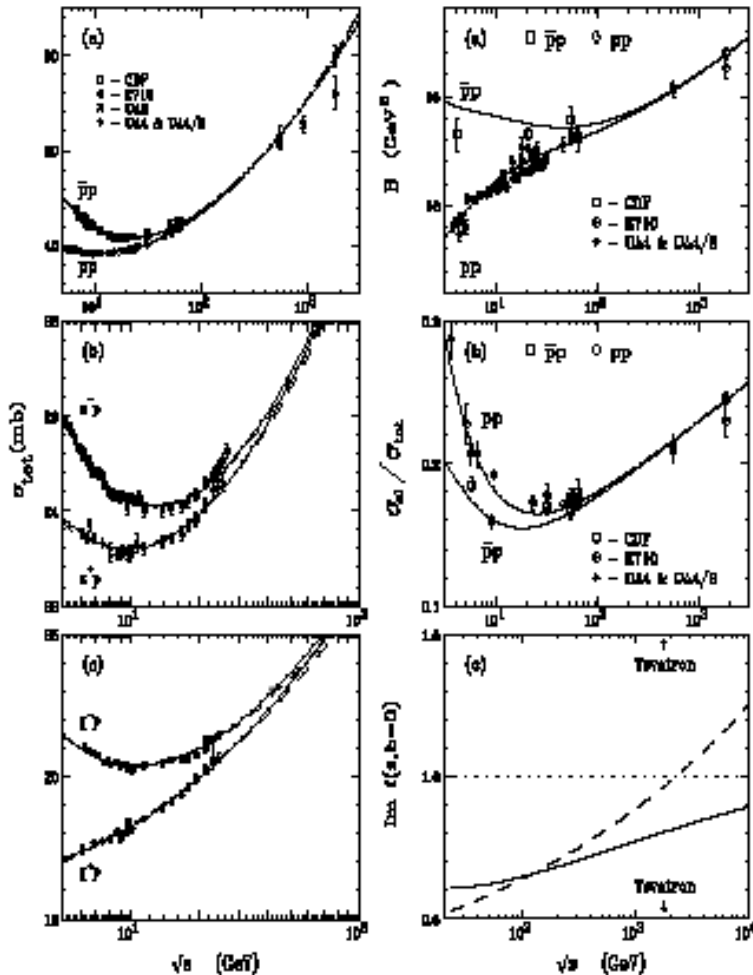
KG, Phys. Rep. 101 (1983) 171

Total & Elastic Cross Sections

Total and Elastic Cross Sections

Covolan, Montanha and Goulianos, Phys. Lett. B 389 (1996) 176

$$\alpha_P = 1 + \epsilon (\Rightarrow 0.104) + 0.25t \quad \alpha_{P'} = 0.68 + 0.82t \quad \alpha_{\alpha'P} = 0.46 + 0.92t$$



QCD expectations

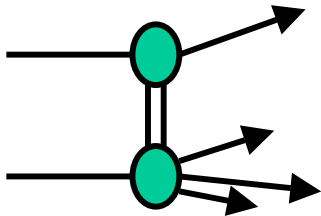
The diagram shows two incoming lines on the left meeting at a green circle vertex. Three lines emerge from the vertex to the right. The top line is labeled ϕ . The right side of the diagram is enclosed in a green box with a dotted pattern, containing the expression $\Delta y' = \ln s$. Below the box, the letter y is written. A yellow box at the bottom contains the equation:

$$\sigma_T(s) = \sigma_0 s^\epsilon = \sigma_0 e^{\epsilon \Delta y'}$$

The exponential rise of $\sigma_T(\Delta y')$ is due to the increase of wee partons with $\Delta y'$
 (see E. Levin, An Introduction to Pomerons, Preprint DESY 98-120)

The diagram shows two incoming lines on the left meeting at a vertex. Two lines emerge from the vertex to the right. The top line is labeled ϕ . The right side of the diagram is enclosed in a green box with a dotted pattern, containing the expression $\Delta y = \ln s$. Below the box, the letter y is written. A yellow box at the bottom contains the equation:

$$\text{Im} f_{el}(s, t) \propto e^{(\epsilon + \alpha' t) \Delta y}$$



Renormalization

$$\frac{d^2\sigma_{SD}}{dt d\xi} = f_{IP/p}(t, \xi) \cdot \sigma_{IP-\bar{p}}(M_X^2)$$

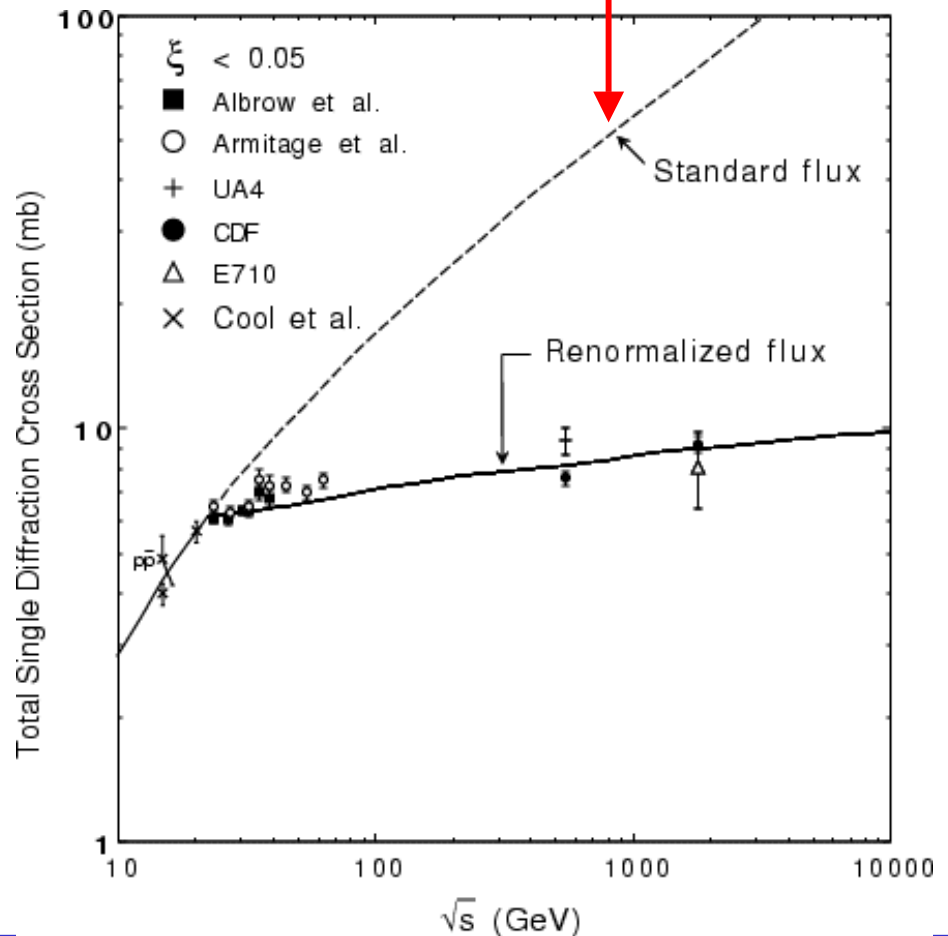
$$\sigma_{SD} \sim S^{2\varepsilon}$$

❖ Unitarity problem:
 With factorization and std pomeron flux σ_{SD} exceeds σ_T at $\sqrt{s} \approx 2 \text{ TeV}$.

❖ Renormalization:
 normalize the Pomeron flux to unity

KG, PLB 358 (1995) 379

$$\int_{\xi_{\min}}^{0.1} \int_{t=-\infty}^0 f_{IP/p}(t, \xi) d\xi dt = 1$$



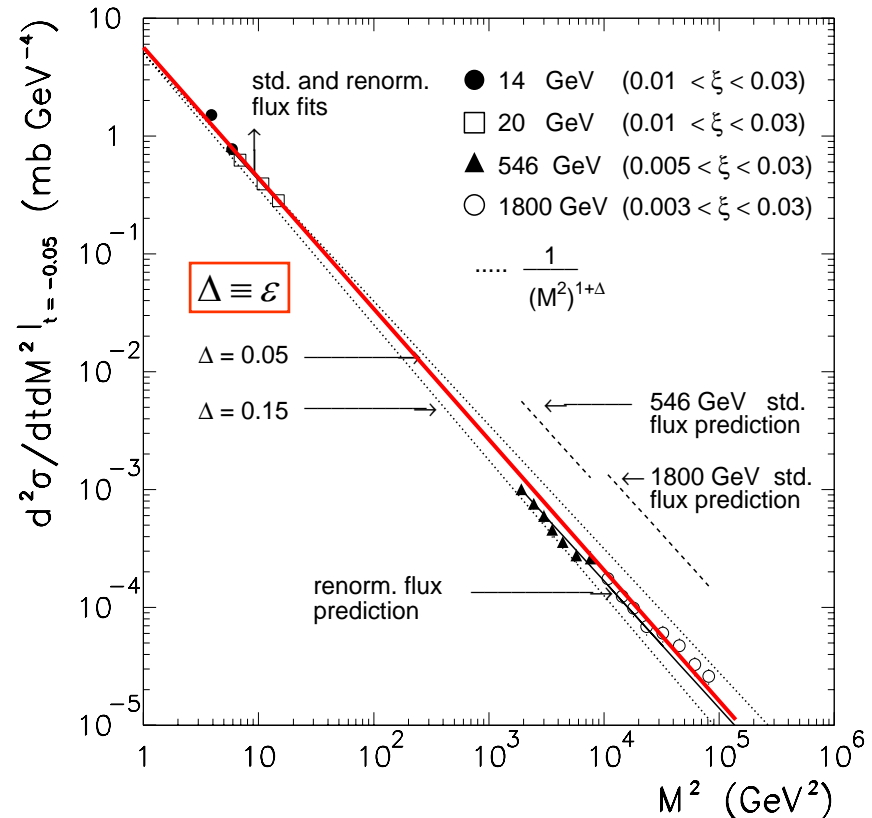
A Scaling Law in Diffraction

Factorization breaks down in favor of M^2 -scaling

renormalization

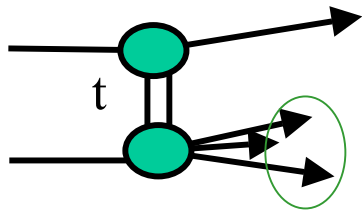
$$\frac{d\sigma}{dM^2} \propto \frac{s^{2\varepsilon} \rightarrow 1}{(M^2)^{1+\varepsilon}}$$

KG&JM, PRD 59 (1999) 114017



Partonic Basis of Renormalization

(KG, hep-ph/0205141)



2 independent variables: $t, \Delta y$

color factor

$$\kappa = \frac{g_{IP-IP-IP}(t)}{\beta_{IP-p-p}(0)} \approx 0.17$$

$$\frac{d^2\sigma}{dt d\Delta y} = \underbrace{C \cdot F_p^2(t_1)}_{\text{Gap probability}} \cdot \left\{ e^{(\varepsilon + \alpha' t)\Delta y} \right\}^2 \cdot \underbrace{\kappa \cdot \left\{ \sigma_0 e^{\varepsilon \Delta y'} \right\}}_{\text{color factor}}$$

Gap probability

$$\sim e^{2\varepsilon \Delta y}$$

$$\int_{\Delta y_{\min}}^{\Delta y = \ln s} s^{2\varepsilon \Delta y} \approx s^{2\varepsilon}$$

Renormalization removes the s-dependence → SCALING

The Factors K and ε

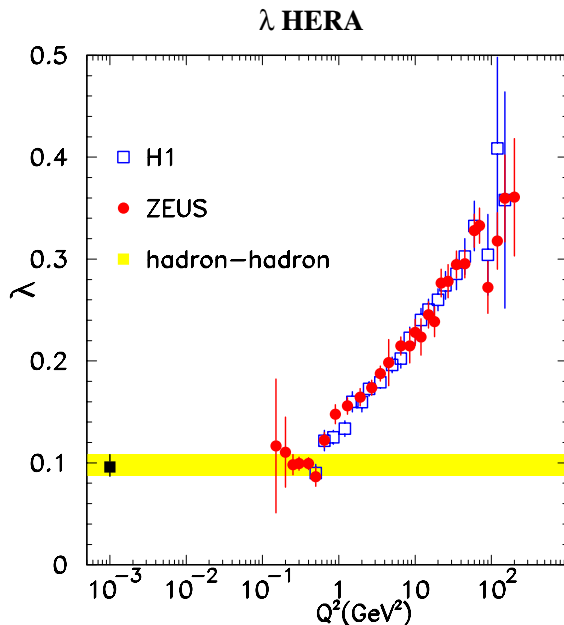
Experimentally:

$$K = \frac{g_{IP-IP-IP}}{\beta_{IP-p}} = 0.17 \pm 0.02, \quad \varepsilon = 0.104$$

KG&JM, PRD 59 (114017) 1999

Color factor:
$$K = f_g \times \frac{1}{N_c^2 - 1} + f_q \times \frac{1}{N_c} \xrightarrow{Q^2=1} \approx 0.75 \times \frac{1}{8} + 0.25 \times \frac{1}{3} = 0.18$$

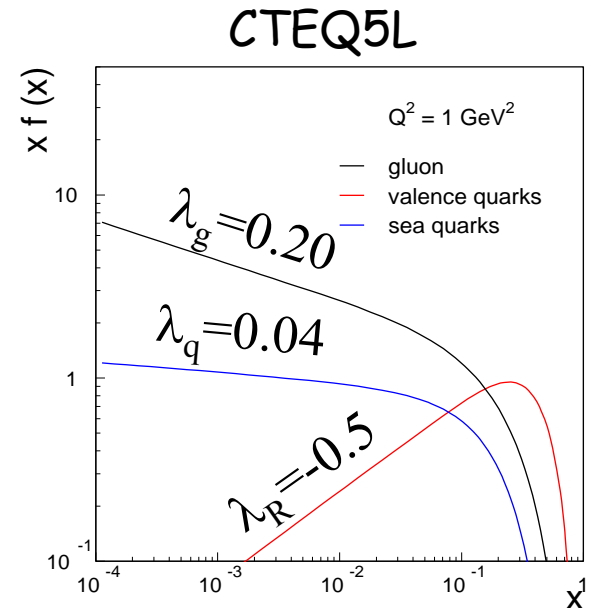
Pomeron intercept:
$$\varepsilon = \lambda_g \cdot w_g + \lambda_q \cdot w_q = 0.12$$



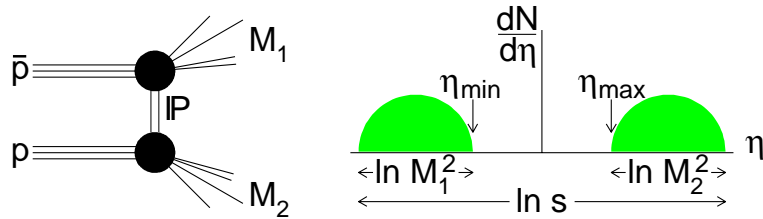
$$x \cdot f(x) = \frac{1}{x^\lambda}$$

f_g = gluon fraction
 f_q = quark fraction

$$\int_{x=1/s}^1 f(x) dx \sim s^\lambda$$

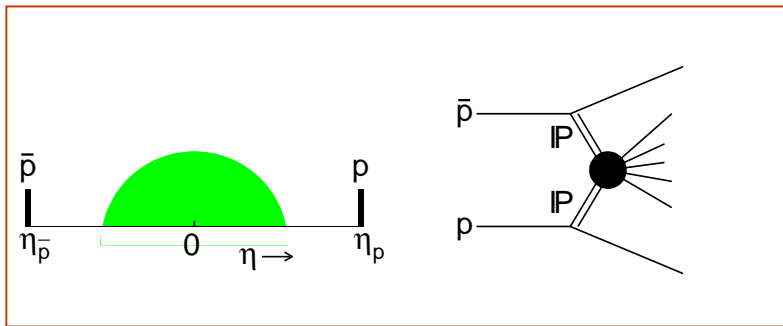


Central and Double Gaps



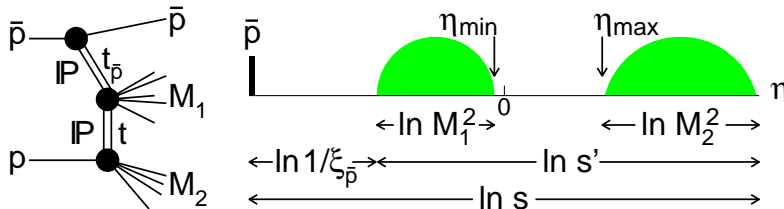
□ Double Diffraction Dissociation

➤ One central gap



□ Double Pomeron Exchange

➤ Two forward gaps

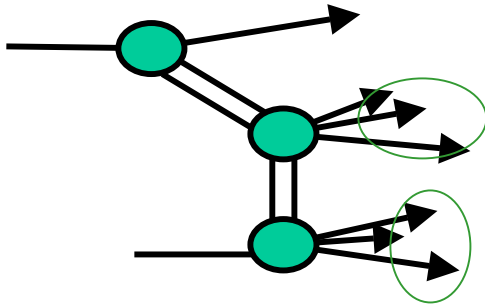


□ SDD: Single+Double Diffraction

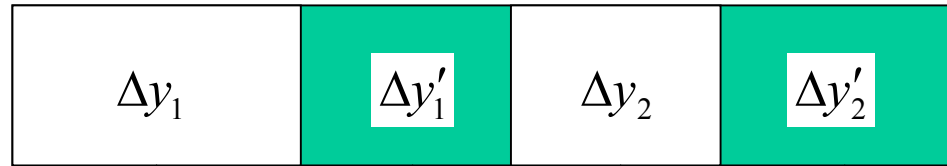
➤ One forward + one central gap

Generalized Renormalization

(KG, hep-ph/0205141)



5 independent variables



y'_1 y_2

t_1 t_2

$$\Delta y = \Delta y_1 + \Delta y_2$$

color factors

$$\frac{d^5 \sigma}{\prod_{i=1-5} dV_i} = C \times F_p^2(t_1) \prod_{i=1-2} \left\{ e^{(\varepsilon + \alpha' t_i) \Delta y_i} \right\}^2 \times \kappa^2 \left\{ \sigma_o e^{\varepsilon(\Delta y'_1 + \Delta y'_2)} \right\}$$

Gap probability
 $\sim e^{2\varepsilon \Delta y}$

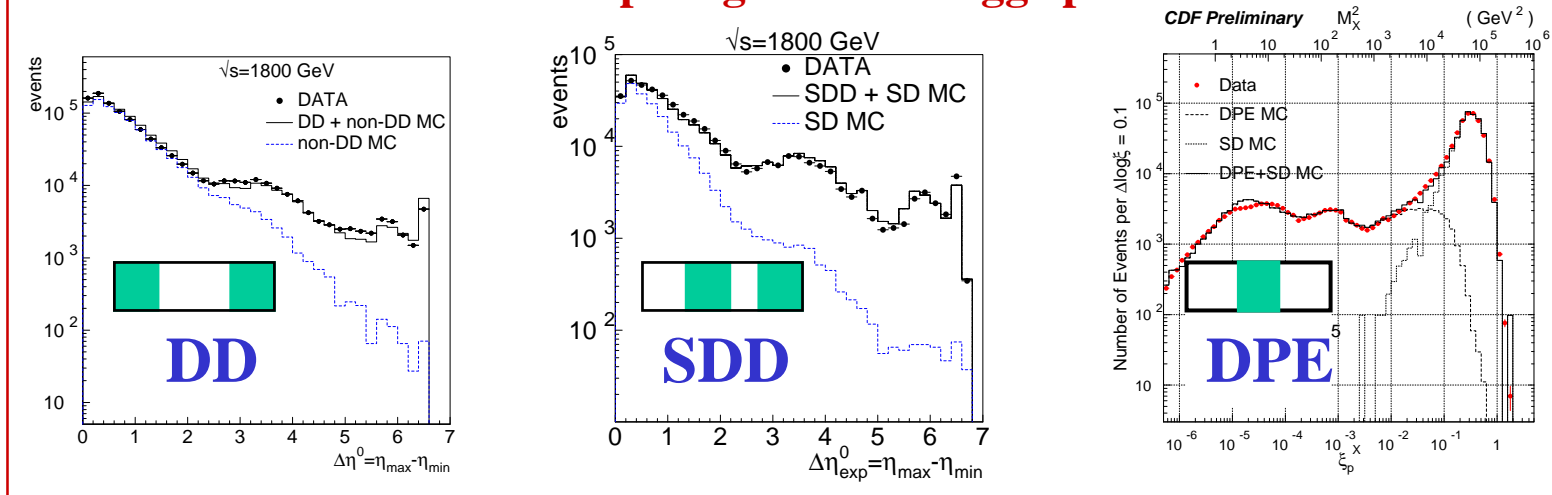
Sub-energy cross section
 (for regions with particles)

$$\int_{\Delta y_{\min}}^{\Delta y = \ln s} s^{2\varepsilon \Delta y} \approx s^{2\varepsilon}$$

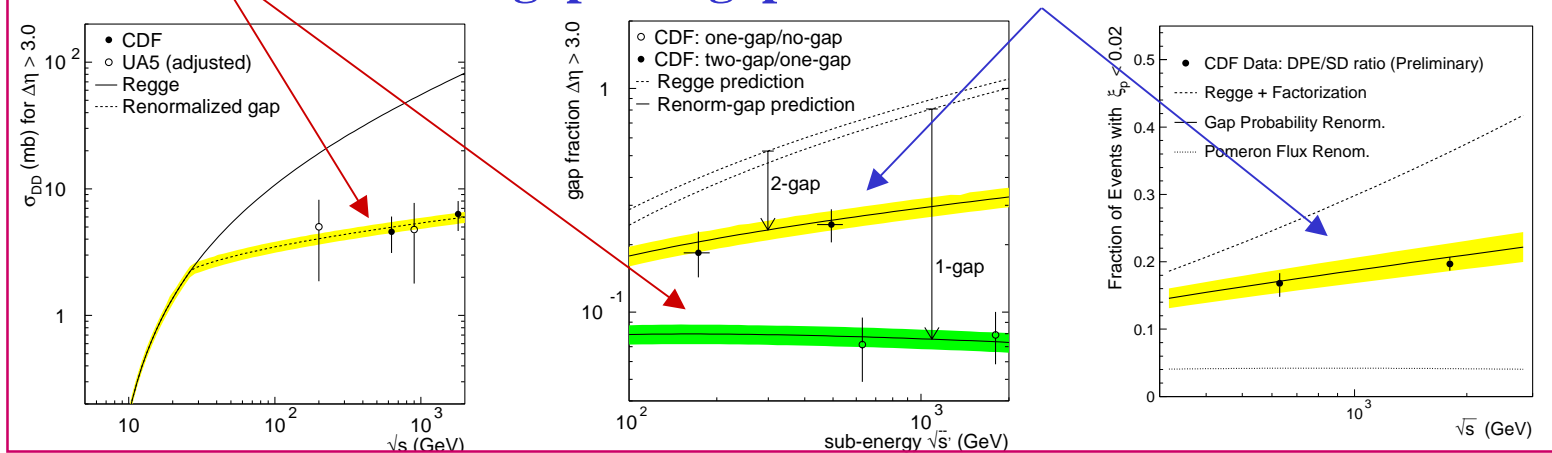
Same suppression as for single gap!

Central & Double-Gap Results

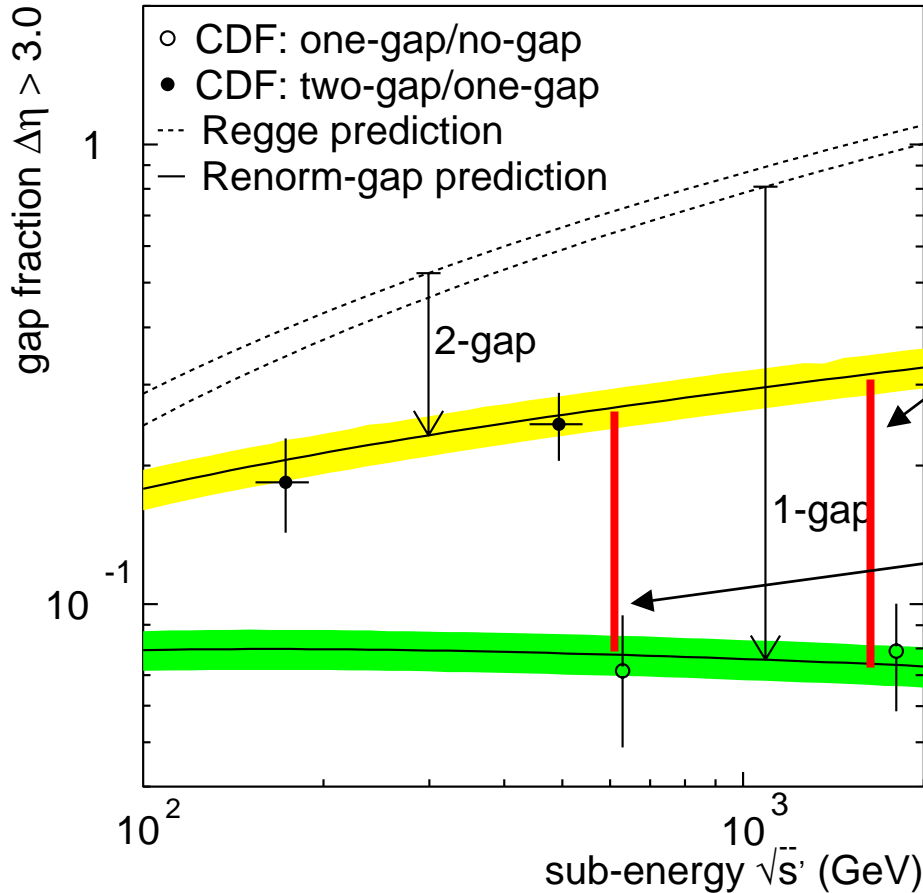
Differential shapes agree with Regge predictions



- One-gap cross sections are suppressed
- Two-gap/one-gap ratios are $\approx \kappa = 0.17$



Soft Gap Survival Probability



$$S = \frac{\phi \left[\begin{array}{c} \text{gap} \\ \eta \end{array} \right] / \phi \left[\begin{array}{c} \text{no-gap} \\ \eta \end{array} \right]}{\phi \left[\begin{array}{c} \text{gap} \\ \eta \end{array} \right] / \phi \left[\begin{array}{c} \text{no-gap} \\ \eta \end{array} \right]}$$

$$S_{2\text{-gap}/1\text{-gap}}^{1\text{-gap}/0\text{-gap}} (1800 \text{ GeV}) \approx 0.23$$

$$S_{2\text{-gap}/1\text{-gap}}^{1\text{-gap}/0\text{-gap}} (630 \text{ GeV}) \approx 0.29$$

Soft Diffraction Conclusions

Experiment:

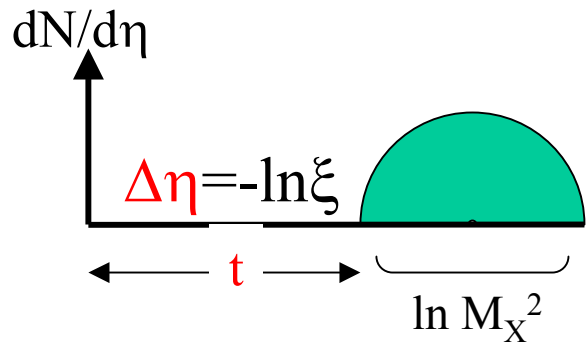
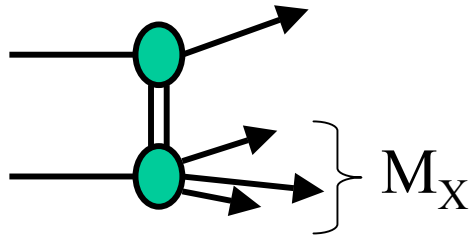
- M^2 - scaling
- Non-suppressed double-gap to single-gap ratios

Phenomenology:

- Generalized renormalization
- Obtain Pomeron intercept and tripe-Pomeron coupling from inclusive PDF's and color factors

Soft vs Hard Diffraction

SOFT DIFFRACTION

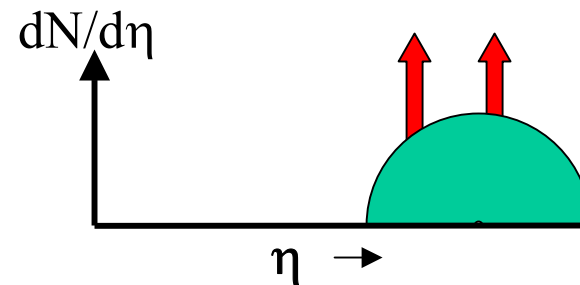
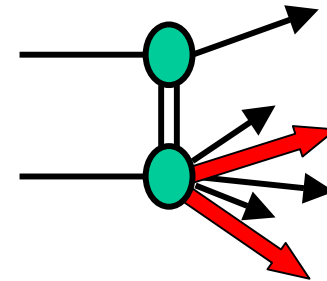


$$\xi = \Delta P_L / P_L$$

ξ = fractional momentum loss
of scattered (anti)proton

Variables: (ξ, t) or $(\Delta\eta, t)$

HARD DIFFRACTION



Additional variables: (x, Q^2)

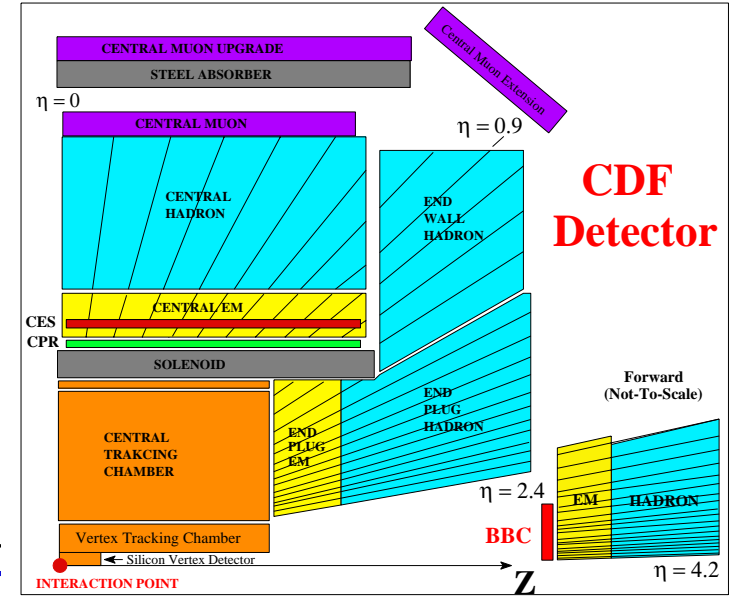
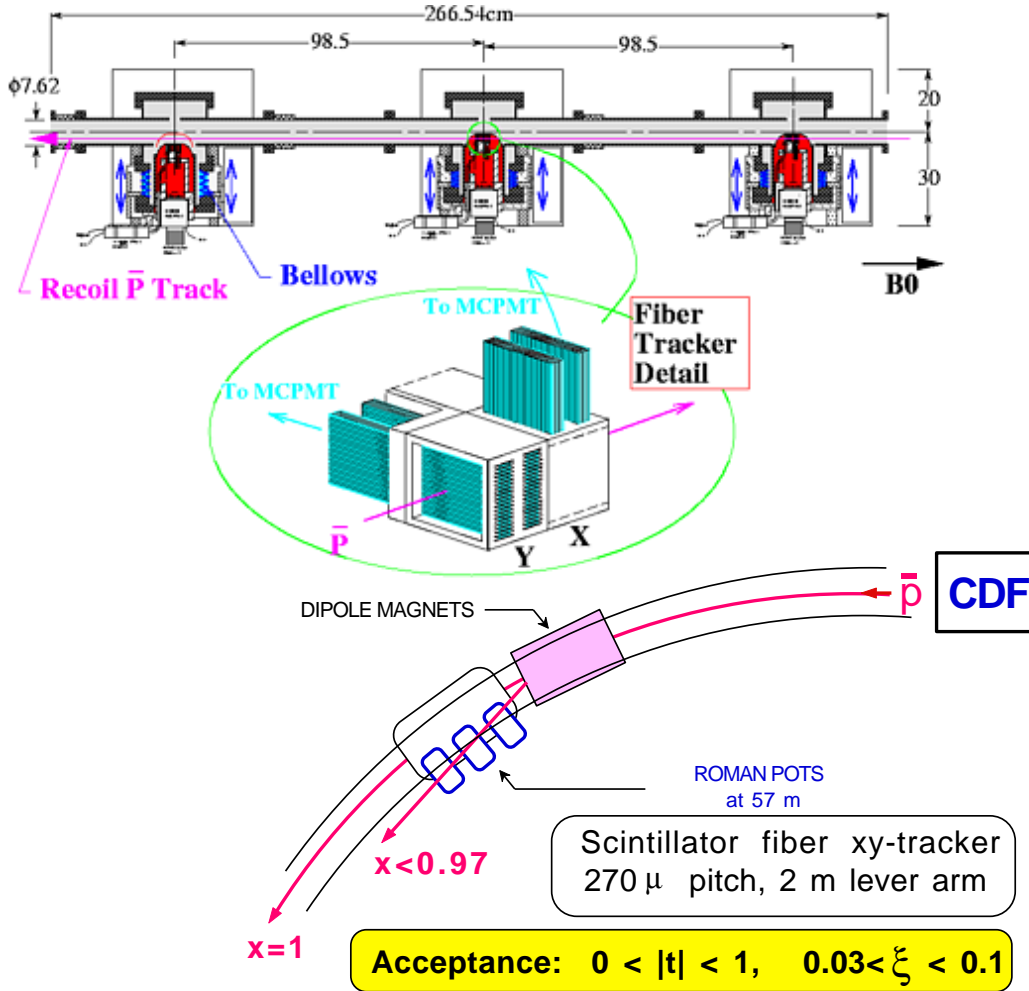
$$x_{Bj} = \sum E_T^{jet} e^{-\eta^{jet}} / \sqrt{s}$$

$$x = \beta \xi, \quad Q^2 = (E_T^{jet})^2$$

Run-IC

CDF-I

Run-IA,B



Forward Detectors

BBC $3.2 < \eta < 5.9$

FCAL $2.4 < \eta < 4.2$

Diffractive Fractions @ CDF

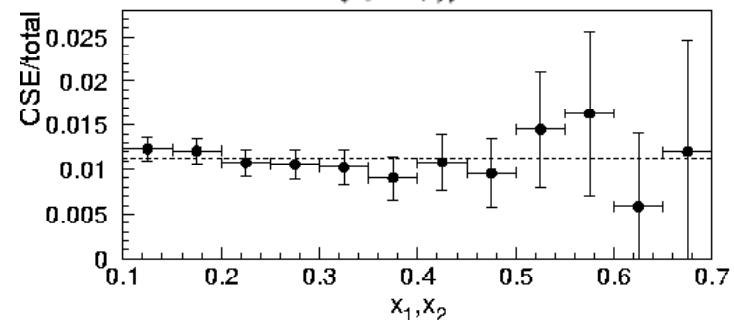
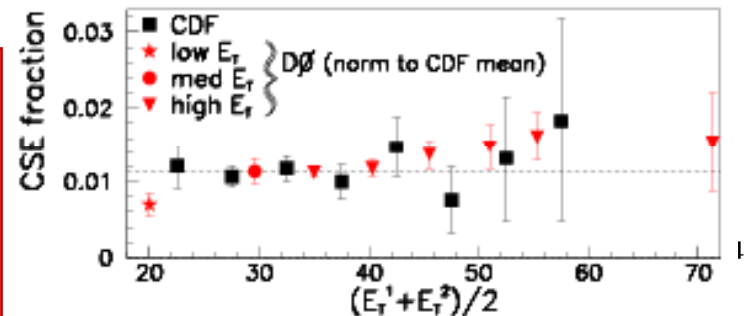
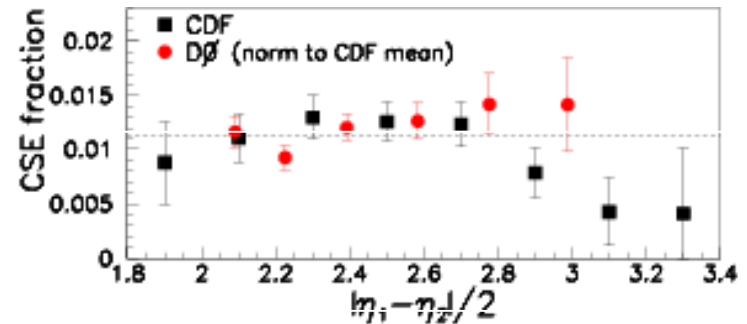
$$\bar{p}p \rightarrow X + \text{gap}$$

SD/ND fraction at 1800 GeV

X	Fraction(%)
W	1.15 (0.55)
JJ	0.75 (0.10)
b	0.62 (0.25)
J/ ψ	1.45 (0.25)

$$\bar{p}p \rightarrow \text{Jet} + \text{gap} + \text{Jet}$$

DD/ND gap fraction at 1800 GeV



- All SD/ND fractions ~1%
- Gluon fraction $f_g = 0.54 \pm 0.15$
- Suppression by ~5 relative to HERA
→ gap survival probability ~20%

Factorization OK @ Tevatron
at 1800 GeV (single energy) ?

Diffractive Structure F'n @CDF

$$\bar{p} + p \rightarrow \bar{p} + Jet + Jet + X$$

- Measure ratio of SD/ND dijet rates as a f'n of $x_{\bar{p}}$

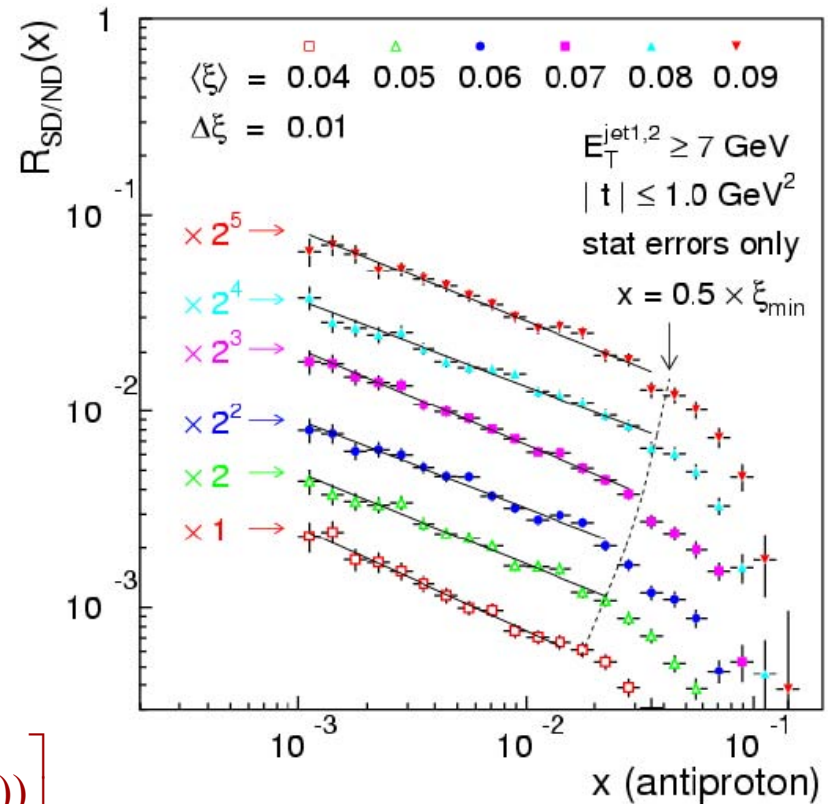
$$x_{\bar{p}} \equiv p_{g,q}/p_{\bar{p}} = \frac{\sum_{i=1}^{2(3)} E_T^i \cdot e^{-\eta^i}}{\sqrt{s}}$$

$$\frac{R_{SD}}{R_{ND}}(x_{\bar{p}}) \approx R_0 \cdot x_{\bar{p}}^{-0.45}$$

- In LO-QCD ratio of rates equals ratio of structure f'n's

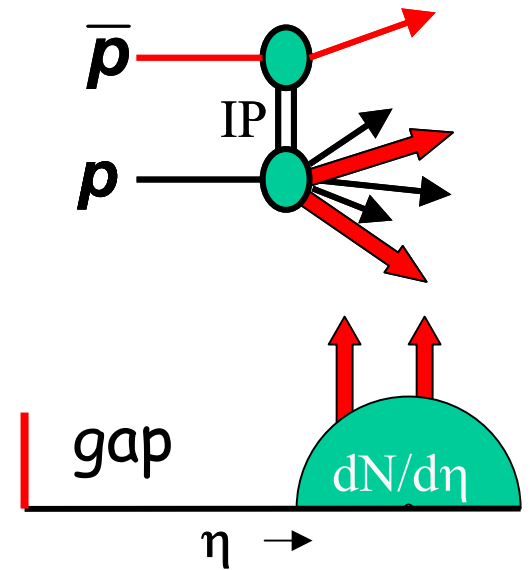
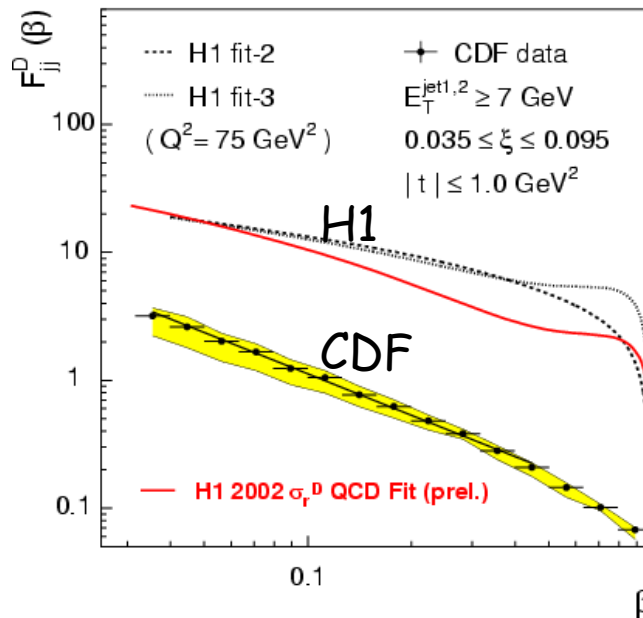
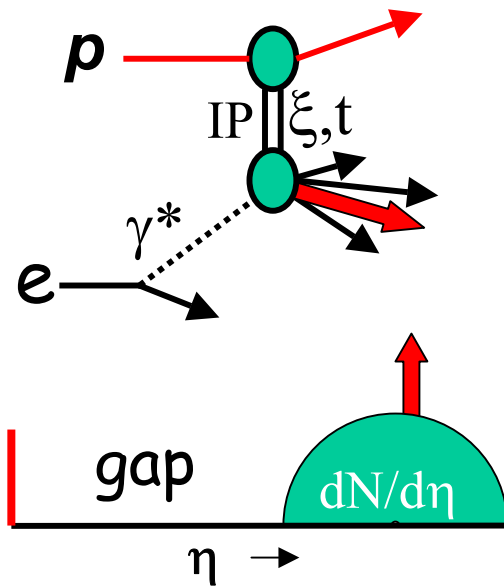
$$F_{jj}(x_{\bar{p}}) = x_{\bar{p}} \left[g(x_{\bar{p}}) + \frac{C_F}{C_A} \sum (q_i(x_{\bar{p}}) + \bar{q}_i(x_{\bar{p}})) \right]$$

SD/ND Rates vs $x_{\bar{p}}$



Breakdown of QCD Factorization

HERA $\xrightarrow{\text{The clue to understanding the Pomeron}}$ TEVATRON



$$F_2(Q^2, x)$$

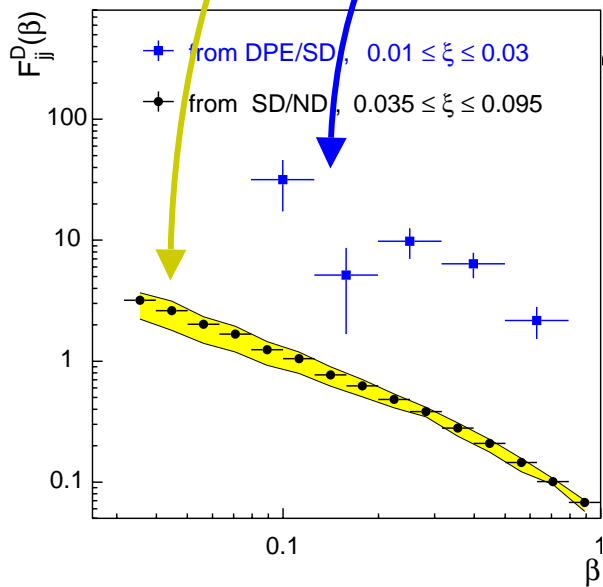
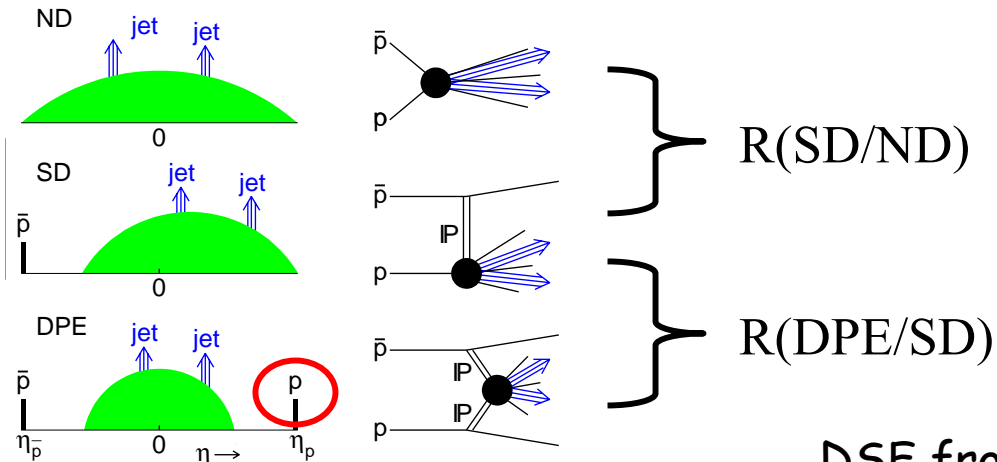
$$F_2^D(Q^2, \beta, \xi, t)$$

$$F_{JJ}(E_T^{Jet}, x)$$

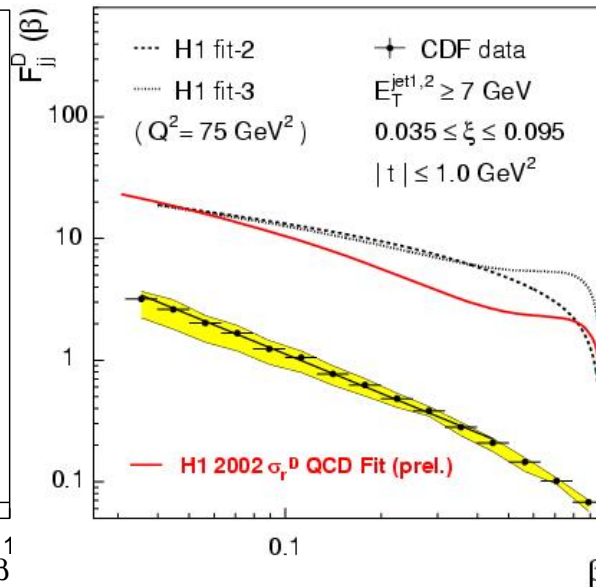
$$F_{JJ}^D(E_T^{Jet}, \beta, \xi, t)$$

???

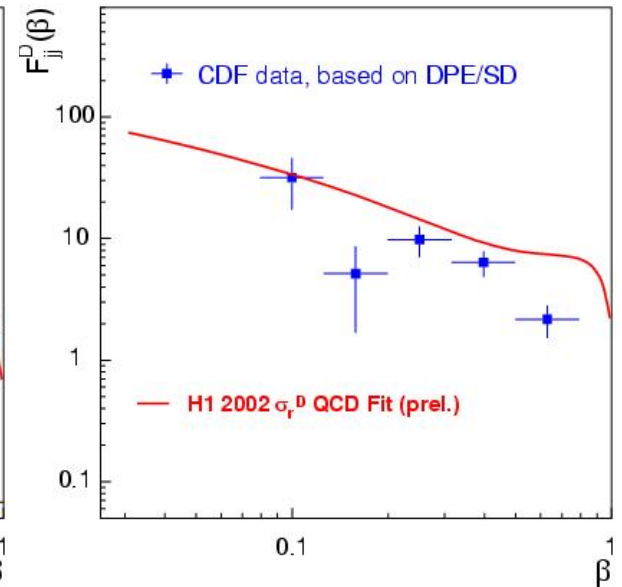
Restoring Diffractive Factorization



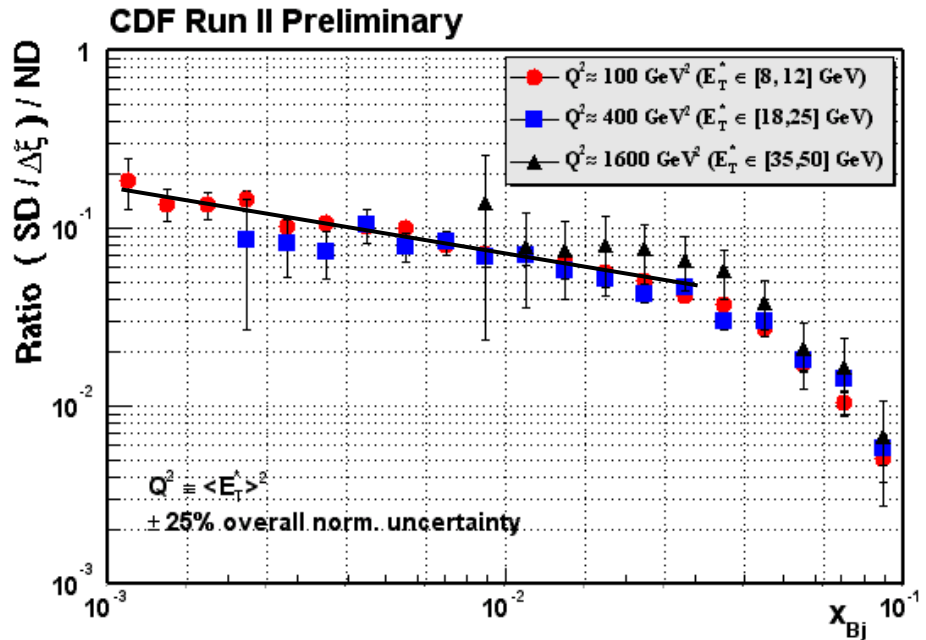
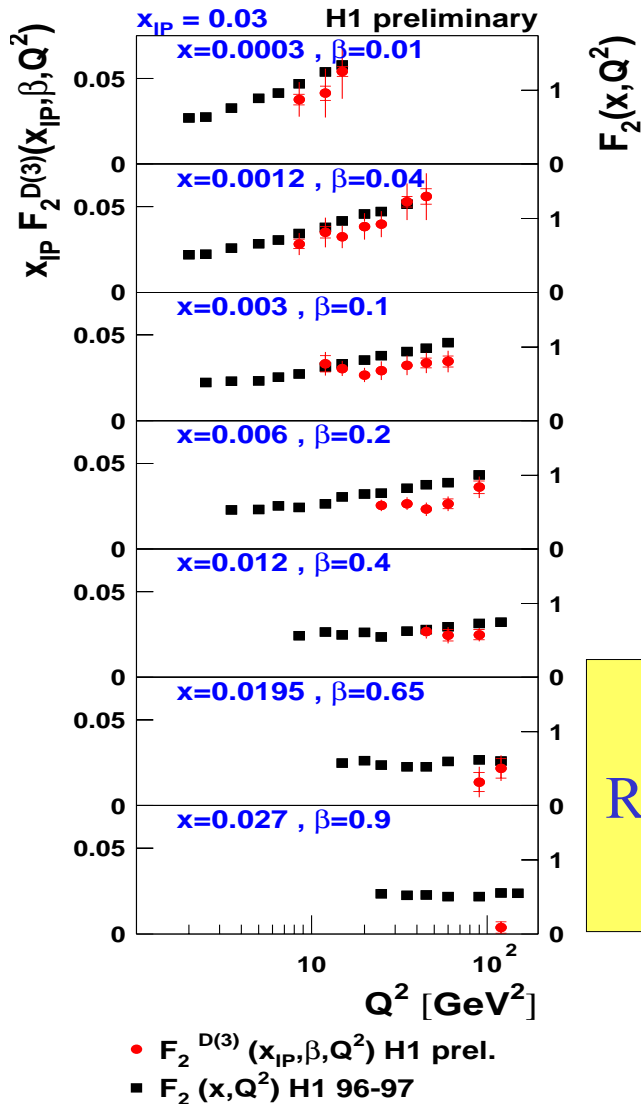
DSF from single-gaps



DSF from double-gaps:
Factorization restored!



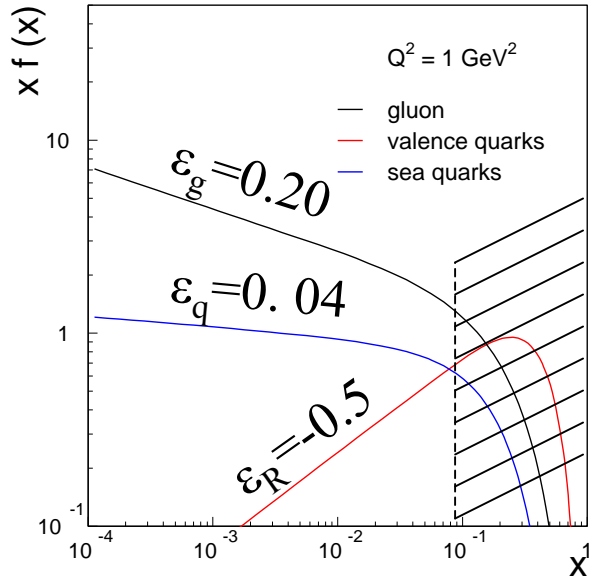
Q² dependence of DSF



$$R \left(\frac{F^D(Q^2, x, \xi)}{F(Q^2, x)} \right) \Rightarrow \begin{cases} \sim \text{no } Q^2 \text{ dependence} \\ \sim \text{flat at HERA} \\ \sim 1/x^{0.5} \text{ at Tevatron} \end{cases}$$

Pomeron evolves similarly to proton
except for for renormalization effects

Diffractive Structure Function from the Deep Sea



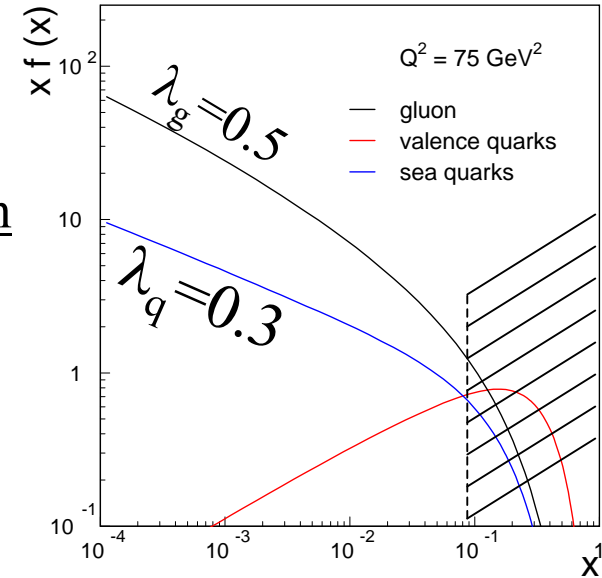
$$x \cdot f(x) = \frac{1}{x^\varepsilon}$$

Power-law region

$$\xi_{\max} = 0.1$$

$$x_{\max} = 0.1$$

$$\beta < 0.05\xi$$



$$F^D(q^2, x, \xi) \propto \frac{1}{\xi^{1+\varepsilon}} \cdot F(q^2, x) \propto \frac{1}{\xi^{1+\varepsilon}} \cdot \frac{C(q^2)}{(\beta\xi)^{\lambda(q^2)}} \Rightarrow \frac{A_{\text{NORM}}}{\xi^{1+\varepsilon+\lambda}} \cdot \kappa \cdot \frac{C}{\beta^\lambda}$$

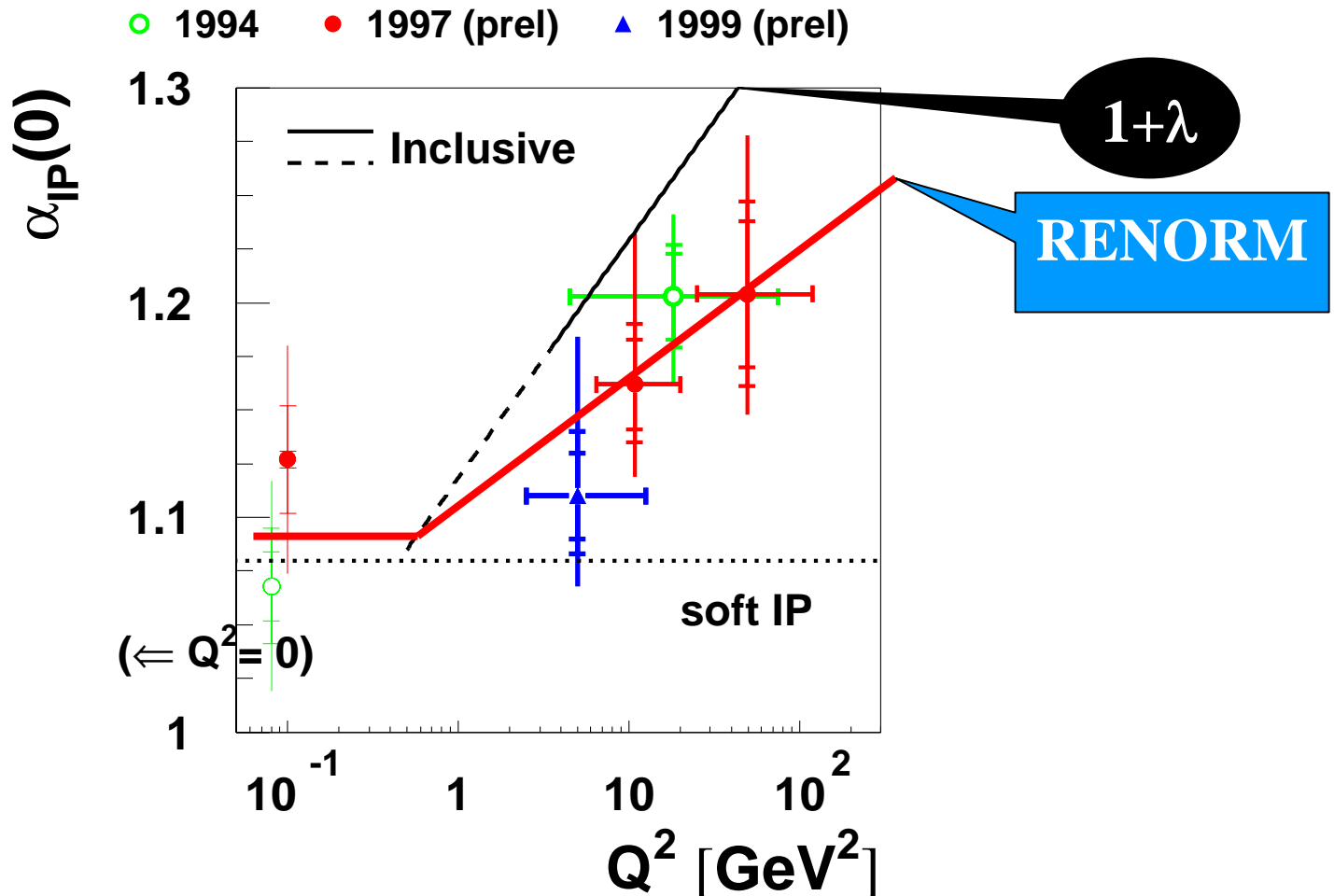
HERA(no RENORM): $R_{DIS}^{DDIS}(x) \xrightarrow{\text{fixed } \xi} \text{constant}$

TEVATRON (RENORM) : $R_{ND}^{SD}(x) \propto x^{-(\varepsilon + \lambda)}$

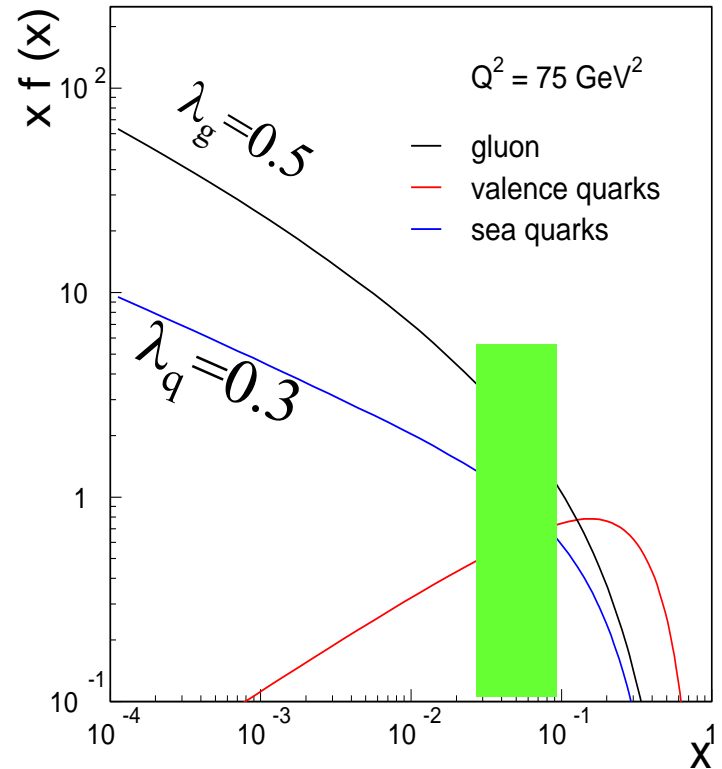
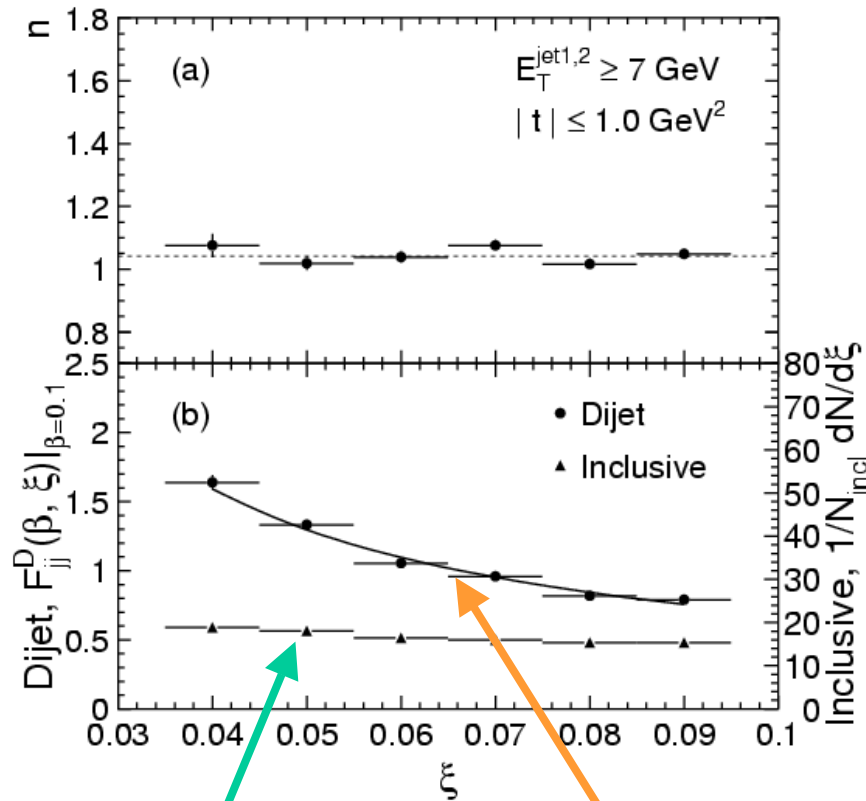
$$2\varepsilon_{DDIS} = \varepsilon + \lambda(Q^2)$$

Pomeron Intercept from H1

H1 Diffractive Effective $\alpha_{IP}(0)$ $\alpha_{IP}(t) = 1 + \varepsilon + \alpha' t$



ξ -dependence: Inclusive vs Dijets



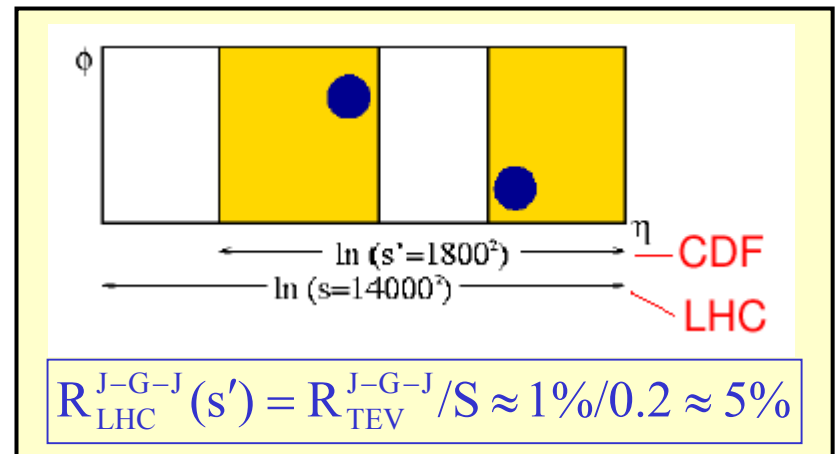
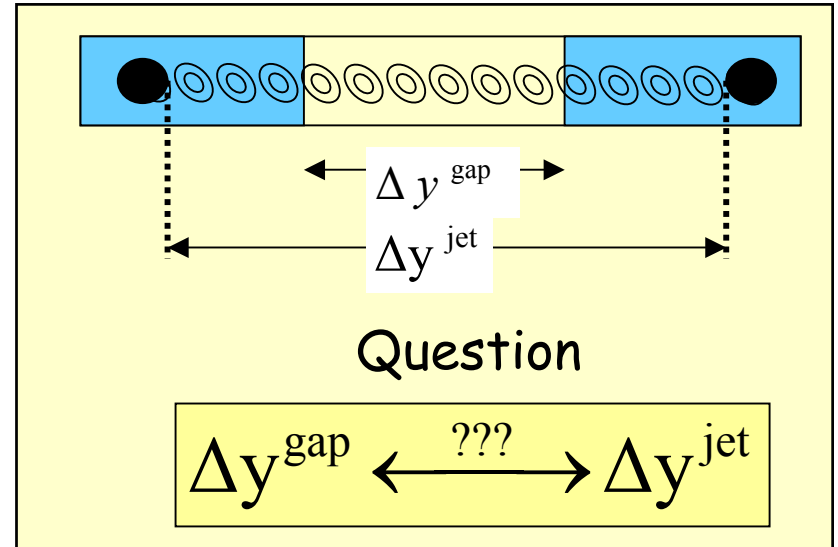
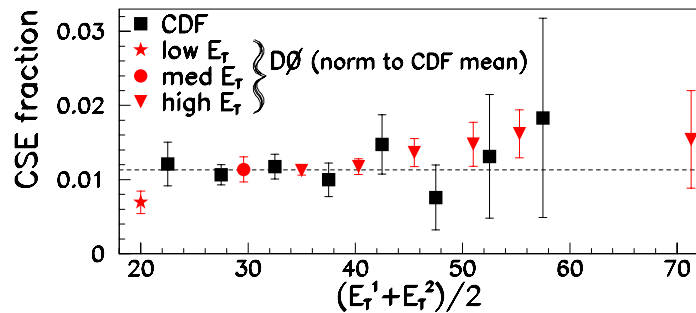
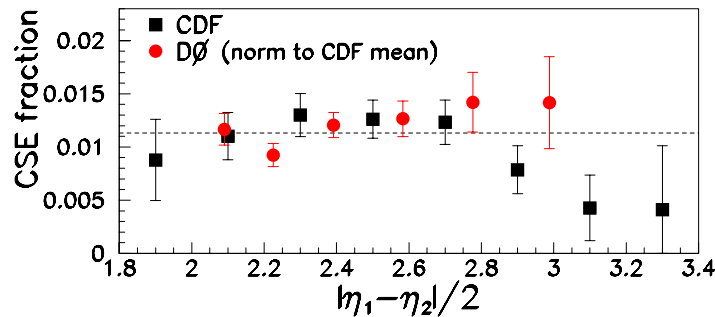
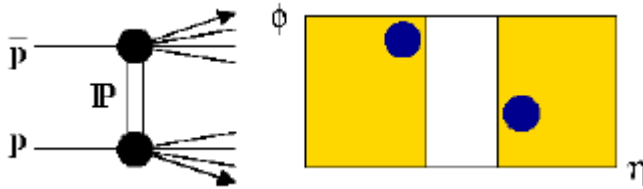
$$\frac{d\sigma_{\text{incl}}}{d\xi} \propto \text{constant}$$

$$F_{jj}^D(\beta, \xi) \propto \frac{1}{\beta^n} \cdot \frac{1}{\xi^m} \quad (n = 1.0 \pm 0.1, \quad m = 0.9 \pm 0.1)$$

Pomeron dominated

Gap Between Jets

$\bar{p} + p \rightarrow \text{Jet} + \text{Gap} + \text{Jet}$



Summary

SOFT DIFFRACTION

- M^2 - scaling
- Non-suppressed double-gap to single-gap ratios

HARD DIFFRACTION

- Flavor-independent SD/ND ratio
- Little or no Q^2 -dependence in SD/ND ratio

- ✓ Universality of gap probability in soft and hard diffraction
- ✓ Pomeron evolves similarly to proton

Diffraction appears to be a low-x partonic exchange subject to color constraints