

QCD ASPECTS OF HADRONIC DIFFRACTION

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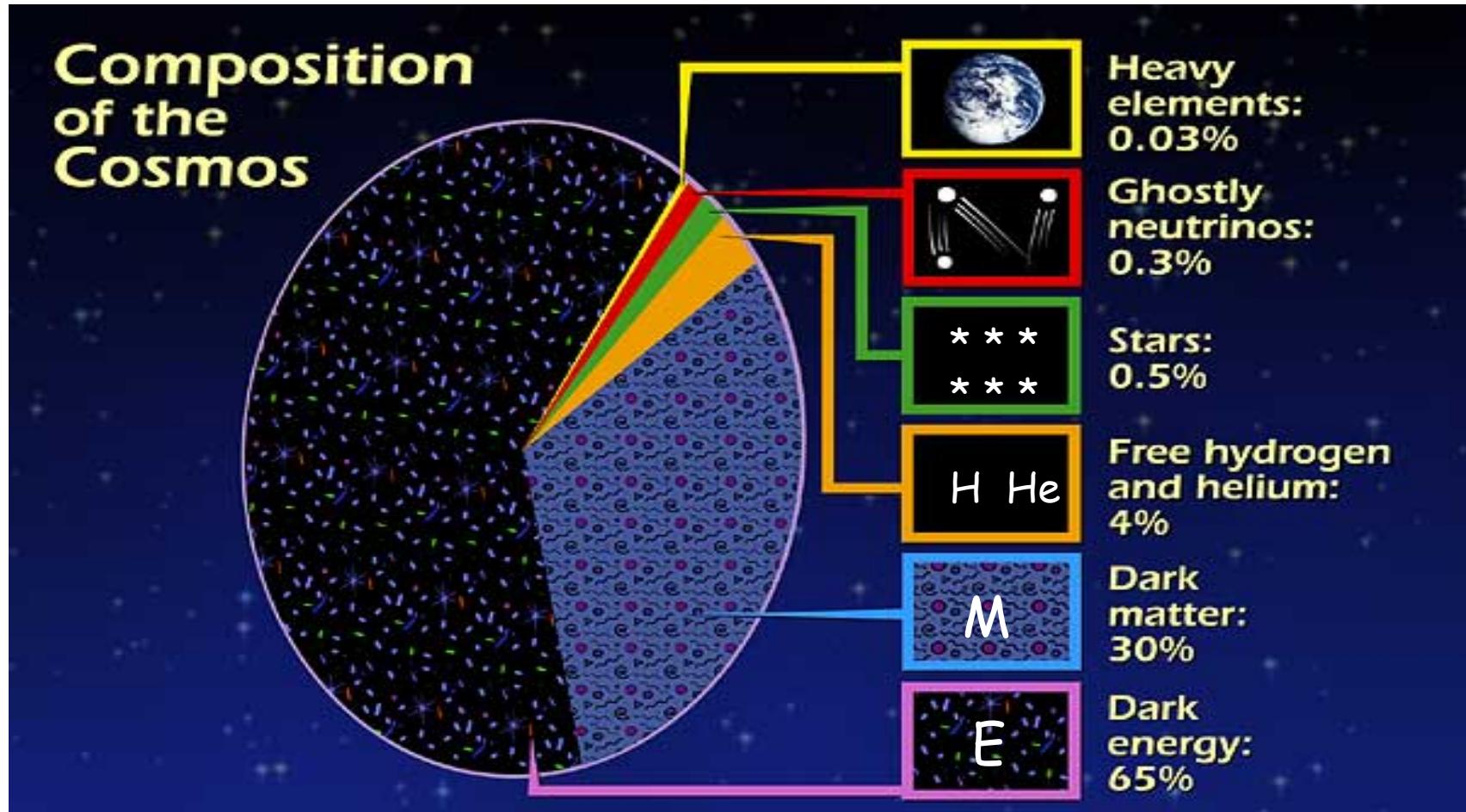
High Energy Physics Seminar

University of Connecticut
7 February 2005

- CDF results
- Comparison with HERA
- QCD aspects
- Tev2LHC



What is Dark Energy?



Rapidity Gaps

Bj, PRD 47 (1993) 101: regions of (pseudo)rapidity devoid of particles

Non-diffractive interactions

Rapidity gaps are formed by multiplicity fluctuations.

From Poisson statistics:



$$P(\Delta y) = e^{-\rho \Delta y} \quad \left(\rho = \frac{dn}{dy} \right)$$

(ρ =particle density in rapidity space)

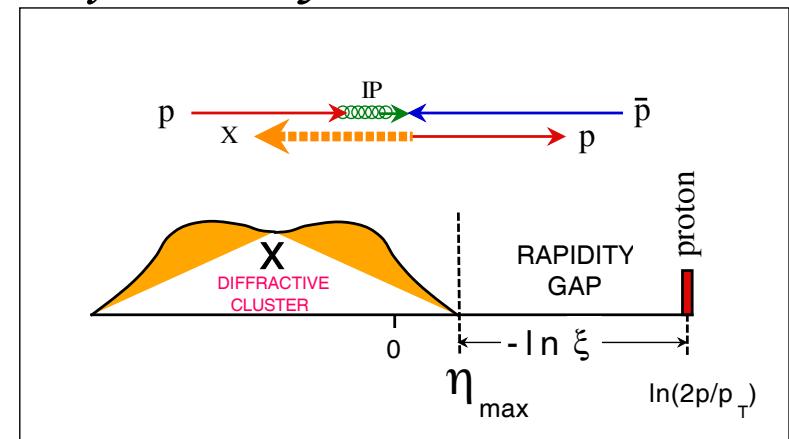
Gaps are exponentially suppressed

Diffractive interactions

Rapidity gaps at $t=0$ grow with Δy .

$$\xi \equiv \Delta p / p$$

$$\Delta y \approx -\ln \xi = \ln s - \ln M^2$$



$$\left(\frac{d\sigma}{d\Delta y} \right)_{t=0} \sim e^{2\varepsilon \Delta y} \Rightarrow \frac{d\sigma}{dM^2} \sim \frac{1}{(M^2)^{1+\varepsilon}}$$

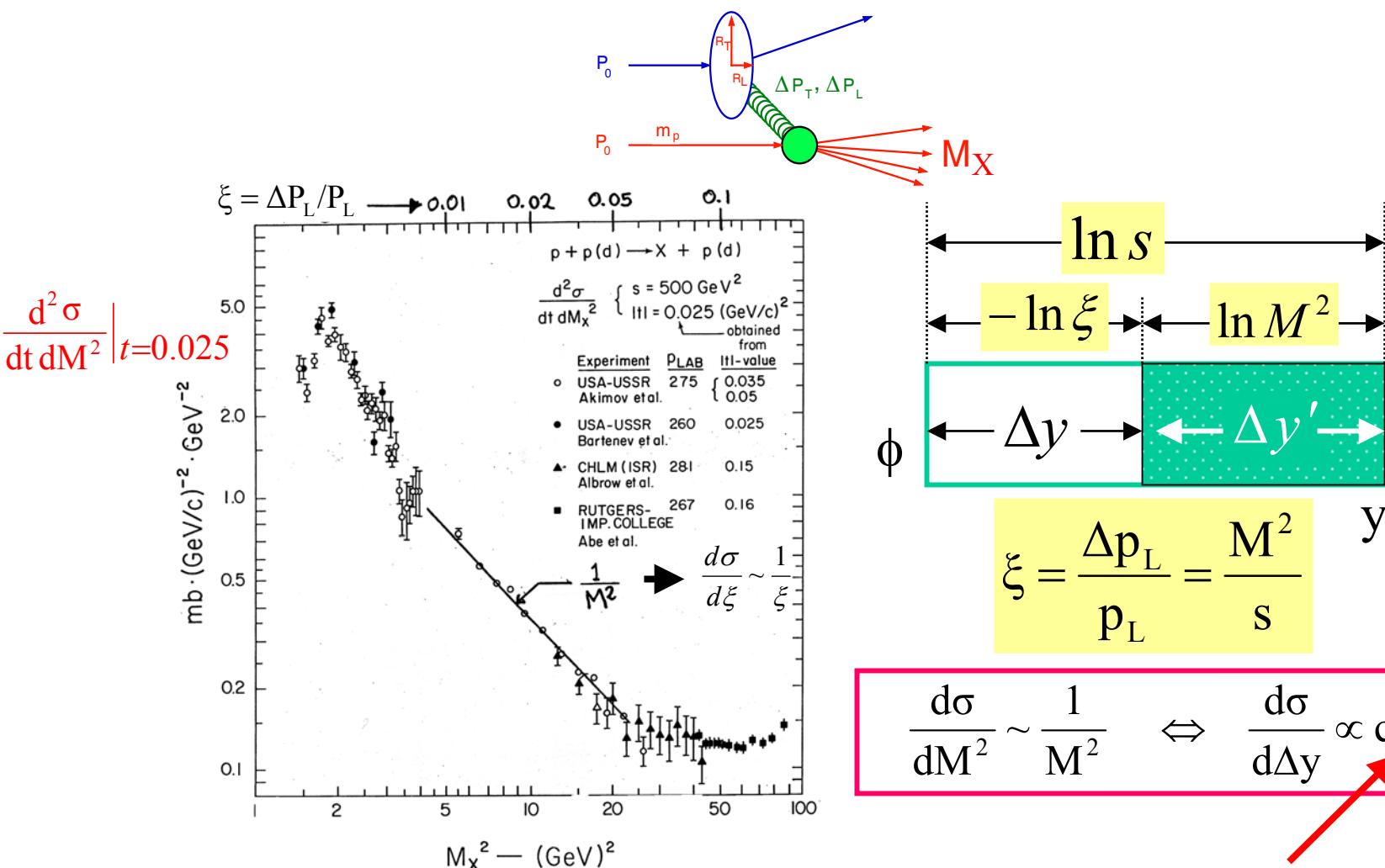
2 ε : negative particle density!

Forty Years of Diffraction

<http://physics.rockefeller.edu/dino/my.html>

- + 1960's BNL: first observation of $p p \rightarrow p X$
 - + 1970's Fermilab fixed target, ISR, SPS
→ Regge theory & factorization
- Review: KG, Phys. Rep. 101 (1983) 169
- + 1980's UA8: diffractive dijets \Rightarrow hard diffraction
 - + 1990's Tev Run-I: Regge factorization breakdown
Tev/ HERA: QCD factorization breakdown
 - + 21st C Multigap diffraction: restoration of factorization
Ideal for diffractive studies @ LHC

The First 20 Years



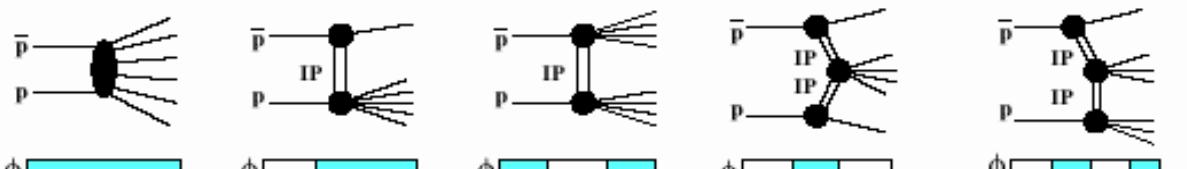
KG, Phys. Rep. 101 (1983) 171

POMERON: color singlet
w/vacuum quantum numbers

The Last 20 Years

Diffraction@CDF in Run I 16 papers

- Elastic scattering** PRD 50 (1994) 5518
- Total cross section** PRD 50 (1994) 5550
- Diffraction**

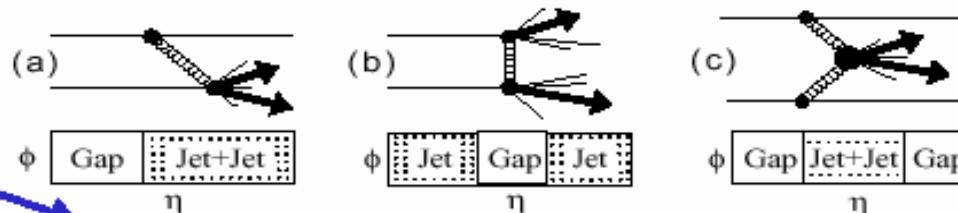


SOFT diffraction

| ϕ Control sample η | ϕ Non-Diffractive (ND) η | ϕ Single-Diffractive (SD) η | ϕ Double Diffractive (DD) η | ϕ Double Pomeron Exchange (DPE) η | ϕ Single + Double Diffractive (SDD) η |
|------------------------------|------------------------------------|---------------------------------------|---------------------------------------|---|---|
| PRD 50 (1994) 5535 | PRD 87 (2001) 141802 | PRL 93(2004)141601 | PRL 91(2003)011802 | | |

HARD diffraction

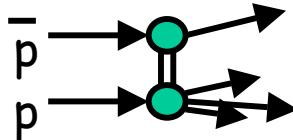
PRL references



with roman pots

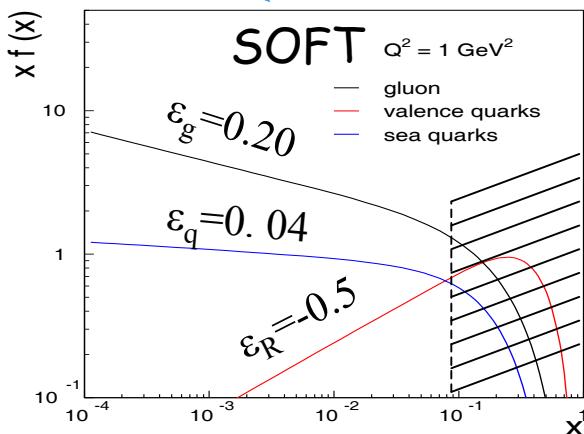
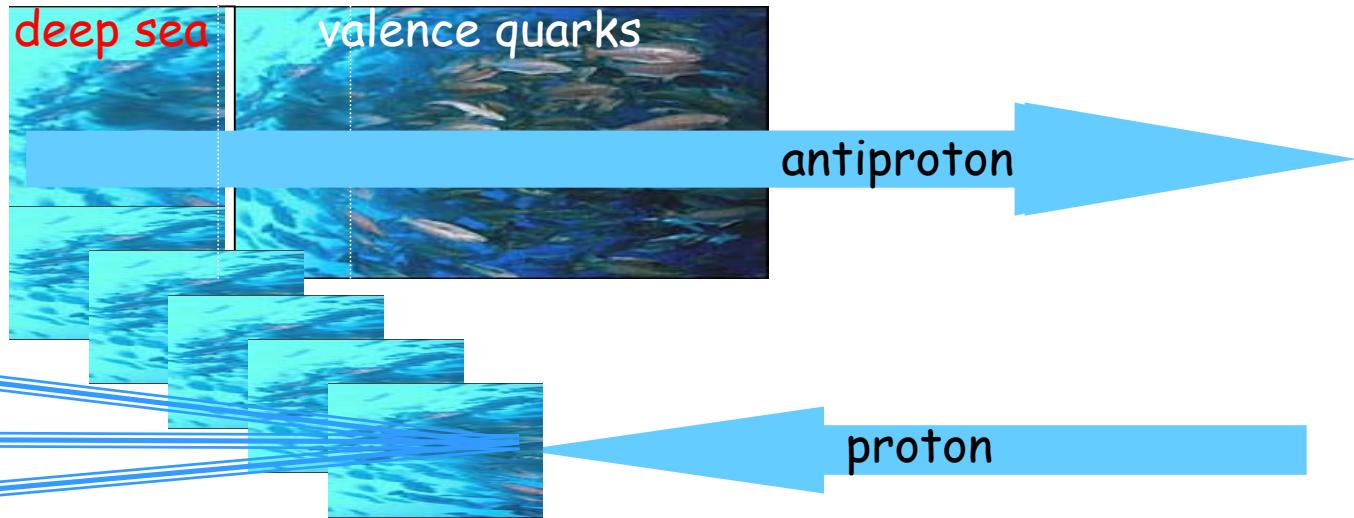
| |
|---------------------|
| JJ 84 (2000) 5043 |
| JJ 88 (2002) 151802 |

| | | |
|----------------------------|-------------------|-------------------|
| W 78 (1997) 2698 | JJ 74 (1995) 855 | JJ 85 (2000) 4217 |
| JJ 79 (1997) 2636 | JJ 80 (1998) 1156 | |
| b-quark 84 (2000) 232 | JJ 81 (1998) 5278 | |
| J/ ψ 87 (2001) 241802 | | |

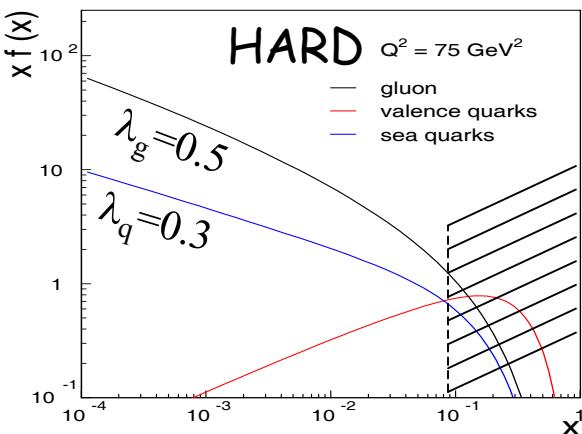


Diffraction in QCD

Derive diffractive from inclusive PDFs and color factors



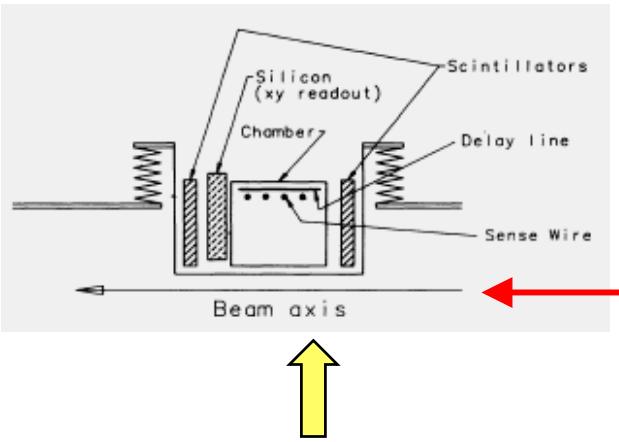
$$x \cdot f(x) = \frac{1}{x^\varepsilon (\text{or } \lambda)}$$



CDF in Run I-0 (1988-89)

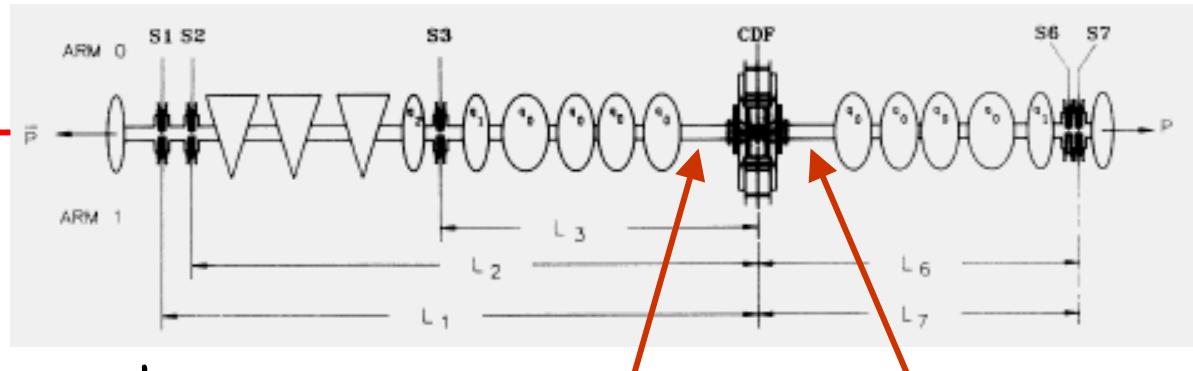
Elastic, single diffractive, and total cross sections
@ 546 and 1800 GeV

Roman Pot Spectrometers



Roman Pot Detectors

- Scintillation trigger counters
- Wire chamber
- Double-sided silicon strip detector



Additional Detectors
Trackers up to $|\eta| = 7$

Results

- Total cross section
- Elastic cross section
- Single diffraction

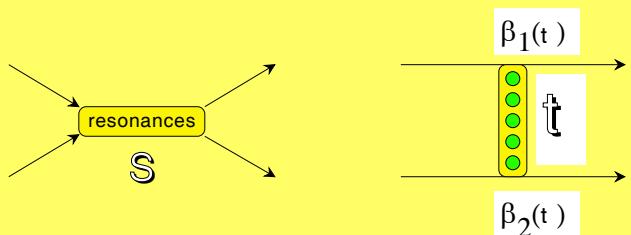
$$\sigma^{\text{tot}} \sim S^\varepsilon$$

$d\sigma/dt \sim \exp[2\alpha' \ln s] \rightarrow$ shrinking forward peak

Breakdown of Regge factorization

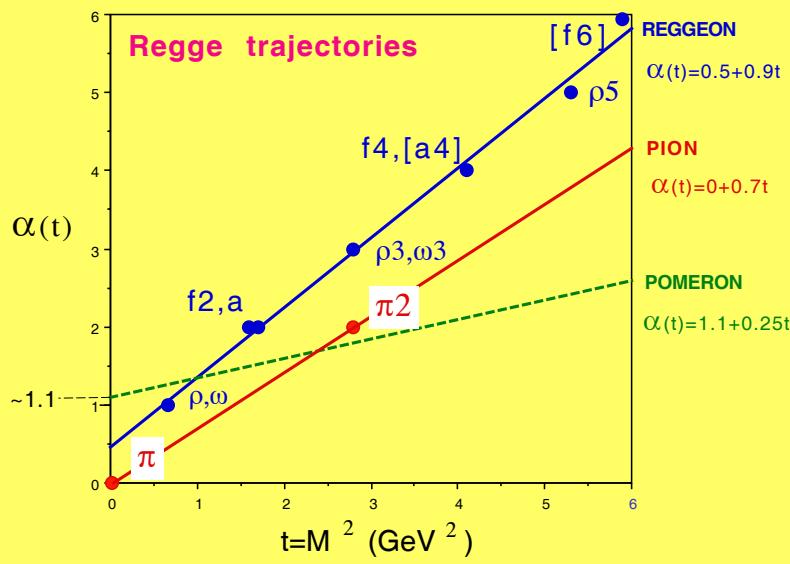
Regge Theory

REGGE THEORY



$$T(s,t) = \frac{1}{s} \beta_1(t) \beta_2(t) s^{\alpha(t)} \phi_{a(t)}$$

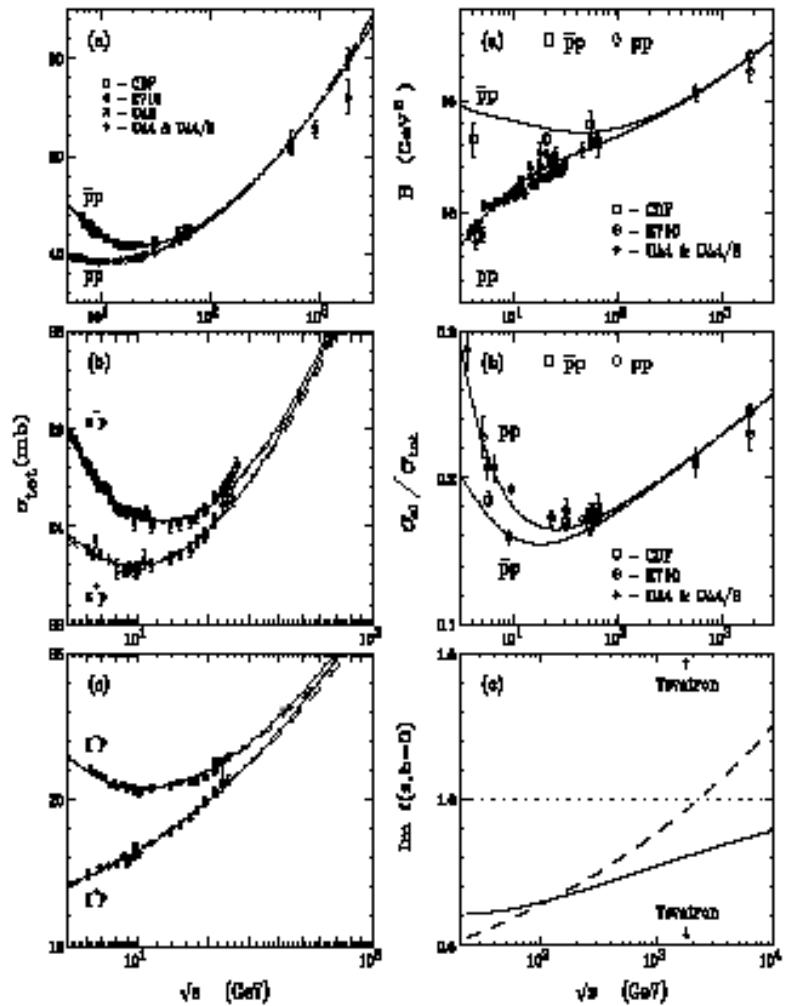
$$\sigma_T = \beta^{(0)} s^{\alpha(0)-1}$$

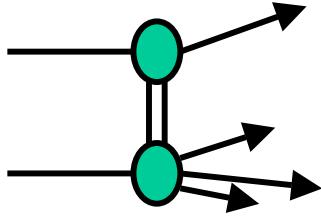


Total and Elastic Cross Sections

Covolan, Montanha and Goulianos, Phys. Lett. B 389 (1996) 176

$$\alpha_F = 1 + c (\Rightarrow 0.104 + 0.25t) \quad \alpha_{F/\pi} = 0.68 + 0.82t \quad \alpha_{\pi/F} = 0.46 + 0.92t$$





Renormalization

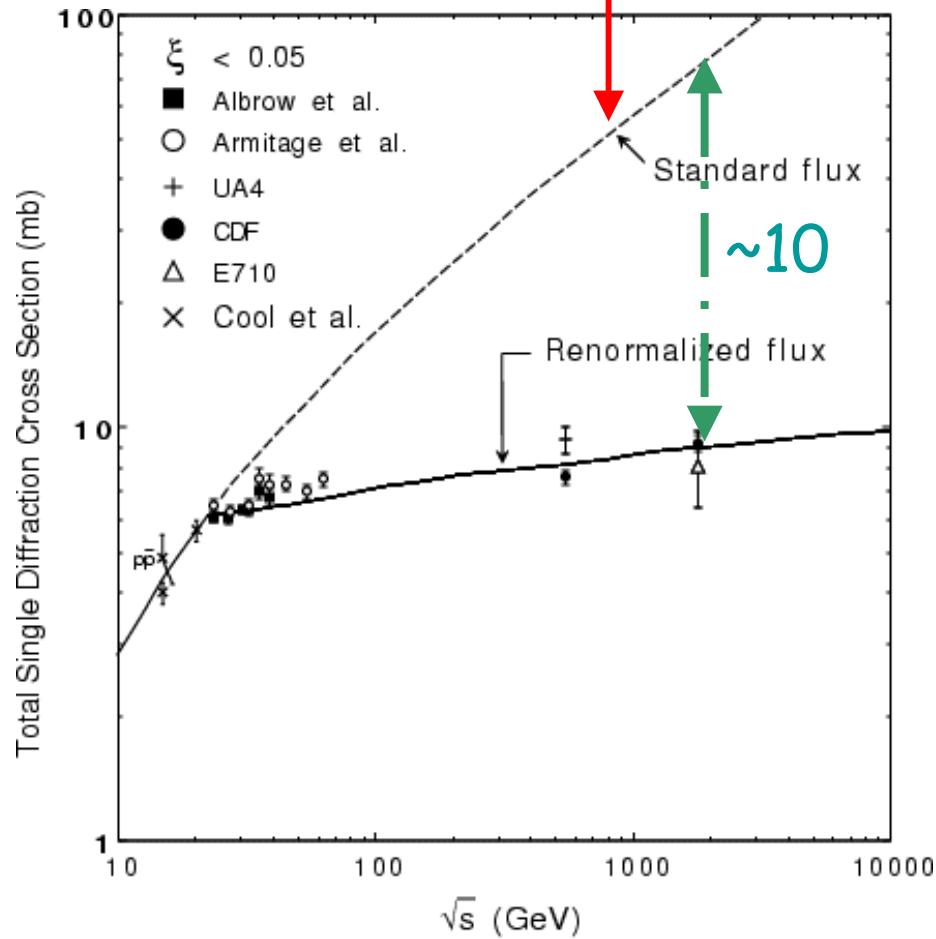
$$\frac{d^2\sigma_{SD}}{dt d\xi} = f_{IP/p}(t, \xi) \cdot \sigma_{IP-\bar{p}}(M_X^2)$$

$$\sigma_{SD} \sim s^{2\varepsilon}$$

- ❖ Unitarity problem:
With factorization
and std pomeron flux
 σ_{SD} exceeds σ_T at
 $\sqrt{s} \approx 2 \text{ TeV}$.
- ❖ Renormalization:
normalize the pomeron
flux to unity

KG, PLB 358 (1995) 379

$$\int_{\xi_{\min}}^{0.1} \int_{t=-\infty}^0 f_{IP/p}(t, \xi) d\xi dt = 1$$

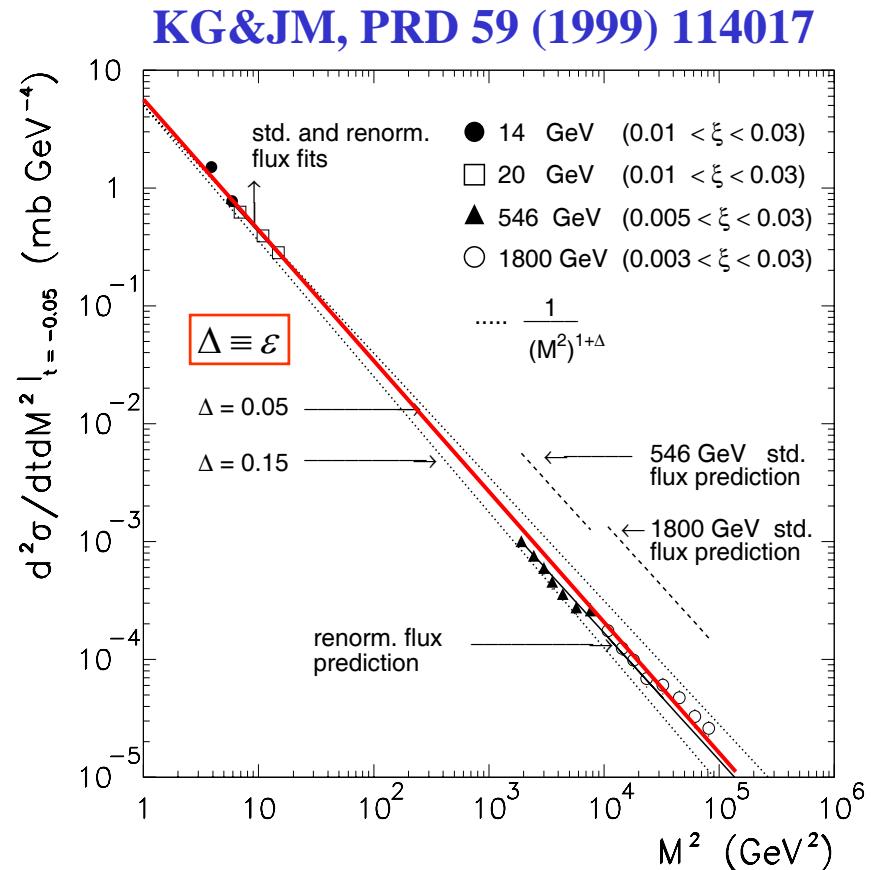


A Scaling Law in Diffraction

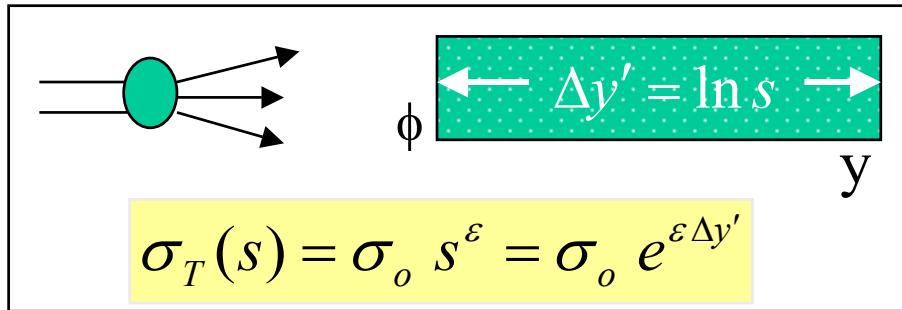
Factorization breaks
down in favor of
 M^2 -scaling

renormalization

$$\frac{d\sigma}{dM^2} \propto \frac{s^{2\varepsilon}}{(M^2)^{1+\varepsilon}}$$



The QCD Connection

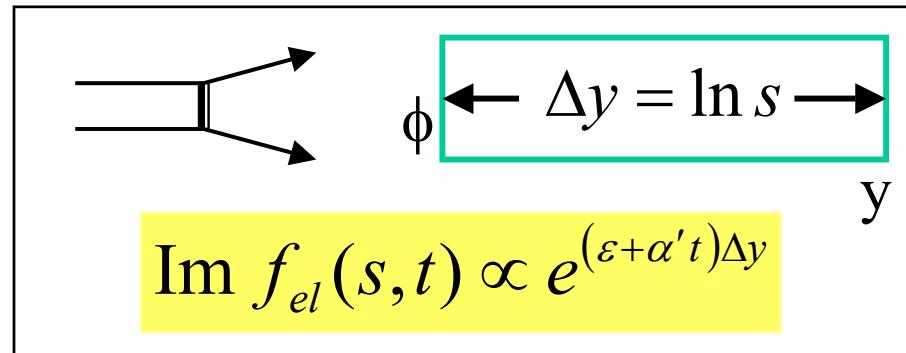


A Feynman diagram showing two incoming gluons (represented by two horizontal lines) interacting via a pomeron exchange (ϕ) to produce two outgoing gluons (two horizontal lines). A green box labeled $\Delta y' = \ln s$ is associated with the pomeron exchange.

$$\sigma_T(s) = \sigma_o s^\varepsilon = \sigma_o e^{\varepsilon \Delta y'}$$

The exponential rise of $\sigma_T(\Delta y')$ is due to the increase of wee partons with $\Delta y'$

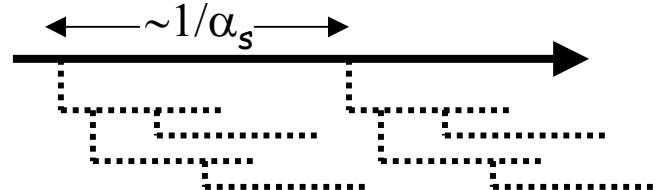
(see E. Levin, An Introduction to Pomerons, Preprint DESY 98-120)



A Feynman diagram showing an elastic forward scattering process where an incoming gluon (one horizontal line) interacts with a virtual photon (ϕ) to produce an outgoing gluon (one horizontal line). A green box labeled $\Delta y = \ln s$ is associated with the interaction.

$$\text{Im } f_{el}(s, t) \propto e^{(\varepsilon + \alpha' t) \Delta y}$$

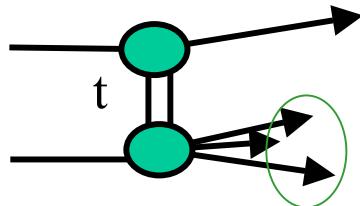
Total cross section:
power law rise with energy



Elastic cross section
forward scattering amplitude

QCD Basis of Renormalization

(KG, hep-ph/0205141)



2 independent variables: $t, \Delta y$

$$\frac{d^2\sigma}{dt d\Delta y} = C \bullet F_p^2(t) \bullet \left\{ e^{(\varepsilon + \alpha' t)\Delta y} \right\}^2 \bullet \kappa \bullet \left\{ \sigma_o e^{\varepsilon \Delta y'} \right\}$$

color factor

$$\kappa = \frac{g_{IP-IP-IP}(t)}{\beta_{IP-p-p}(0)} \approx 0.17$$

Gap probability

$$\downarrow \\ \sim e^{2\varepsilon \Delta y}$$

$$\rightarrow \int_{\Delta y_{\min}}^{\Delta y = \ln s} s^{2\varepsilon \Delta y} \approx s^{2\varepsilon}$$

Renormalization removes the s -dependence \rightarrow SCALING

The Factors κ and ε

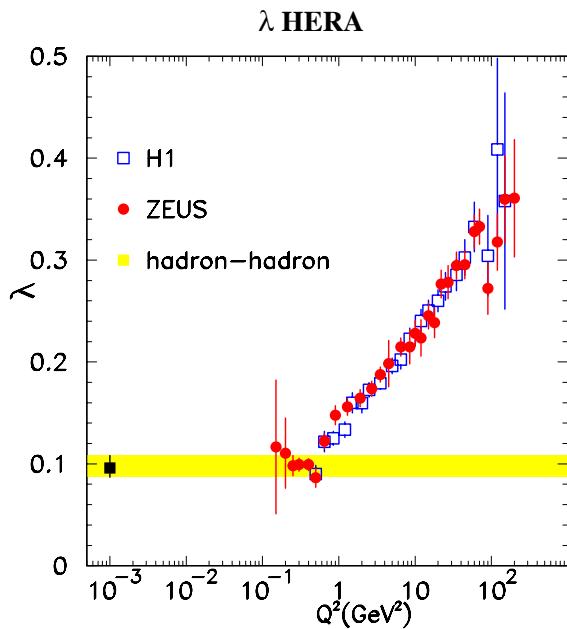
Experimentally:

KG&JM, PRD 59 (114017) 1999

$$\kappa = \frac{g_{IP-IP-IP}}{\beta_{IP-p}} = 0.17 \pm 0.02, \quad \varepsilon = 0.104$$

Color factor: $\kappa = f_g \times \frac{1}{N_c^2 - 1} + f_q \times \frac{1}{N_c} \frac{Q^2}{Q^2 - 1} \approx 0.75 \times \frac{1}{8} + 0.25 \times \frac{1}{3} = 0.18$

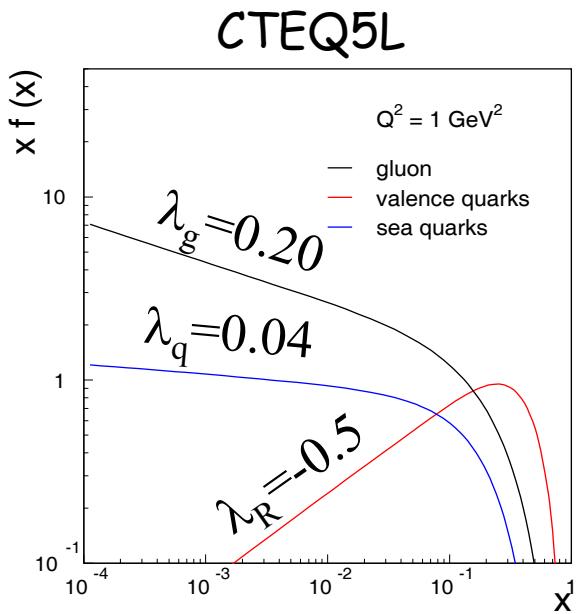
Pomeron intercept: $\varepsilon = \lambda_g \cdot w_g + \lambda_q \cdot w_q = 0.12$



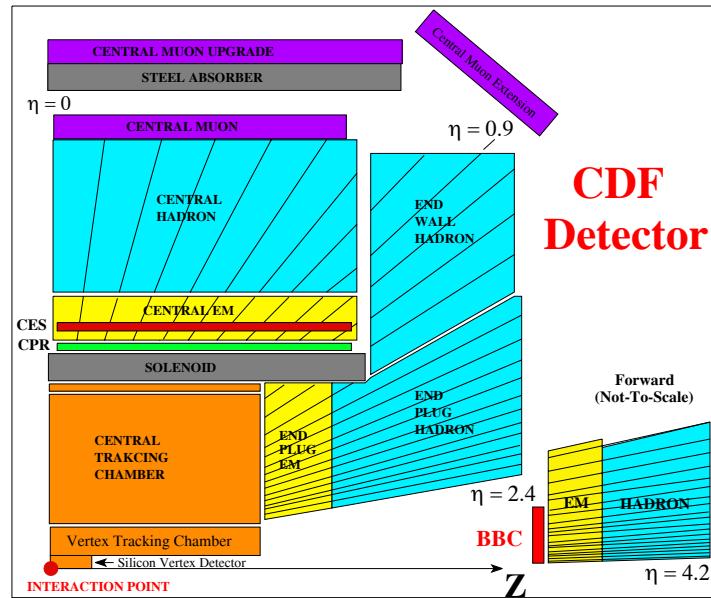
$$x \cdot f(x) = \frac{1}{x^\lambda}$$

f_g =gluon fraction
 f_q =quark fraction

$$\int_{x=1/s}^1 f(x) dx \sim s^\lambda$$



Run-I A,B: Rapidity Gap Studies



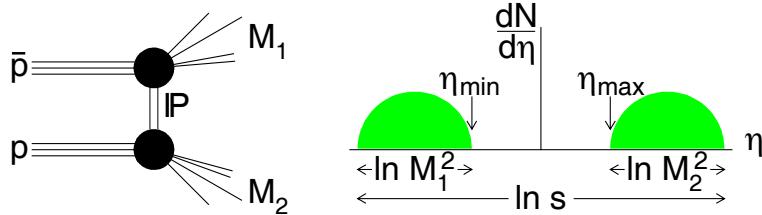
**CDF
Detector**

Forward Detectors

BBC $3.2 < \eta < 5.9$

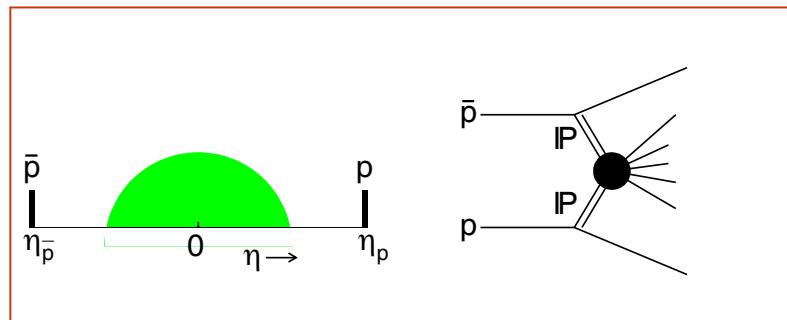
FCAL $2.4 < \eta < 4.2$

Central and Double Gaps



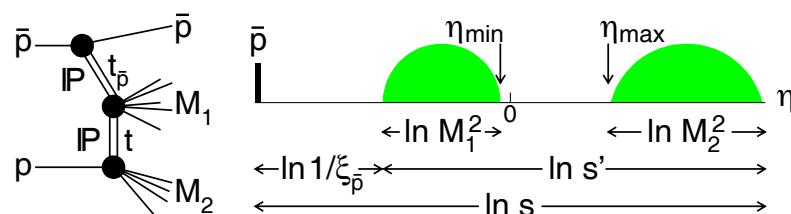
□ Double Diffraction Dissociation

➤ One central gap



□ Double Pomeron Exchange

➤ Two forward gaps

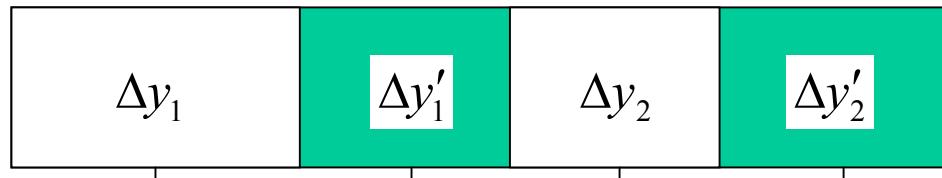
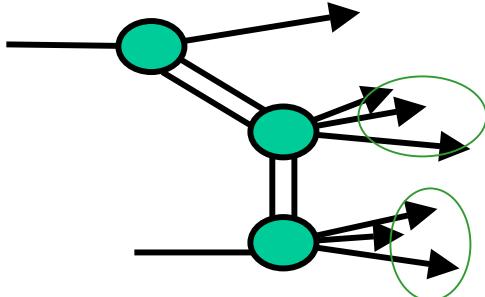


□ SDD: Single+Double Diffraction

➤ One forward + one central gap

Multigap Renormalization

(KG, hep-ph/0205141)



5 independent variables

$$\left\{ \begin{array}{c} t_1 \\ y'_1 \\ \Delta y = \Delta y_1 + \Delta y_2 \\ t_2 \end{array} \right.$$

color factors

$$\frac{d^5 \sigma}{\prod_{i=1-5} dV_i} = C \times F_p^2(t_1) \prod_{i=1-2} \left\{ e^{(\varepsilon + \alpha' t_i) \Delta y_i} \right\}^2 \times \kappa^2 \left\{ \sigma_o e^{\varepsilon (\Delta y'_1 + \Delta y'_2)} \right\}$$

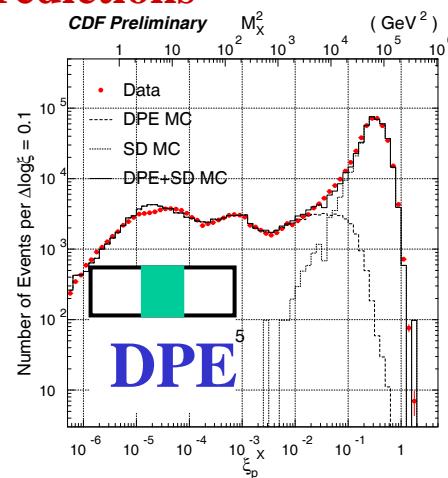
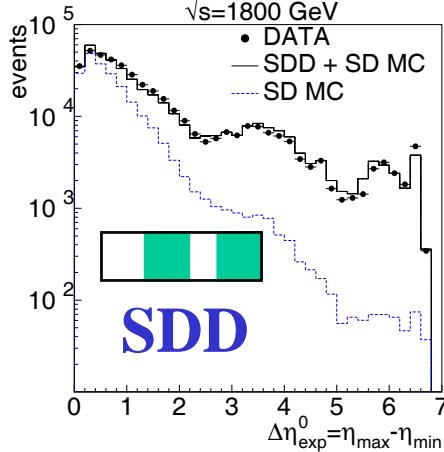
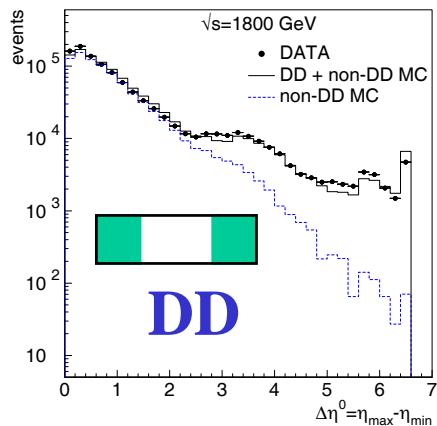
Gap probability Sub-energy cross section
 $\sim e^{2\varepsilon \Delta y}$ (for regions with particles)

$$\int_{\Delta y_{\min}}^{\Delta y = \ln s} s^{2\varepsilon \Delta y} \approx s^{2\varepsilon}$$

Same suppression
as for single gap!

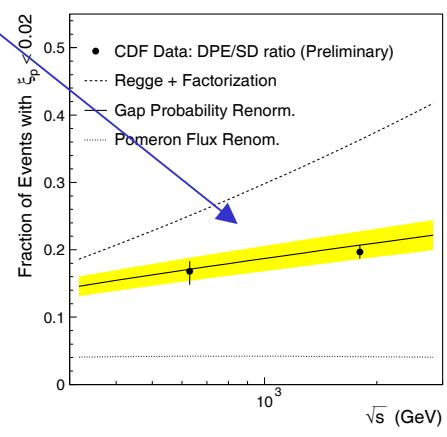
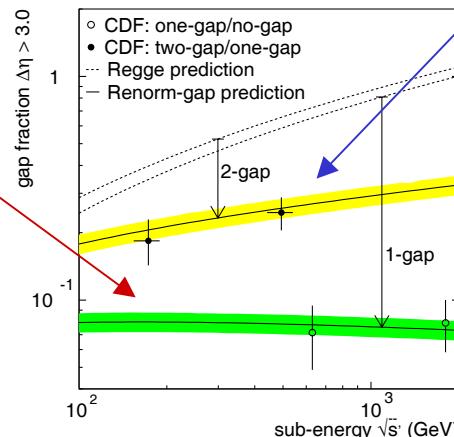
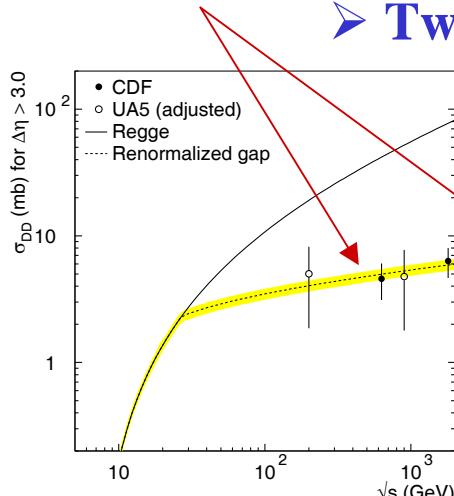
Central & Double-Gap Results

Differential shapes agree with Regge predictions

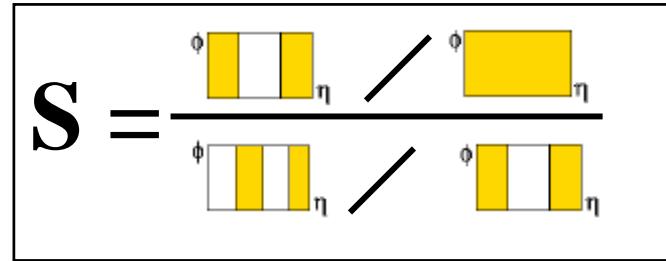
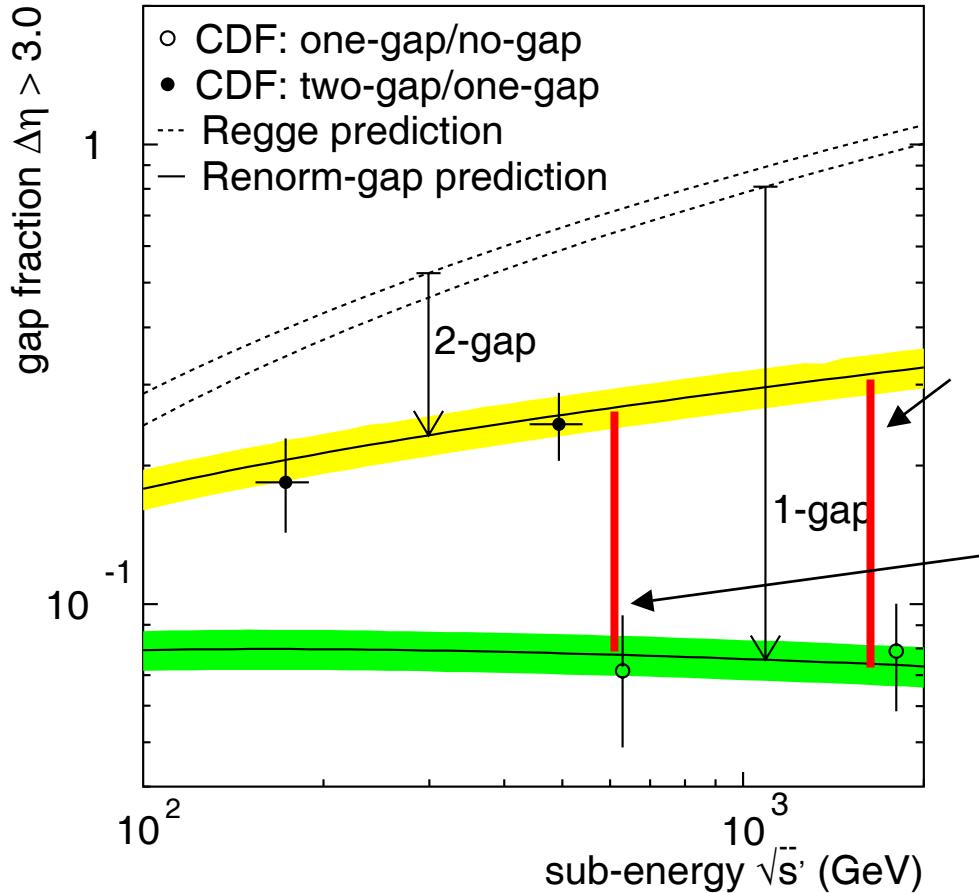


➤ One-gap cross sections are suppressed

➤ Two-gap/one-gap ratios are $\approx \kappa = 0.17$



Gap Survival Probability



$$S_{2\text{-gap}/1\text{-gap}}^{1\text{-gap}/0\text{-gap}}(1800 \text{ GeV}) \approx 0.23$$

$$S_{2\text{-gap}/1\text{-gap}}^{1\text{-gap}/0\text{-gap}}(630 \text{ GeV}) \approx 0.29$$

Results similar to predictions by:
 Gotsman-Levin-Maor
 Kaidalov-Khoze-Martin-Ryskin
 Soft color interactions

Soft Diffraction Summary

Experiment:

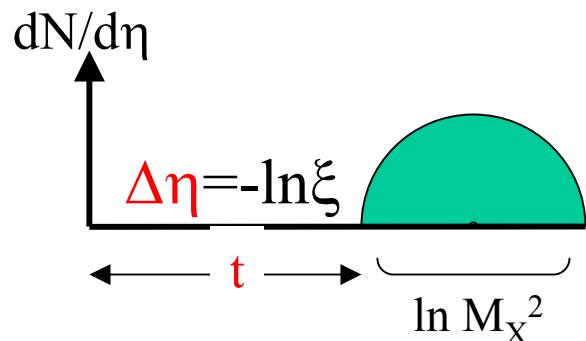
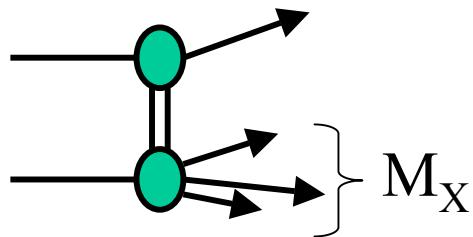
- M^2 - scaling
- Non-suppressed double-gap to single-gap ratios

Phenomenology:

- Generalized renormalization
- Obtain Pomeron intercept and triple-Pomeron coupling from inclusive PDF's and color factors

Hard Diffraction @ CDF

□ SOFT DIFFRACTION

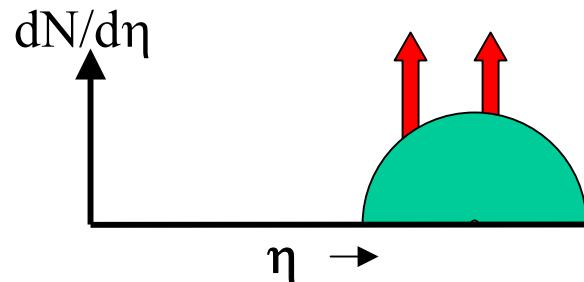
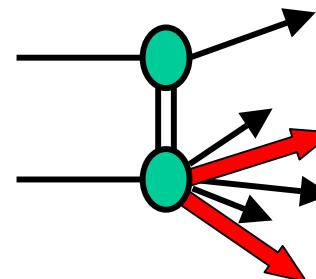


$$\xi = \Delta P_L / P_L$$

ξ =fractional momentum loss
of scattered (anti)proton

Variables: (ξ, t) or $(\Delta\eta, t)$

□ HARD DIFFRACTION



Additional variables: (x, Q^2)

$$x_{Bj} = \sum E_T^{jet} e^{-\eta^{jet}} / \sqrt{s}$$

$$x = \beta \xi, \quad Q^2 = (E_T^{jet})^2$$

Diffractive Fractions @ CDF

$\bar{p}p \rightarrow X + \text{gap}$
SD/ND fraction at 1800 GeV

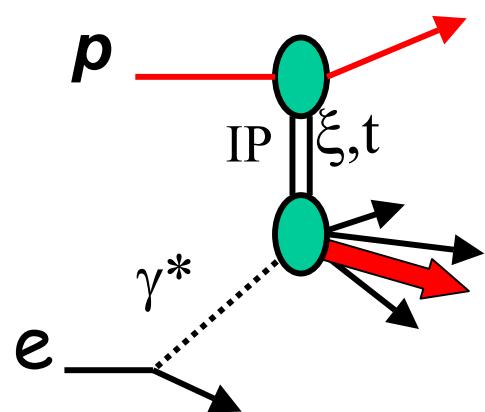
| X | Fraction(%) |
|-----------|-------------|
| W | 1.15 (0.55) |
| JJ | 0.75 (0.10) |
| b | 0.62 (0.25) |
| J/ ψ | 1.45 (0.25) |

All fractions $\sim 1\%$
→ Factorization $\sim \text{OK} @ \text{Tevatron}$
at fixed c.m.s. energy.

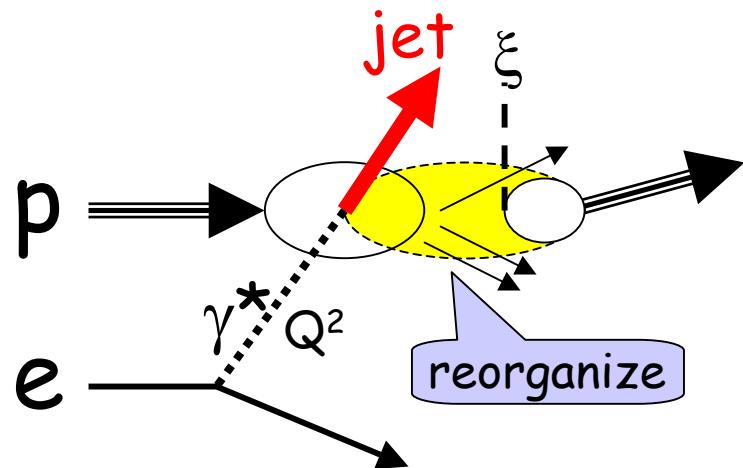
Diffractive DIS @ HERA

J. Collins: Factorization should hold

Pomeron exchange



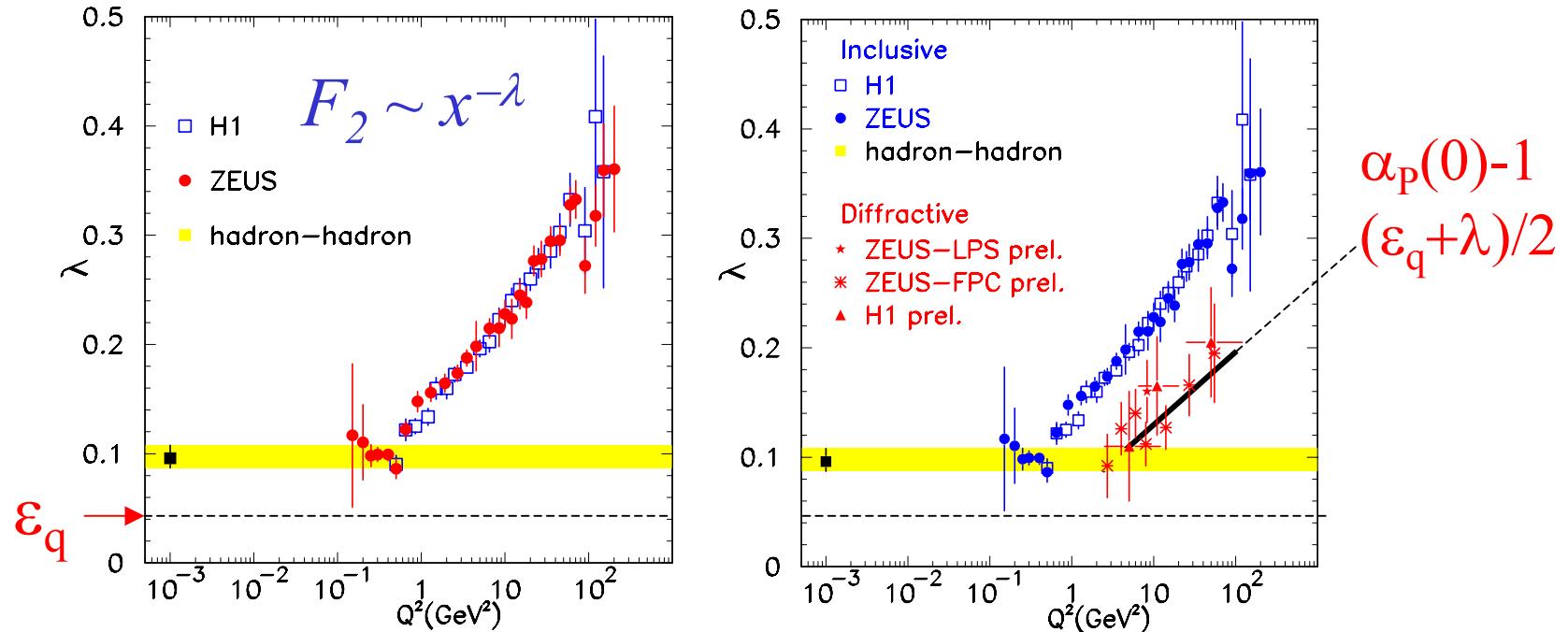
Color reorganization



$$F_2^{D(3)}(\xi, x, Q^2) \propto \frac{1}{\xi^{1+\epsilon}} \cdot F_2(x, Q^2)$$

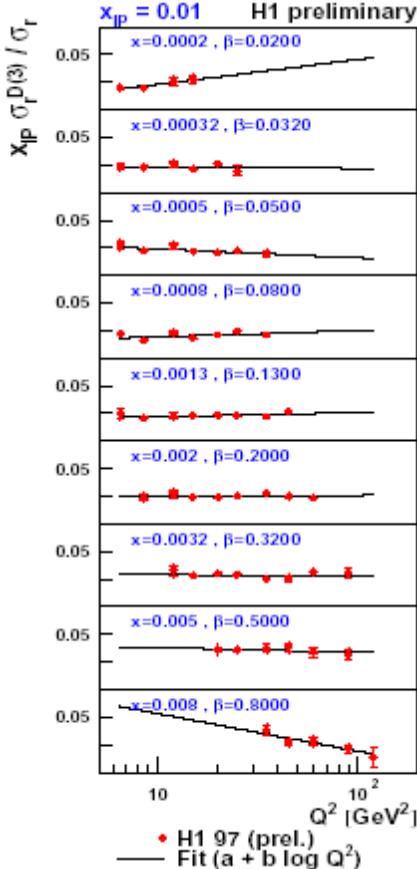
Inclusive vs Diffractive DIS

KG, “Diffraction: a New Approach,” J.Phys.G26:716-720,2000 e-Print Archive: [hep-ph/0001092](https://arxiv.org/abs/hep-ph/0001092)



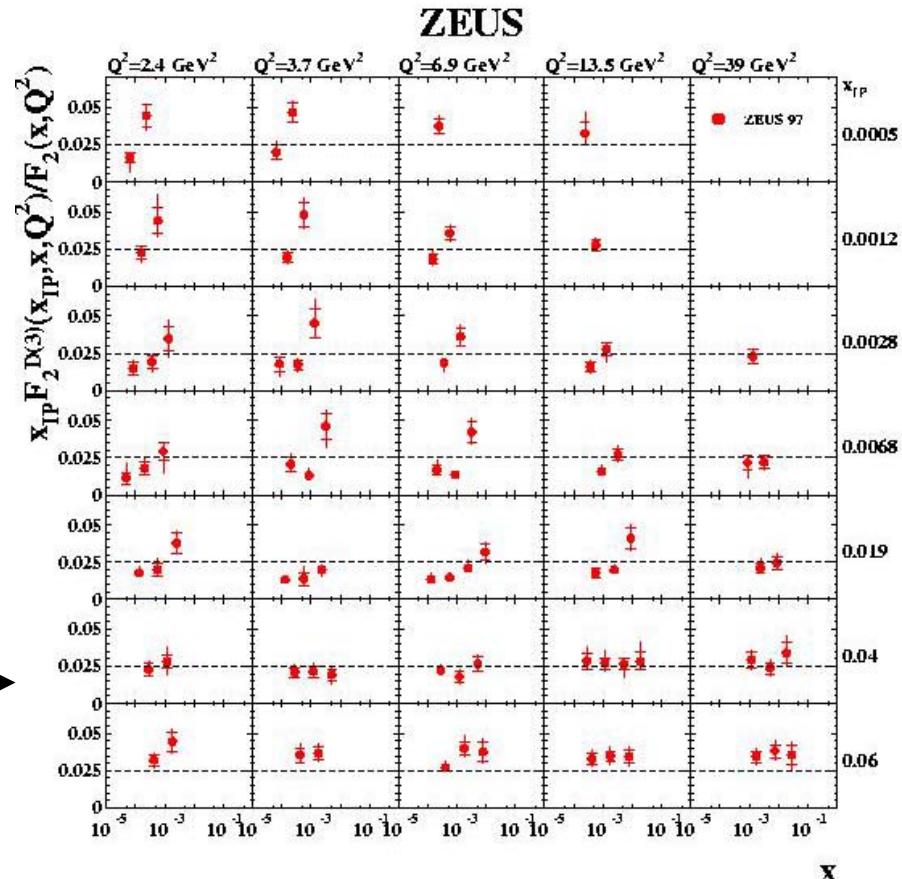
$$F_2^{D(3)}(\xi, \beta, Q^2) \propto \frac{1}{\xi^{1+\varepsilon}} \cdot \frac{C(Q^2)}{(\beta \xi)^{\lambda(Q^2)}} \propto \frac{1}{\xi^{1+\varepsilon+\lambda}} \cdot \frac{C}{\beta^\lambda}$$

$\sigma^{\text{diff}}/\sigma^{\text{incl}}$ DIS at HERA

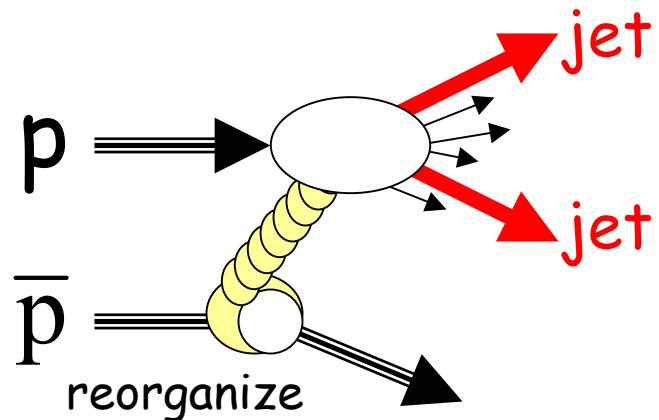


At fixed x :
flat Q^2 -dependence

At fixed Q^2 :
flat x -dependence



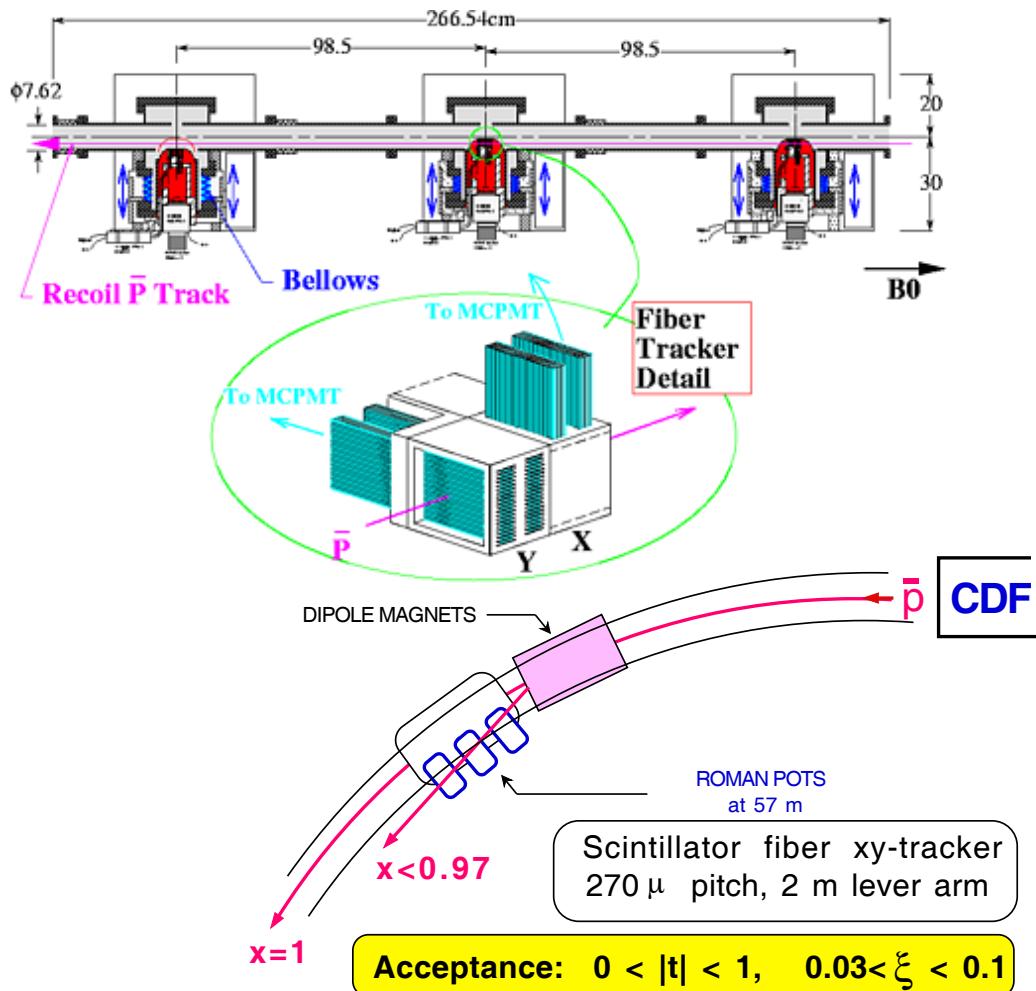
Diffractive Dijets @ Tevatron



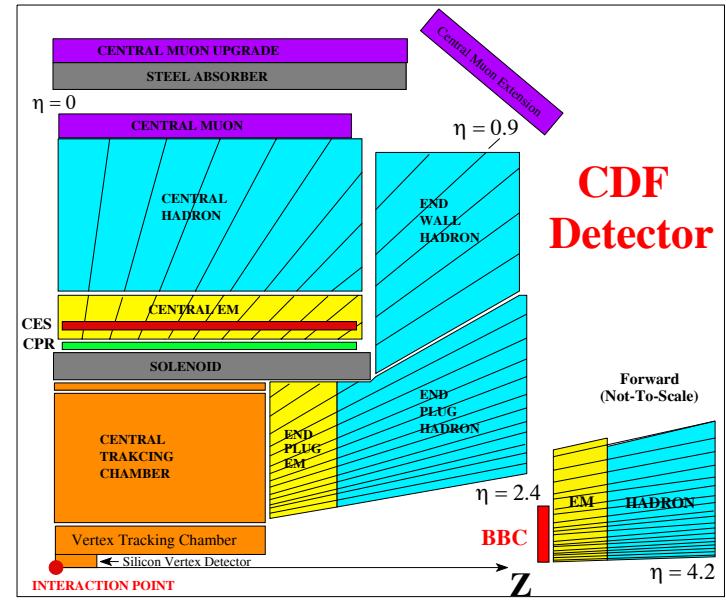
$$F^D(\xi, x, Q^2) \propto \frac{1}{\xi^{1+2\varepsilon}} \cdot F(x/\xi, Q^2)$$

CDF-IC

Run-IC



Run-IA,B

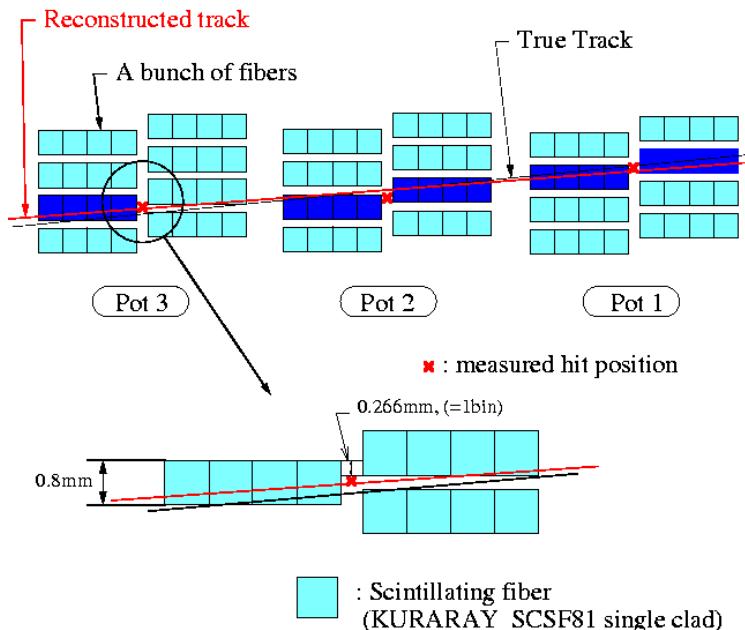


Forward Detectors

BBC $3.2 < \eta < 5.9$
FCAL $2.4 < \eta < 4.2$

Roman Pot tracking

FIBER TRACKER



Run 175066, Event 517876

POT-1

POT-2

POT-3

$\xi = 0.059$

POT-1

POT-2

POT-3

POT-Y Fiber

Diffractive Structure F'n @CDF

$$\bar{p} + p \rightarrow \bar{p} + Jet + Jet + X$$

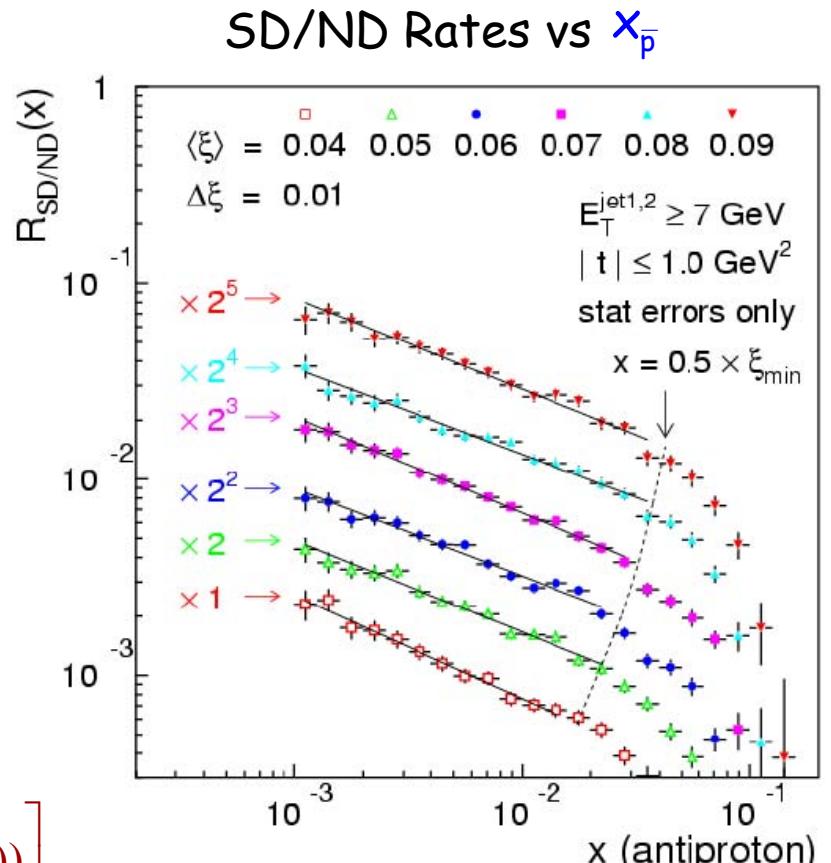
- Measure ratio of SD/ND dijet rates as a f'n of $x_{\bar{p}}$

$$x_{\bar{p}} \equiv p_{g,q}/p_{\bar{p}} = \frac{\sum_{i=1}^{2(3)} E_T^i \cdot e^{-\eta^i}}{\sqrt{s}}$$

$$R_{\frac{SD}{ND}}(x_{\bar{p}}) \approx R_0 \cdot x_{\bar{p}}^{-0.45}$$

- In LO-QCD ratio of rates equals ratio of structure fn's

$$F_{jj}(x_{\bar{p}}) = x_{\bar{p}} \left[g(x_{\bar{p}}) + \frac{C_F}{C_A} \sum (q_i(x_{\bar{p}}) + \bar{q}_i(x_{\bar{p}})) \right]$$



$F^D_{JJ}(\xi, \beta, Q^2)$ @ Tevatron

$$F^D(\xi, \beta, Q^2) \propto \frac{1}{\xi^{1+2\varepsilon}} \cdot \frac{C(Q^2)}{(x/\xi)^{\lambda(Q^2)}} \propto \frac{1}{(\beta s)^{2\varepsilon}} \cdot \frac{1}{\xi^{1+2\varepsilon}} \cdot \frac{C}{\beta^\lambda}$$

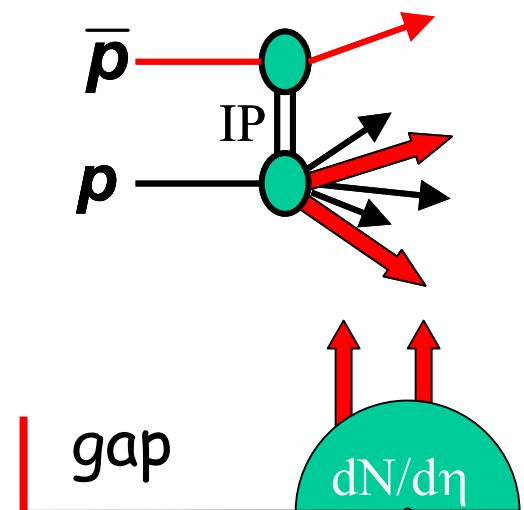
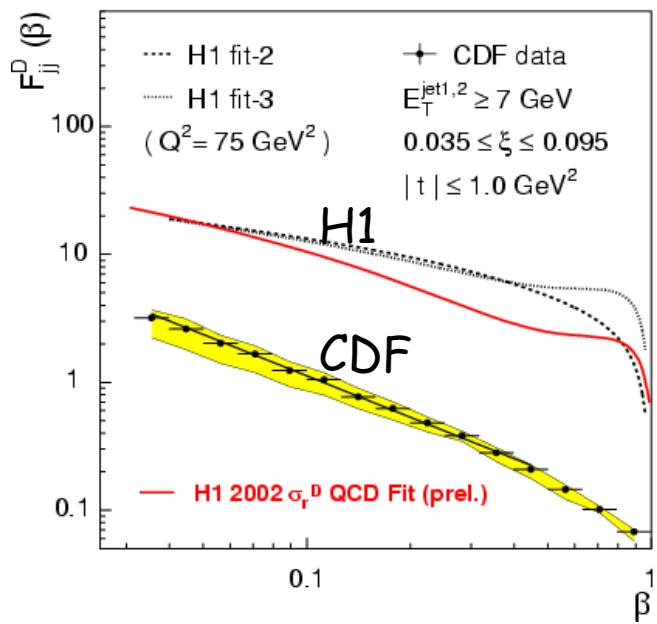
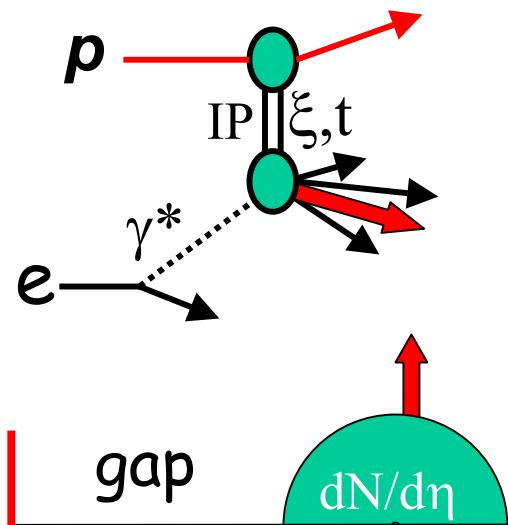
$$N_{\text{renorm}}^{-1} = \int_{\xi_{\min}}^1 \frac{d\xi}{\xi^{1+2\varepsilon}} \quad \xrightarrow{\xi_{\min} = \frac{x_{\min}}{\beta} \sim \frac{1}{\beta s}} \quad (\beta s)^{2\varepsilon}$$

$$\text{RENORM} \quad \Rightarrow \quad R_{ND}^{SD}(x) \sim \frac{1}{s^{2\varepsilon}} \frac{1}{\xi^{1-\lambda(Q^2)}} \cdot x^{-(2\varepsilon)}$$

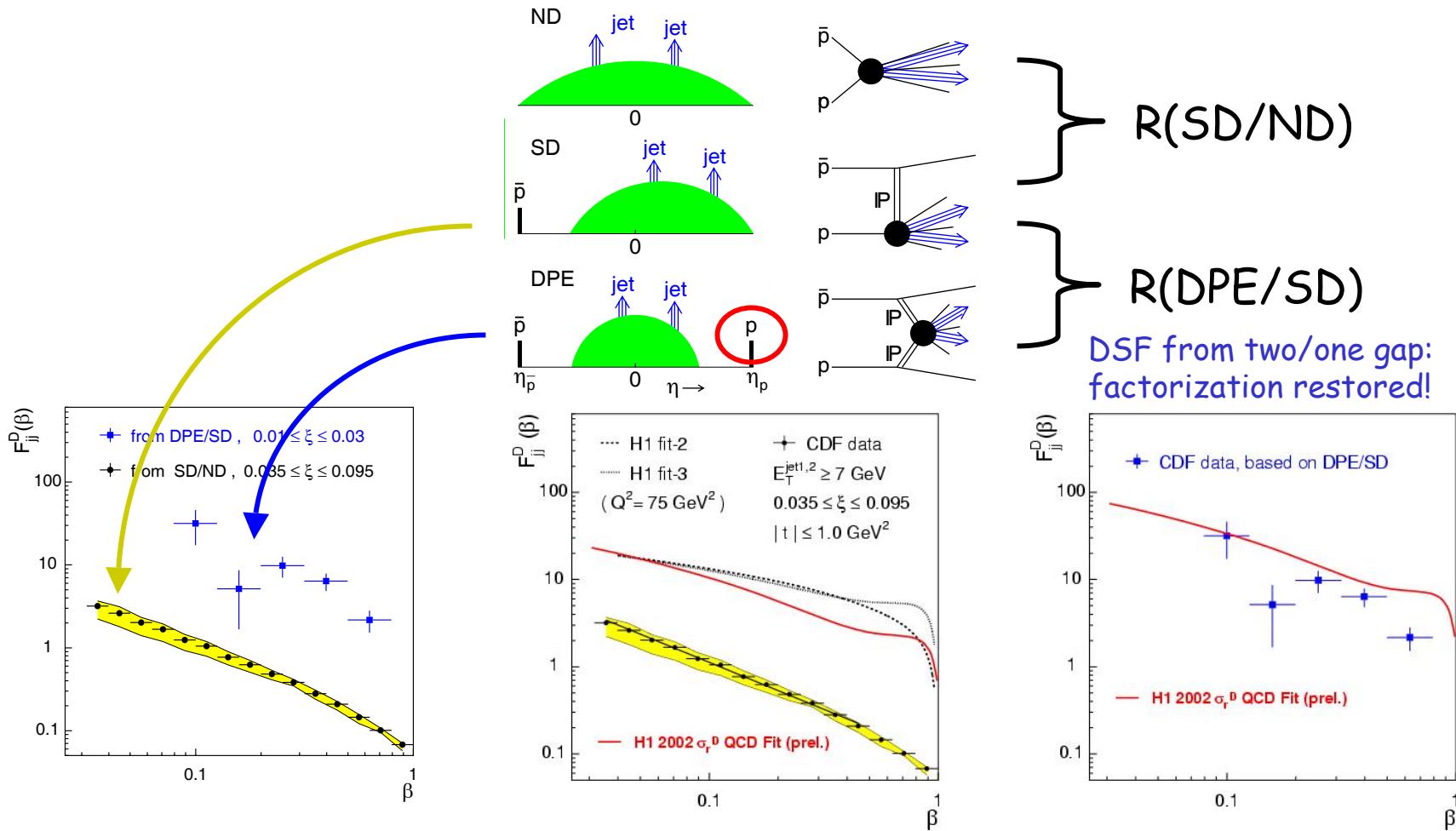
$\varepsilon_g = 0.2 \rightarrow x^{-0.4}$

Tevatron vs HERA: Factorization Breakdown

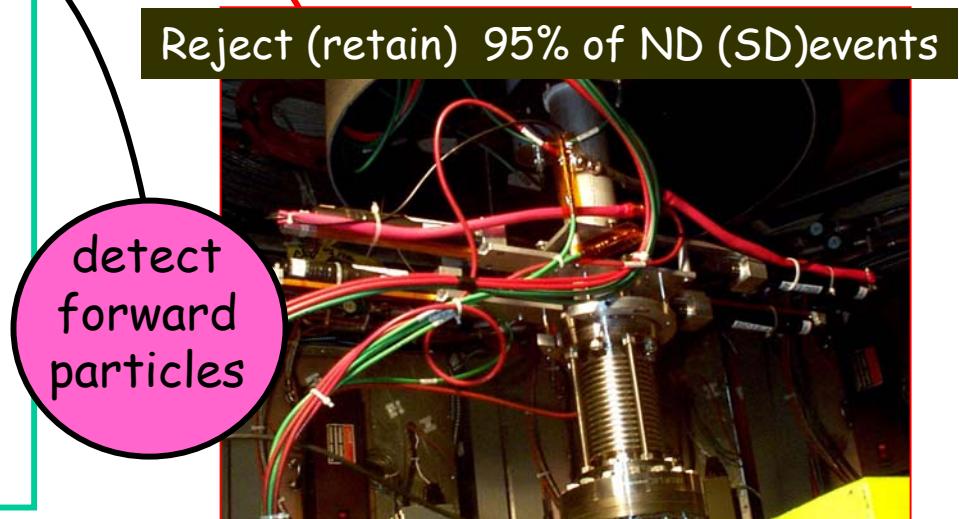
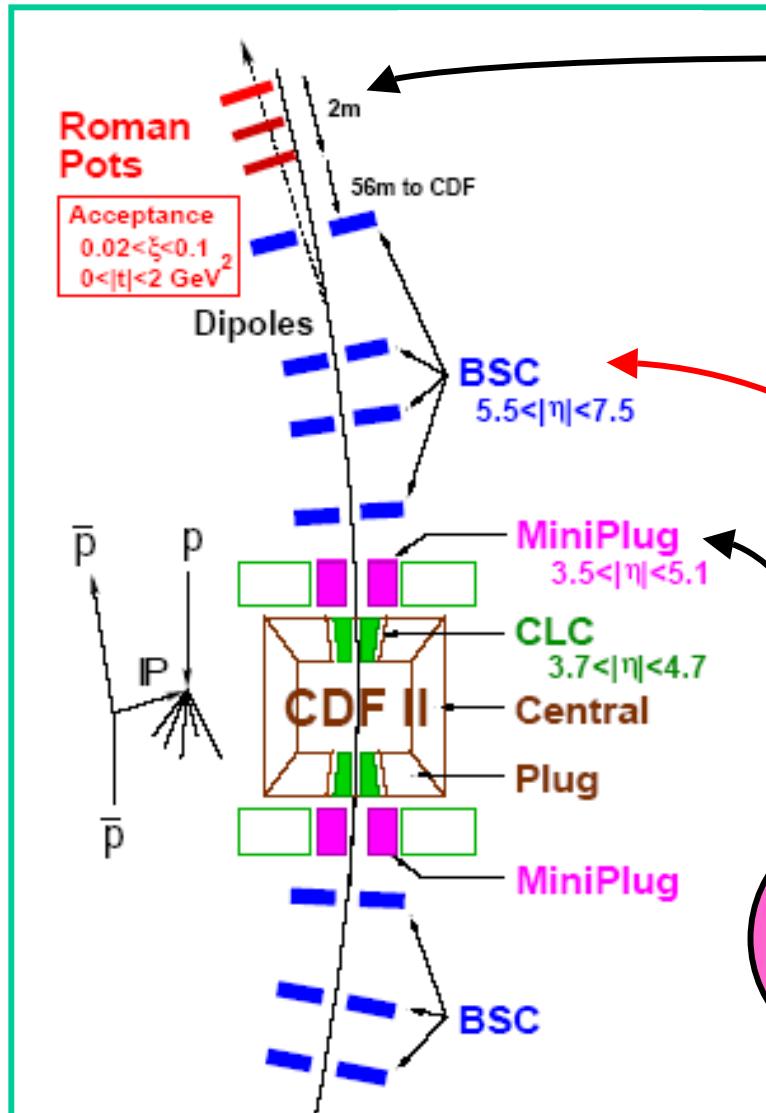
Predicted in KG, PLB 358 (1995) 379



Restoring Factorization



CDF-II

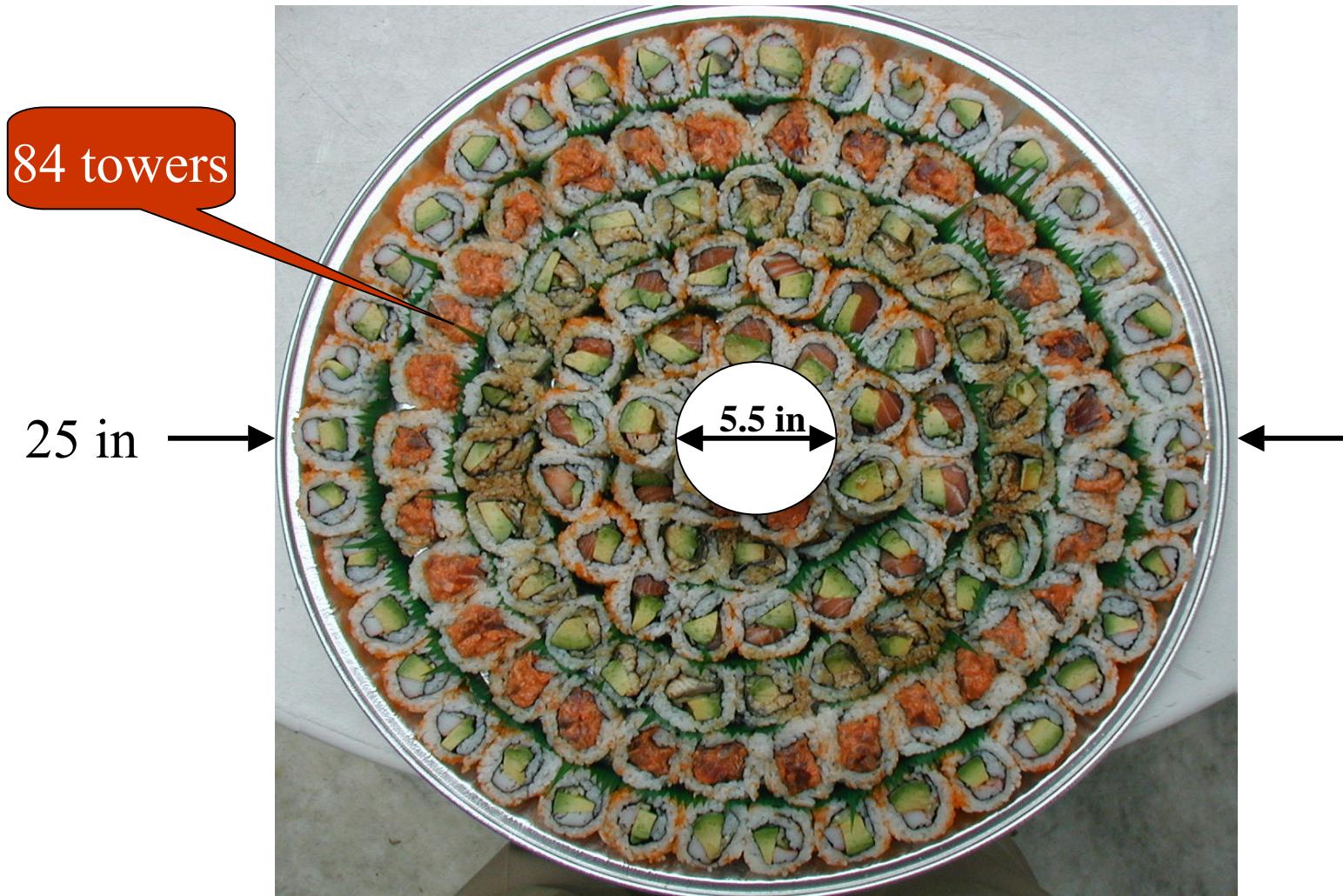


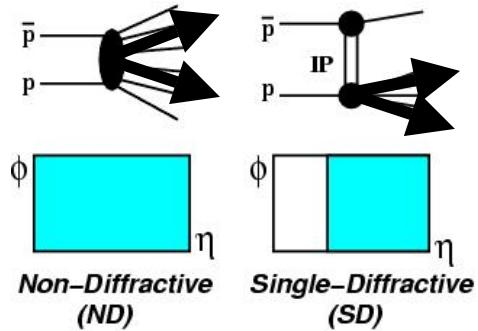
MiniPlug Calorimeter



About 1500 wavelength shifting fibers of 1 mm dia. are 'strung' through holes drilled in $36 \times \frac{1}{4}$ " lead plates sandwiched between reflective Al sheets and guided into bunches to be viewed individually by multi-channel photomultipliers.

Artist's View of MiniPlug

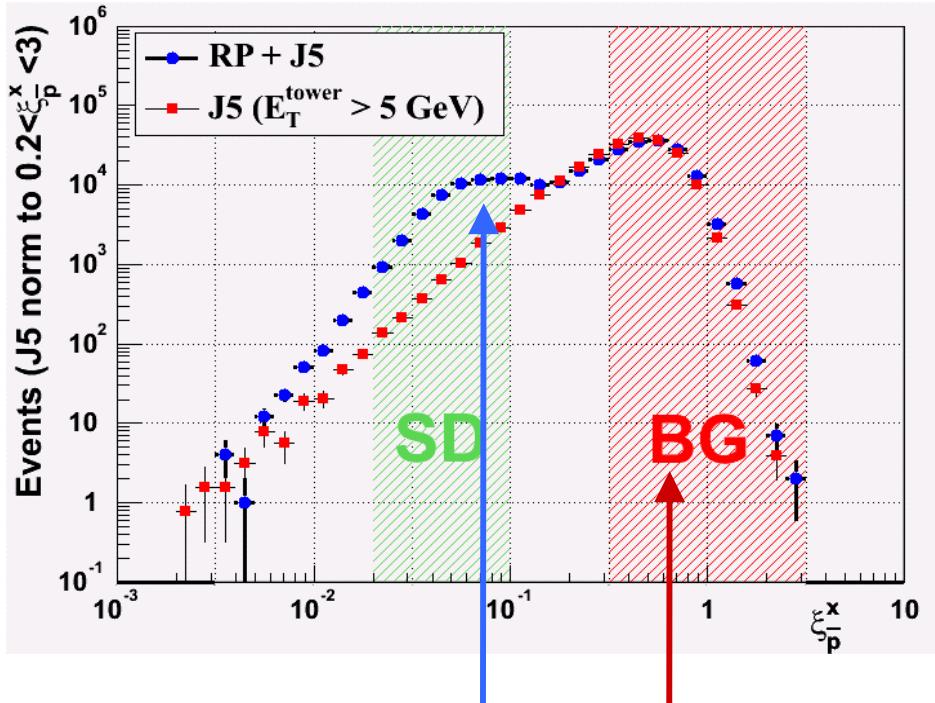
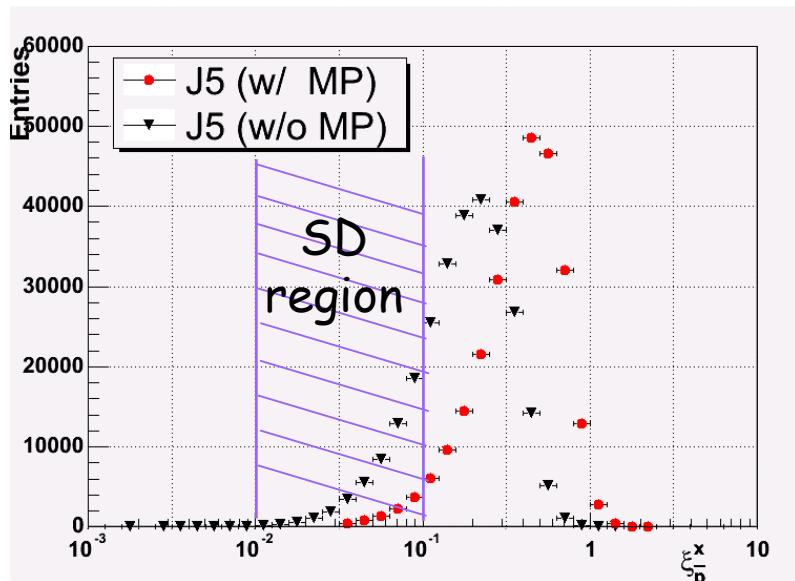




Diffractive dijets

ξ : momentum loss fraction of pbar

$$\xi = \frac{\sum_{\text{(all towers)}} E_T e^{-\eta}}{\sqrt{s}}$$



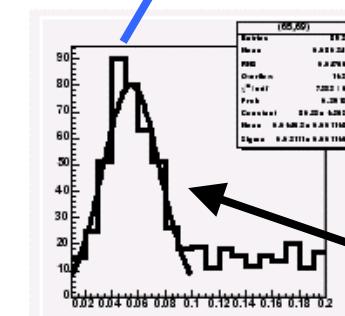
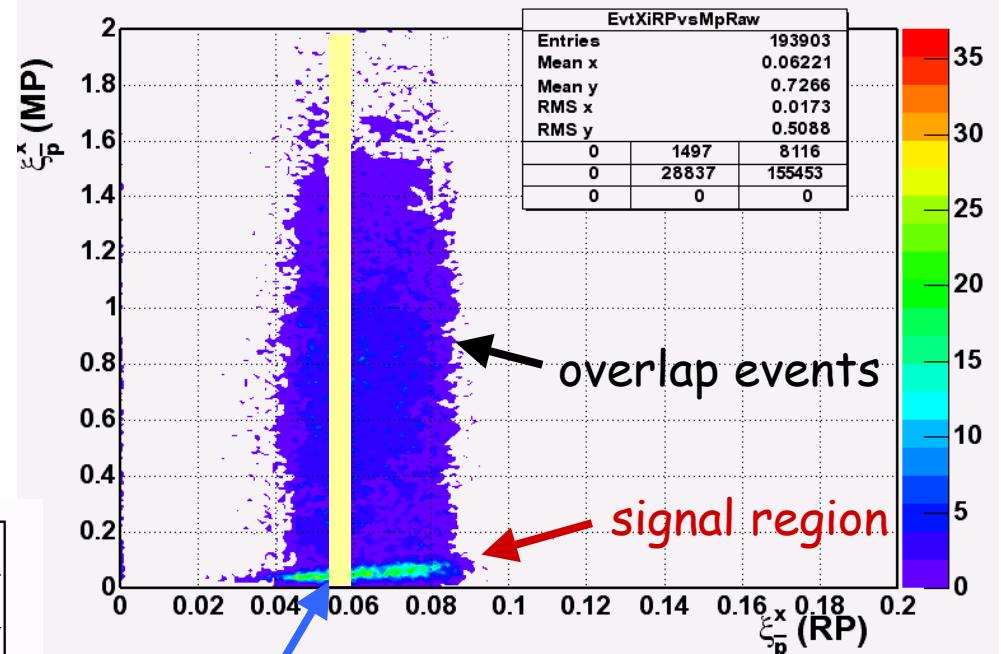
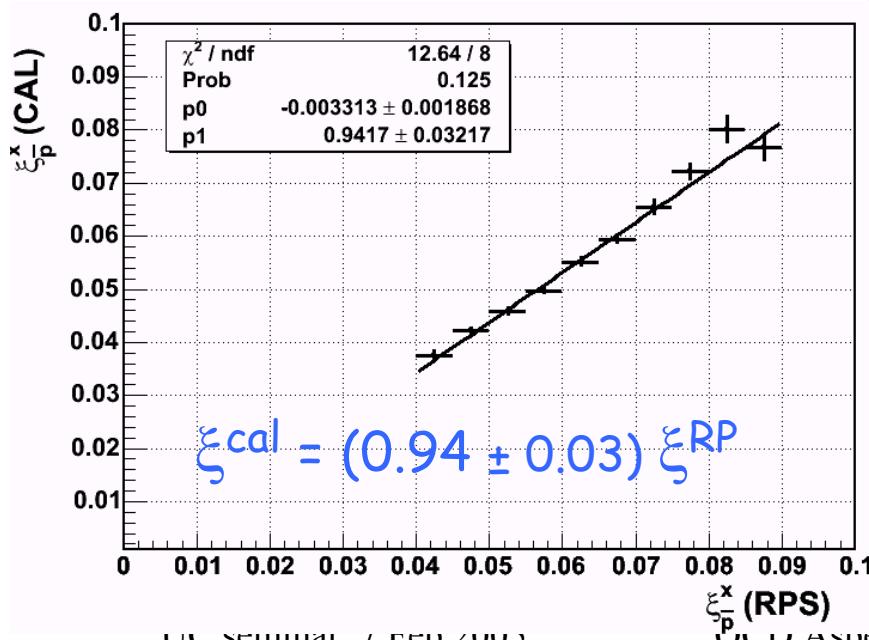
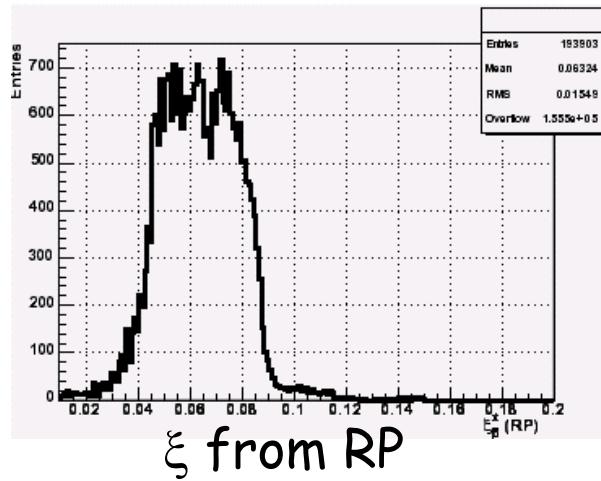
Approx. flat at $\xi < 0.1$

$$\frac{d\sigma}{d\xi} \propto \frac{1}{\xi} \rightarrow \frac{d\sigma}{d(\log \xi)} = \text{const}$$

overlap events

MP energy scale: $\pm 25\% \rightarrow \Delta \log \xi = \pm 0.1$
 RP acceptance ($0.03 < \xi < 0.1$) $\sim 80\%$ (Run I)

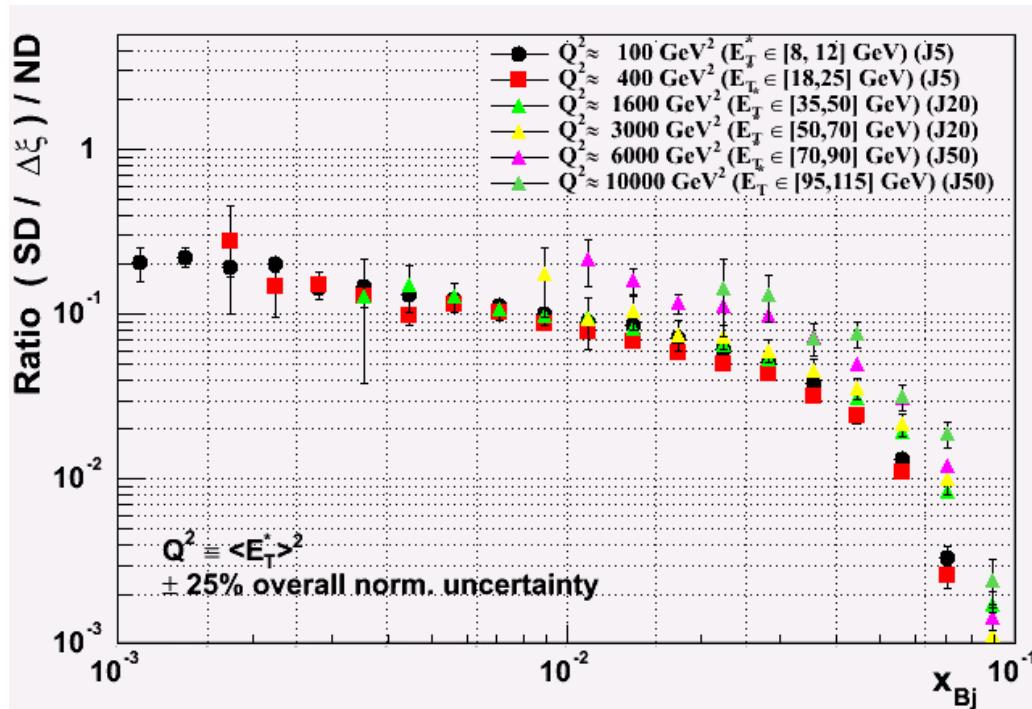
ξ : RP vs calorimeter



ξ_{CAL}^x distribution
for slice of ξ_{RP}^x

$\sigma/\text{mean} \sim 30\%$

Q^2 -dependence of SD/ND ratio

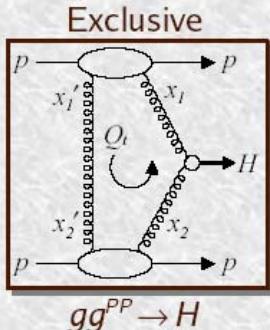


- No appreciable Q^2 dependence
within $100 < Q^2 < 10,000 \text{ GeV}^2$
- ⇒ Pomeron evolves similarly to proton

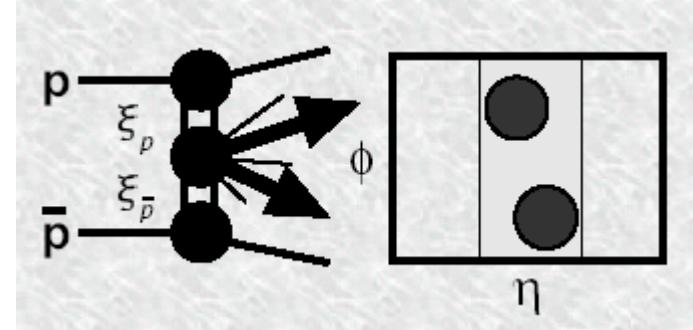
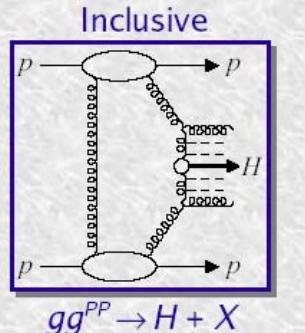
Exclusive Dijets in DPE

Interest in diffractive Higgs production

Calibrate on exclusive dijets



Khoze, Martin,
Ryskin
Eur. Phys. J.
C23, 311 (2001),
C26, 229 (2002)



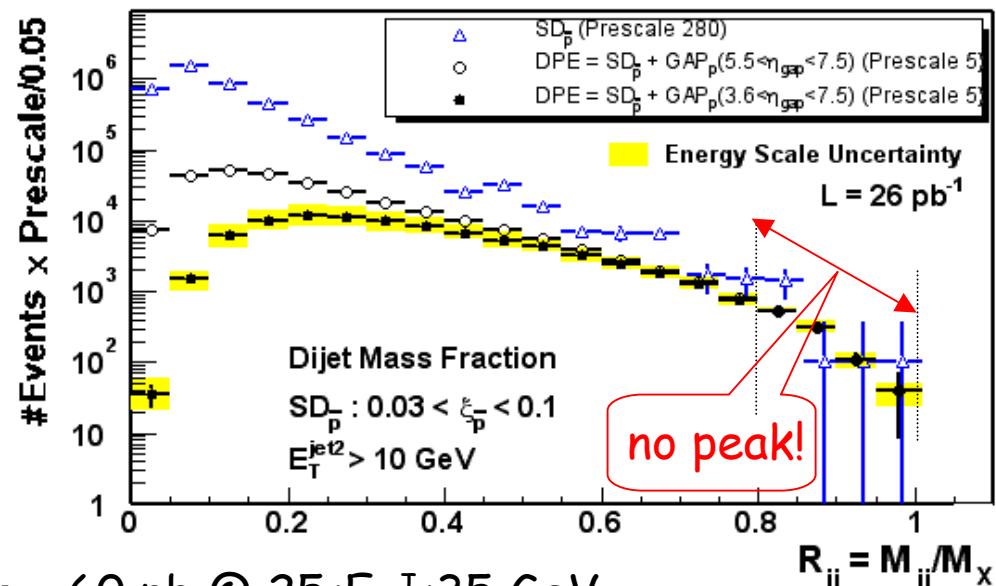
Dijet mass fraction

$$R_{jj} = \frac{M_{jj}^{\text{cone}}}{M_X}$$

| E_T^{jet} | $\sigma_{\text{DPE}}^{\text{excl jj}}(R_{jj} > 0.8)$ |
|--------------------|--|
| 10 GeV | $970 \pm 65 \pm 272 \text{ pb}$ |
| 25 GeV | $34 \pm 5 \pm 10 \text{ pb}$ |

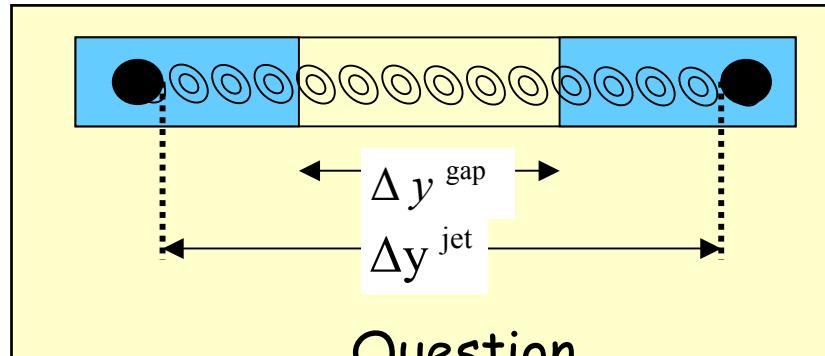
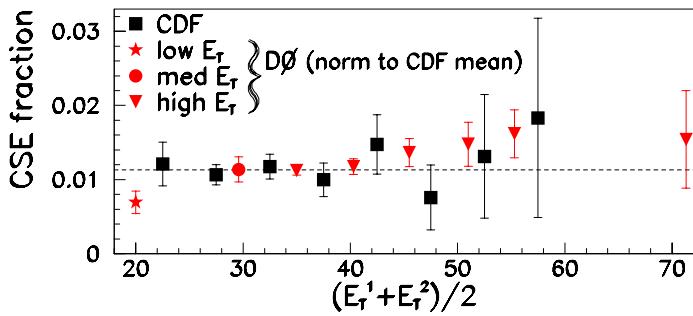
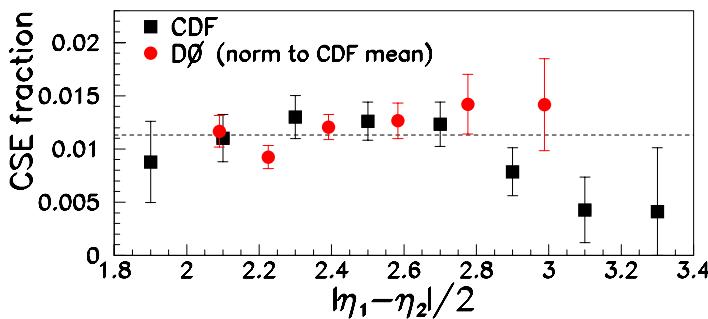
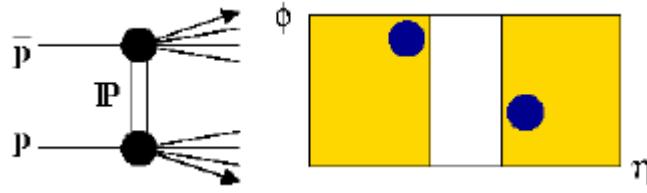
Upper limit for excl DPE-jj
consistent with theory: KMR → 60 pb @ $25 < E_T^{\text{J}} < 35 \text{ GeV}$

CDF Run II Preliminary



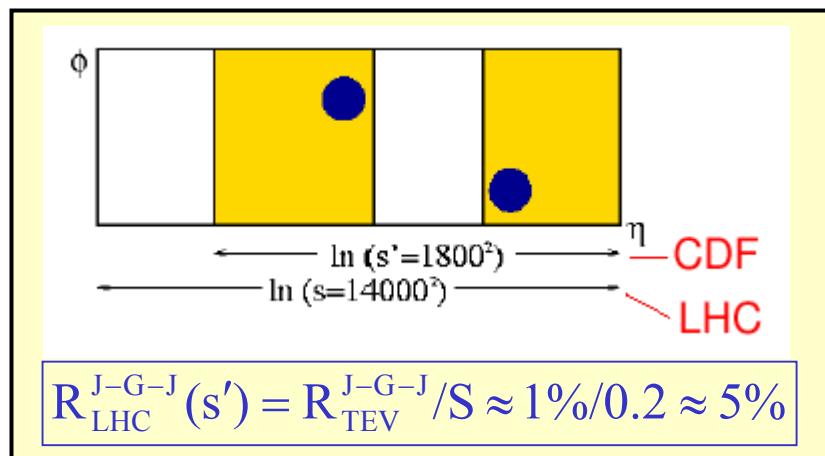
Gap Between Jets

$\bar{p} + p \rightarrow \text{Jet} + \text{Gap} + \text{Jet}$



Question

$$\Delta y^{\text{gap}} \xleftarrow{???)} \Delta y^{\text{jet}}$$



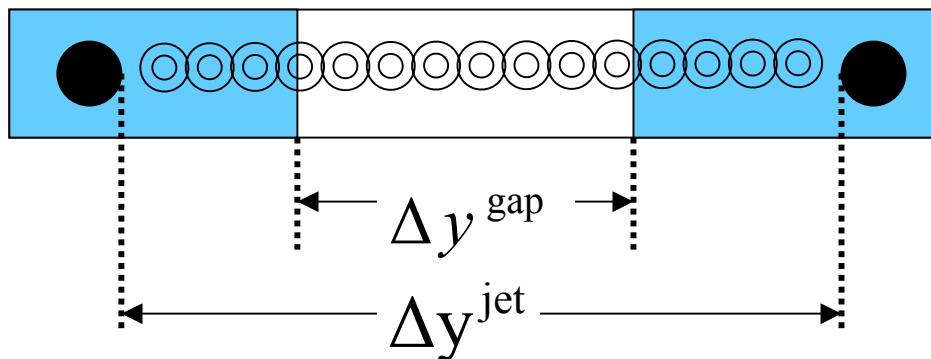
CDF2LHC

TOPIC

- (Q^2, t) dependence of DSF
- Exclusive χ_c production
- Low mass states in DPE
- Exclusive b-bbar production in DPE
- ξ -dependence of DSF
- Jet-gap-Jet w/jets in miniplugs

STATUS

- close to ready
- close to ready
- need good trigger
- need b-trigger
- need low lum run
- need low lum run



$\Delta y^{\text{gap}} = \Delta y^{\text{jet}} \Rightarrow \text{BFKL}$
 $\Delta y^{\text{gap}} \neq \Delta y^{\text{jet}} \Rightarrow \text{composite}$

Summary

SOFT DIFFRACTION

- M^2 - scaling
- Non-suppressed double-gap to single-gap ratios

HARD DIFFRACTION

- Flavor-independent SD/ND ratio
- Little or no Q^2 -dependence in SD/ND ratio

- ✓ Universality of gap prob. across soft and hard diffraction
- ✓ Pomeron evolves similarly to proton

Diffraction appears to be a low- x partonic exchange subject to color constraints