

Diffractive and total pp cross sections at the LHC and beyond

Konstantin Goulianos

The Rockefeller University

<http://physics.rockefeller.edu/dino/myhtml/conference.html>

DIFFRACTION 2010

International Workshop on Diffraction in High-Energy Physics

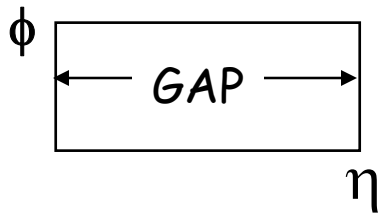
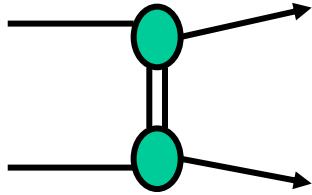


CONTENTS

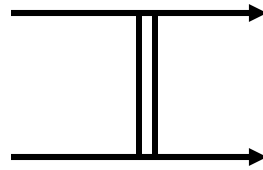
- Introduction
- Diffractive cross sections
- The total cross section
- Ratio of pomeron intercept to slope
- Conclusions

Diffractive pp/ $\bar{p}p$ Processes

Elastic scattering

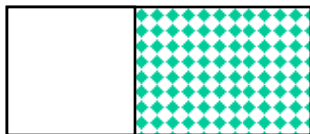
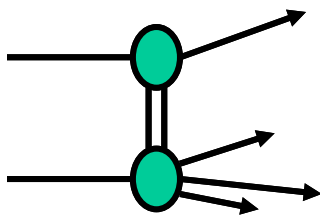
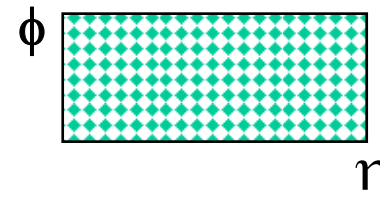
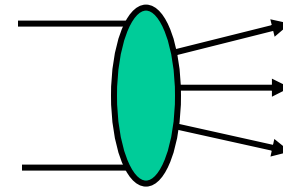


$$\sigma_T = \text{Im } f_{el}(t=0)$$

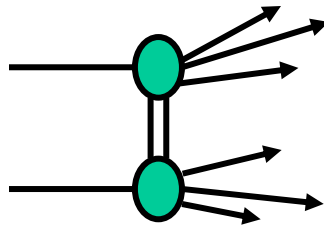


OPTICAL
THEOREM

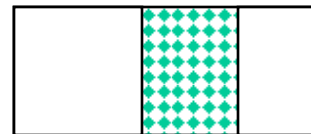
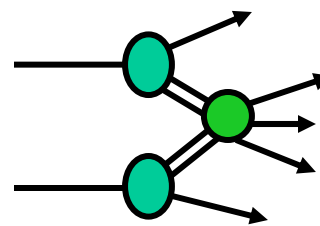
Total cross section



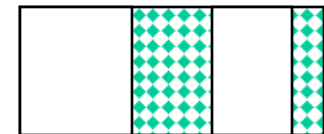
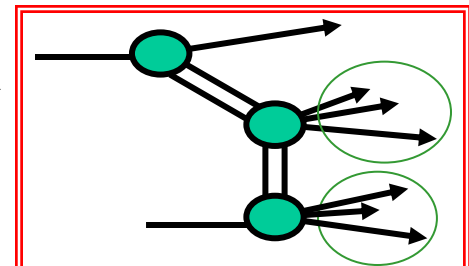
SD



DD



DPE

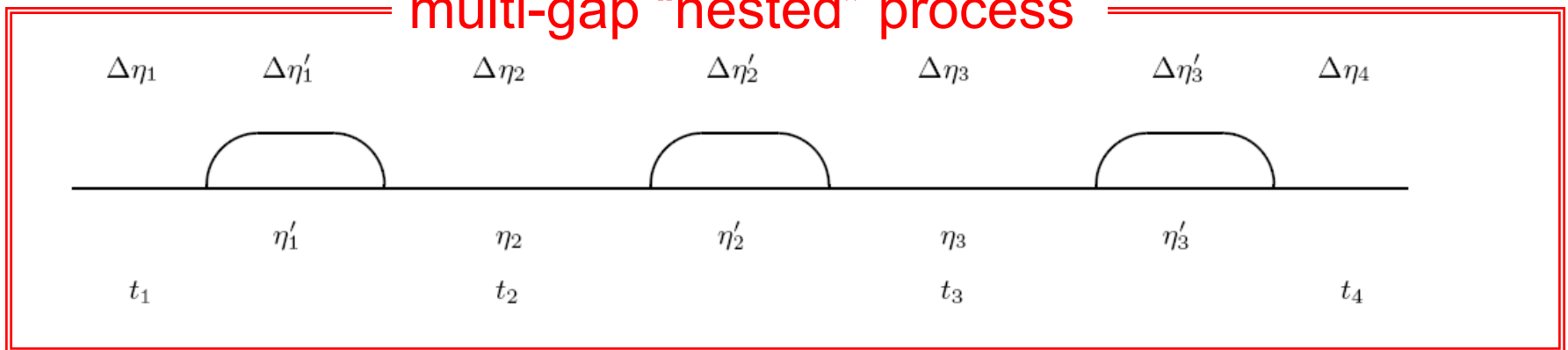


SDD=SD+DD

Basic and combined (“nested”) diffractive processes

acronym	basic diffractive processes
$\text{SD}_{\bar{p}}$	$\bar{p}p \rightarrow \bar{p} + \text{gap} + [p \rightarrow X_p],$
SD_p	$\bar{p}p \rightarrow [\bar{p} \rightarrow X_{\bar{p}}] + \text{gap} + p,$
DD	$\bar{p}p \rightarrow [\bar{p} \rightarrow X_{\bar{p}}] + \text{gap} + [p \rightarrow X_p],$
DPE	$\bar{p}p \rightarrow \bar{p} + \text{gap} + X_c + \text{gap} + p,$
	2-gap combinations of SD and DD
$\text{SDD}_{\bar{p}}$	$\bar{p}p \rightarrow \bar{p} + \text{gap} + X_c + \text{gap} + [p \rightarrow X_p],$
SDD_p	$\bar{p}p \rightarrow [\bar{p} \rightarrow X_{\bar{p}}] + \text{gap} + X_c + \text{gap} + p.$

multi-gap “nested” process



The problem: the Regge theory description violates unitarity at high s

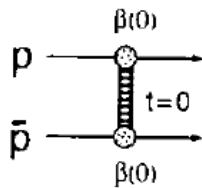
$$\left(\frac{d\sigma_{el}}{dt}\right)_{t=0} \sim \left(\frac{s}{s_0}\right)^{2\epsilon}, \quad \sigma_t \sim \left(\frac{s}{s_0}\right)^\epsilon, \quad \sigma_{sd} \sim \left(\frac{s}{s_0}\right)^{2\epsilon}$$

- $d\sigma/dt$ σ_{sd} grows faster than σ_t as s increases
→ unitarity violation at high s
(similarly for partial x-sections in impact parameter space)
- the unitarity limit is already reached at $\sqrt{s} \sim 2$ TeV

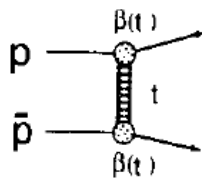
Standard Regge Theory

KG-1995: PLB 358, 379 (1995)

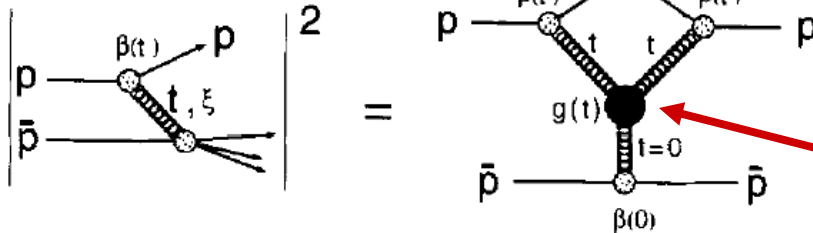
TOTAL CROSS SECTION



ELASTIC SCATTERING



SINGLE DIFFRACTION DISSOCIATION



Parameters:

- ❑ s_0, s_0' and $g(t)$
- ❑ set $s_0' = s_0$ (universal IP)
- ❑ $g(t) \rightarrow g(0) \equiv g_{PPP} \rightarrow \text{KG-1995}$
- ❑ determine s_0 and g_{PPP} – how?

$$\sigma_T = \beta_1(0)\beta_2(0) \left(\frac{s}{s_0}\right)^{\alpha(0)-1} = \sigma_0^{p\bar{p}} \left(\frac{s}{s_0}\right)^\epsilon \quad (1)$$

$$\begin{aligned} \frac{d\sigma_{el}}{dt} &= \frac{\beta_1^2(t)\beta_2^2(t)}{16\pi} \left(\frac{s}{s_0}\right)^{2[\alpha(t)-1]} \\ &= \frac{\sigma_T^2}{16\pi} \left(\frac{s}{s_0}\right)^{2\alpha't} F^4(t) \approx \frac{\sigma_T^2}{16\pi} e^{b_{el}(s)t} \end{aligned} \quad (2)$$

$$F^4(t) \approx e^{b_{0,el}t} \Rightarrow b_{el}(s) = b_{0,el} + 2\alpha' \ln \left(\frac{s}{s_0}\right) \quad (3)$$

$$\begin{aligned} \frac{d^2\sigma_{sd}}{dt d\xi} &= \frac{\beta_1^2(t)}{16\pi} \xi^{1-2\alpha(t)} \left[\beta_2(0) g(t) \left(\frac{s'}{s_0'}\right)^{\alpha(0)-1} \right] \\ &= f_{P/p}(\xi, t) \sigma_T^{p\bar{p}}(s', t) \end{aligned} \quad (4)$$

Global fit to $p^\pm p$, π^\pm , $K^\pm p$ x-sections

CMG-1996
PLB 389, 176 (1996)

A new determination of the soft pomeron intercept

R.J.M. Covolan¹, J. Montanha², K. Goulios³

Regge theory eikonalized

INPUT

$$\alpha_{f/a} = 0.68 + 0.82 t$$

$$\alpha_{\omega/\rho} = 0.46 + 0.92 t$$

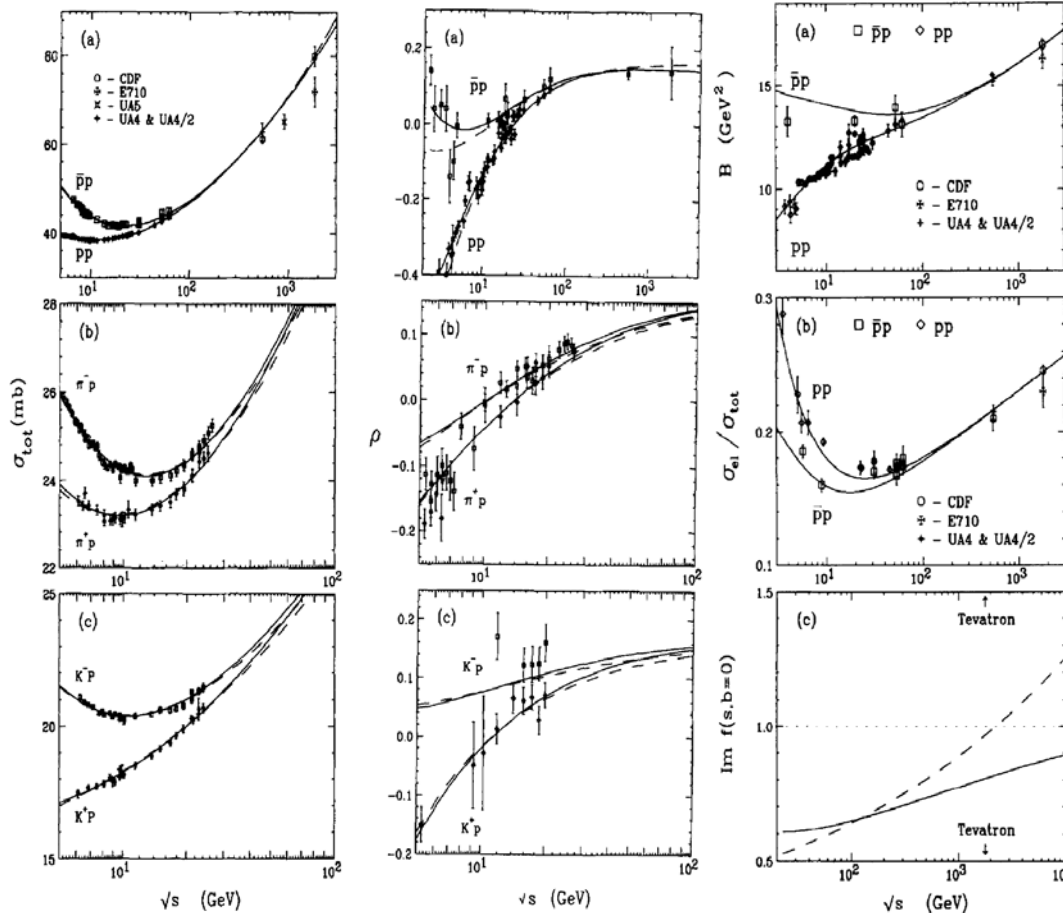
$$\alpha'_{\mathbf{P}} = 0.25 \text{ GeV}^{-2}$$

RESULTS

$$\alpha_{0,\mathbf{P}}^{\text{Born}} = 1.104 \pm 0.002, \quad \alpha_{0,\mathbf{P}}^{\text{Eik}} = 1.122 \pm 0.002$$

$$\sigma_{\text{tot}}^{p^\pm p} = 16.79 s^{0.104} + 60.81 s^{-0.32} \mp 31.68 s^{-0.54}$$

negligible



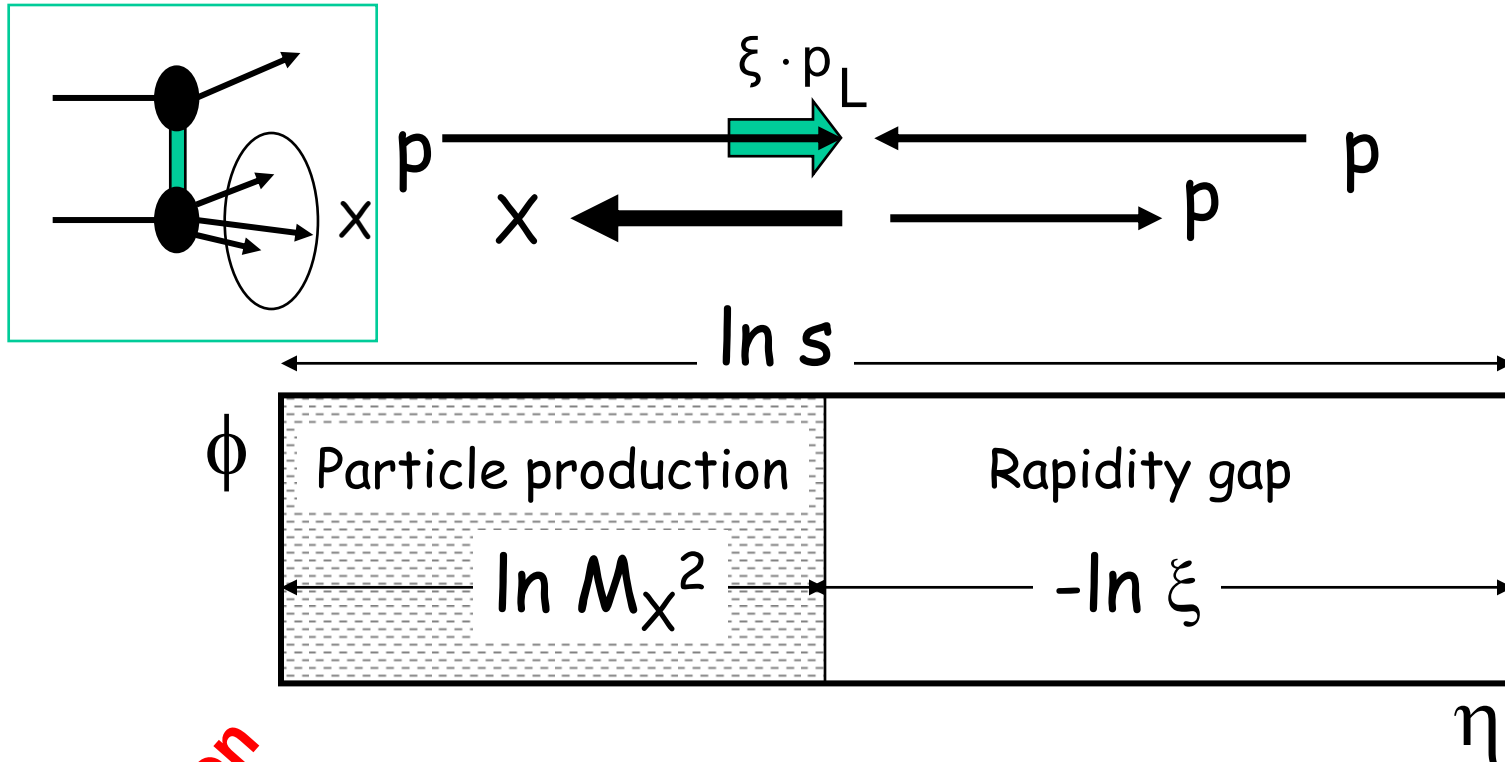
Renormalization

→ the key to diffraction in QCD



Diffractive gaps

definition: gaps not exponentially suppressed

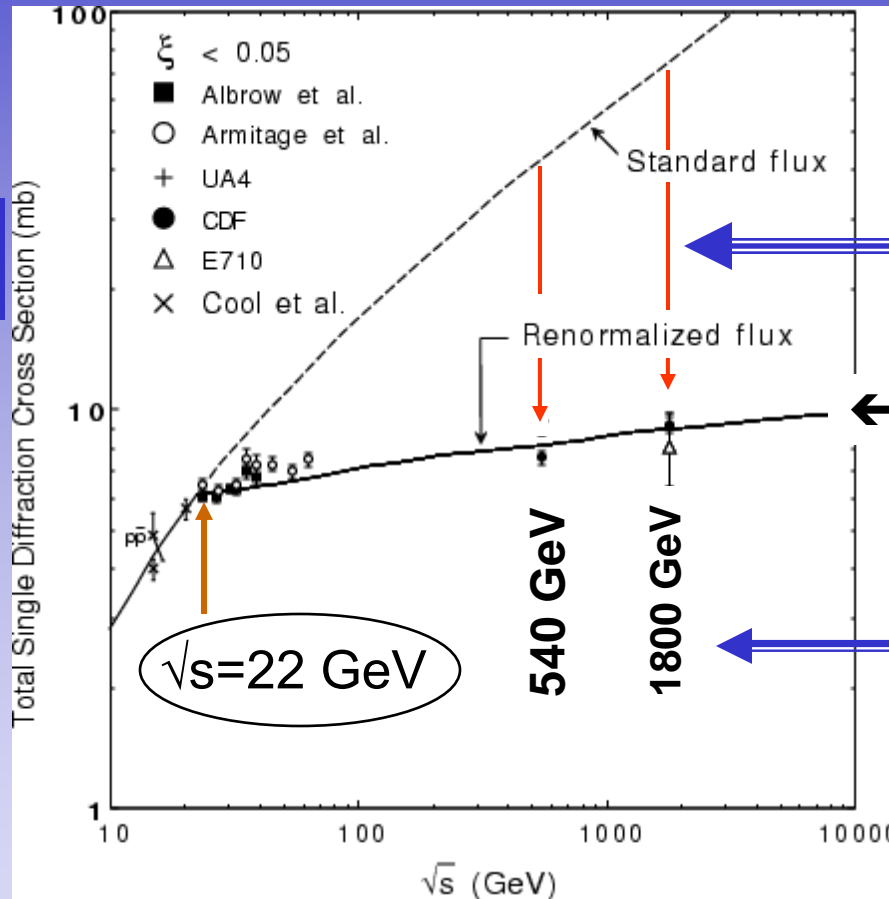
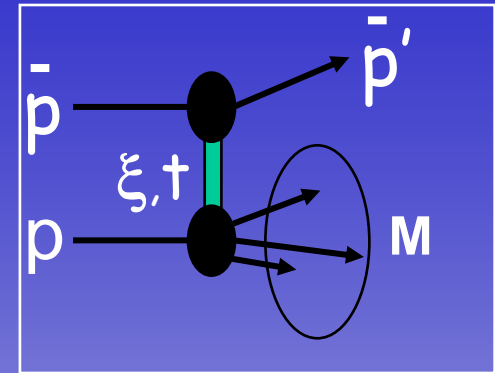


No radiation \rightarrow

$$\left(\frac{d\sigma}{d\Delta\eta} \right)_{t=0} \approx \text{constant} \Rightarrow \frac{d\sigma}{dM^2} \sim \frac{1}{M^2} \Rightarrow \frac{d\sigma}{d\xi} \sim \frac{1}{\xi}$$

σ_{SD}^T ($\bar{p}p$ & pp) - data

→ suppressed relative to Regge for $\sqrt{s} > 22$ GeV



σ_{SD}^T mb

Factor of ~8 (~5) suppression at $\sqrt{s} = 1800$ (540) GeV

← RENORMALIZATION MODEL

KG, PLB 358, 379 (1995)

← CDF Run I results

M² distribution: data

→ $d\sigma/dM^2|_{t=-0.05} \sim$ independent of s over 6 orders of magnitude!

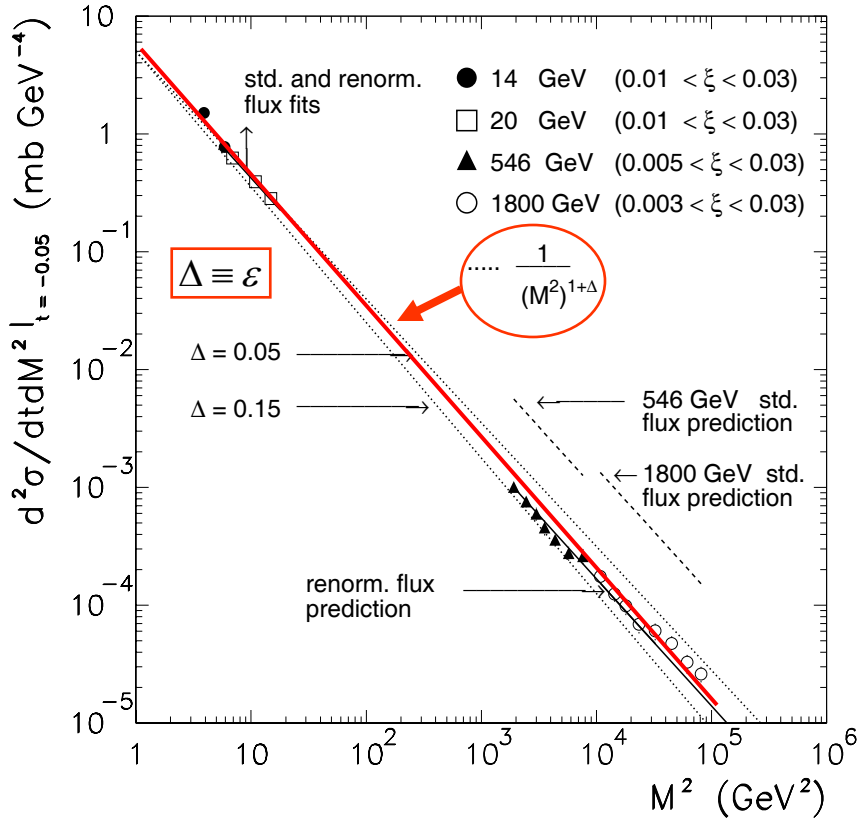
Regge

$$\frac{d\sigma}{dM^2} \propto \frac{s^{2\varepsilon}}{(M^2)^{1+\varepsilon}} \rightarrow 1$$

Independent of S over 6 orders of magnitude in M^2

→ **M² scaling**

KG&JM, PRD 59 (1999) 114017

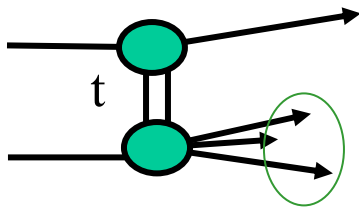


→ factorization breaks down to ensure M² scaling

Single diffraction renormalized – (1)

CORFU-2001: hep-ph/0203141

EDS 2009: http://arxiv.org/PS_cache/arxiv/pdf/1002/1002.3527v1.pdf



2 independent variables: $t, \Delta y$

color factor $\kappa = \frac{g_{IP-IP-IP}(t)}{\beta_{IP-p-p}(0)} \approx 0.17$

$$\frac{d^2 \sigma}{dt d\Delta y} = \underbrace{C \cdot F_p^2(t) \cdot \left\{ e^{(\varepsilon + \alpha' t) \Delta y} \right\}^2}_{\text{gap probability}} \cdot \underbrace{\kappa \cdot \left\{ \sigma_o e^{\varepsilon \Delta y'} \right\}}_{\text{sub-energy x-section}}$$



Gap probability → (re)normalize to unity

Single diffraction renormalized – (2)

color factor

$$\kappa = \frac{g_{IP-IP-IP}(t)}{\beta_{IP-p-p}(0)} \approx 0.17$$

Experimentally:

KG&JM, PRD 59 (114017) 1999

$$\kappa = \frac{g_{IP-IP-IP}}{\beta_{IP-p}} = 0.17 \pm 0.02, \quad \varepsilon = 0.104$$

QCD: $\kappa = f_g \times \frac{1}{N_c^2 - 1} + f_q \times \frac{1}{N_c} \xrightarrow{Q^2 = 1} \approx 0.75 \times \frac{1}{8} + 0.25 \times \frac{1}{3} = 0.18$

Single diffraction renormalized - (3)

$$\frac{d^2 \sigma_{sd}(s, M^2, t)}{dM^2 dt} = \left[\frac{\sigma_0}{16\pi} \sigma_0^{IPp} \right] \frac{s^{2\epsilon}}{N(s, s_0)} \frac{e^{bt}}{(M^2)^{1+\epsilon}}$$

$$b = b_0 + 2\alpha' \ln \frac{s}{M^2} \quad s_0^{\text{CMG}} = (3.7 \pm 1.5) \text{ GeV}^2$$

$$N(s, s_0) \equiv \int_{\xi_{\min}}^{\xi_{\max}} d\xi \int_{t=0}^{-\infty} dt f_{\mathbb{P}/p}(\xi, t) \xrightarrow{s \rightarrow \infty} \sim s_0^\epsilon \frac{s^{2\epsilon}}{\ln s}$$

$$\frac{d^2 \sigma_{sd}(s, M^2, t)}{dM^2 dt} \xrightarrow{s \rightarrow \infty} \sim \ln s \frac{e^{bt}}{(M^2)^{1+\epsilon}}$$

$$\sigma_{sd} \xrightarrow{s \rightarrow \infty} \sim \frac{\ln s}{b \rightarrow \ln s} \Rightarrow \text{const}$$

set to unity
 → determine s_0

Single diffraction renormalized – (4)

$$\frac{d^2 \sigma}{dt d\Delta y} = N_{gap} \cdot \underbrace{C \cdot F_p^2(t) \cdot \left\{ e^{(\varepsilon + \alpha' t) \Delta y} \right\}^2}_{P_{gap}(\Delta y, t)} \cdot \kappa \cdot \left\{ \sigma_0 e^{\varepsilon \Delta y'} \right\}$$

$$N_{gap}^{-1}(s) = \int_{\Delta y, t} P_{gap}(\Delta y, t) d\Delta y dt \xrightarrow{s \rightarrow \infty} C' \cdot \frac{s^{2\varepsilon}}{\ln s}$$

$$\frac{d^2 \sigma}{dt d\Delta y} = C'' \left[e^{\varepsilon(\Delta y - \ln s)} \cdot \ln s \right] e^{(b_0 + 2\alpha' \Delta y)t}$$

Grows slower than s^ε

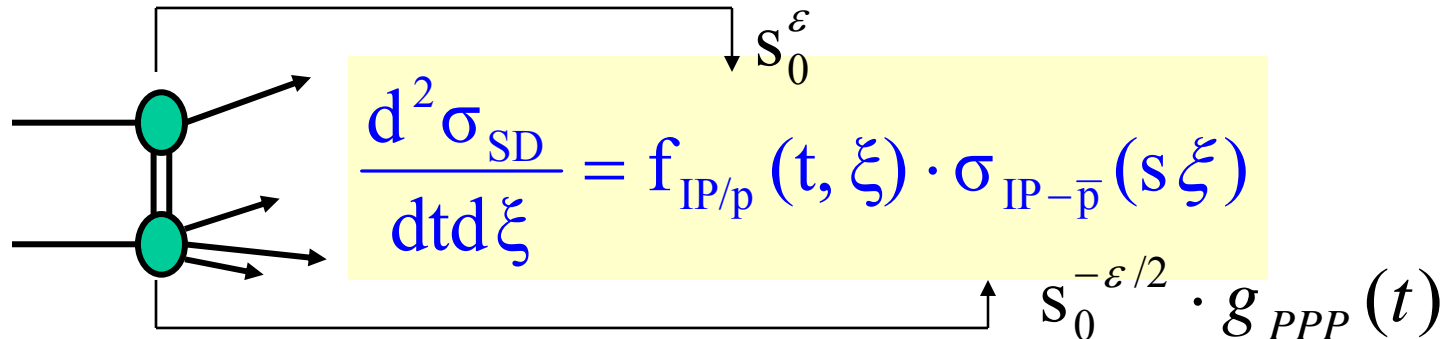
→ Pomplin bound obeyed at all impact parameters

Scale s_0 and triple-pom coupling

Pomeron flux: interpret as gap probability

→ set to unity: determines g_{PPP} and s_0

KG, PLB 358 (1995) 379



Pomeron-proton x-section

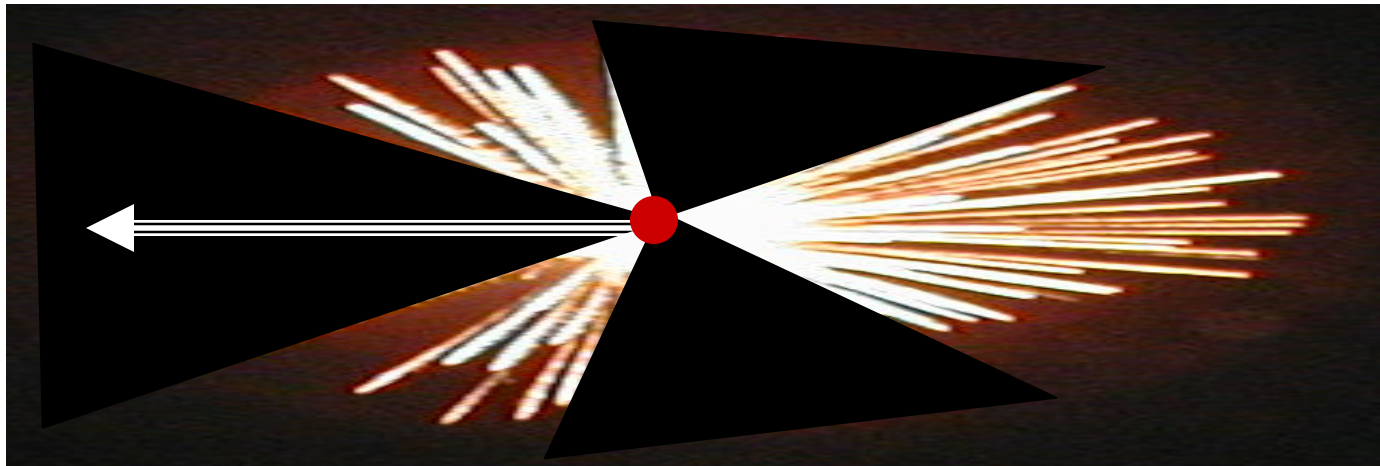
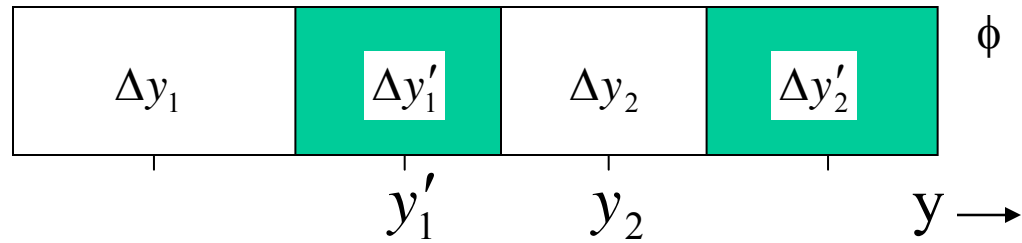
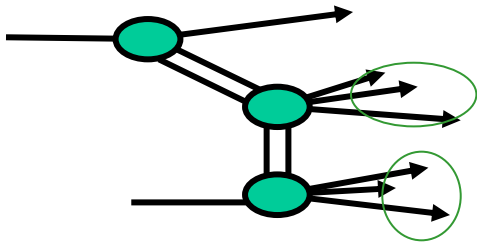
- Two free parameters: s_0 and g_{PPP}
- Obtain product $g_{PPP} \cdot s_0^{\epsilon/2}$ from σ_{SD}
- Renormalized Pomeron flux determines s_0
- Get unique solution for g_{PPP}

$$g_{PPP} = 0.69 \text{ mb}^{-1/2} = 1.1 \text{ GeV}^{-1}$$

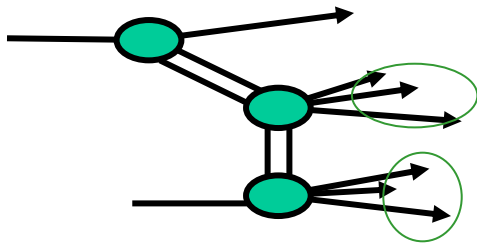
$$S_0 = 3.7 \pm 1.5 \text{ GeV}^2$$

Multigap diffraction

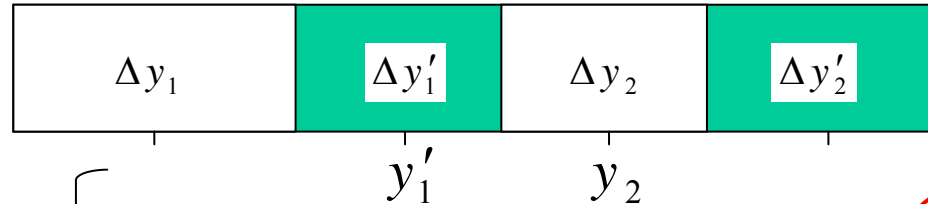
KG, hep-ph/0203141



Multigap cross sections



5 independent variables



$$\left\{ \begin{array}{l} t_1 \\ \Delta y = \Delta y_1 + \Delta y_2 \\ t_2 \end{array} \right.$$

color factor

$$\frac{d^5 \sigma}{\prod_{i=1-5} dV_i} = C \times F_p^2(t_1) \prod_{i=1-2} \left\{ e^{(\varepsilon + \alpha' t_i) \Delta y_i} \right\}^2 \times \kappa^2 \left\{ \sigma_o e^{\varepsilon(\Delta y'_1 + \Delta y'_2)} \right\}$$

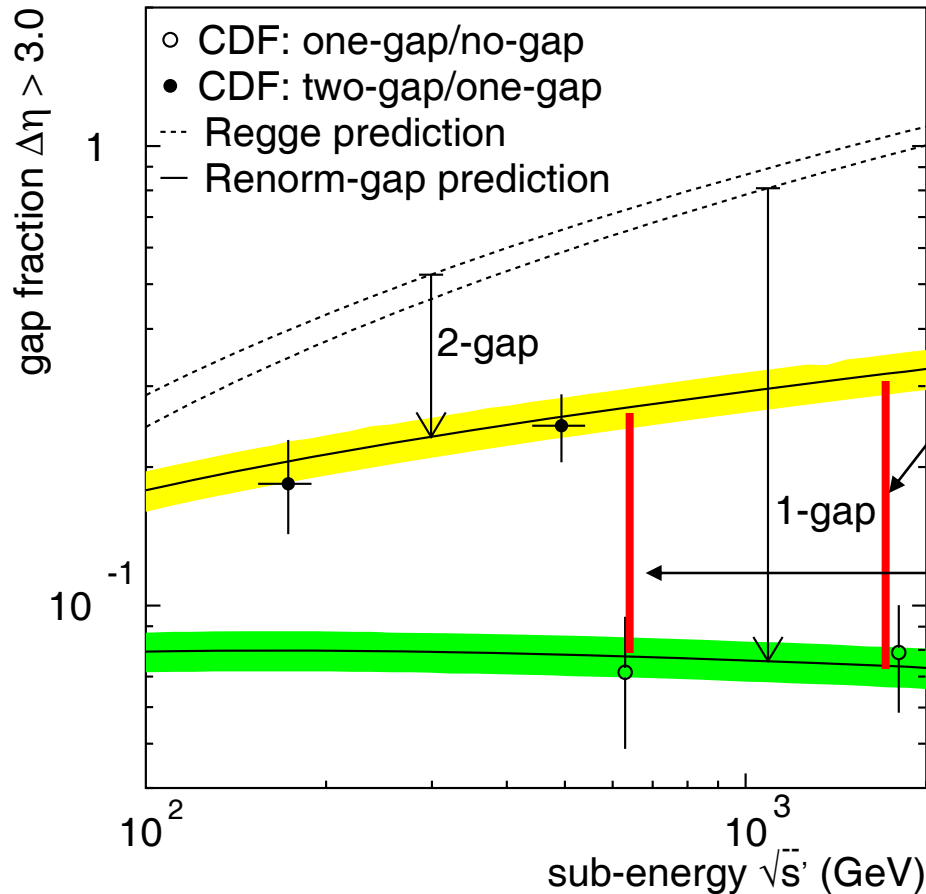
Gap probability

$$\int_{\Delta y, t} \sim s^{2\varepsilon} / \ln s$$

Sub-energy cross section
(for regions with particles)

Same suppression
as for single gap!

Gap survival probability



$$S = \frac{\phi \left[\begin{array}{|c|c|c|} \hline \eta & & \eta \\ \hline \end{array} \right] / \phi \left[\begin{array}{|c|} \hline \eta \\ \hline \end{array} \right]}{\phi \left[\begin{array}{|c|c|c|} \hline \eta & & \eta \\ \hline \end{array} \right] / \phi \left[\begin{array}{|c|c|c|} \hline \eta & & \eta \\ \hline \end{array} \right]}$$

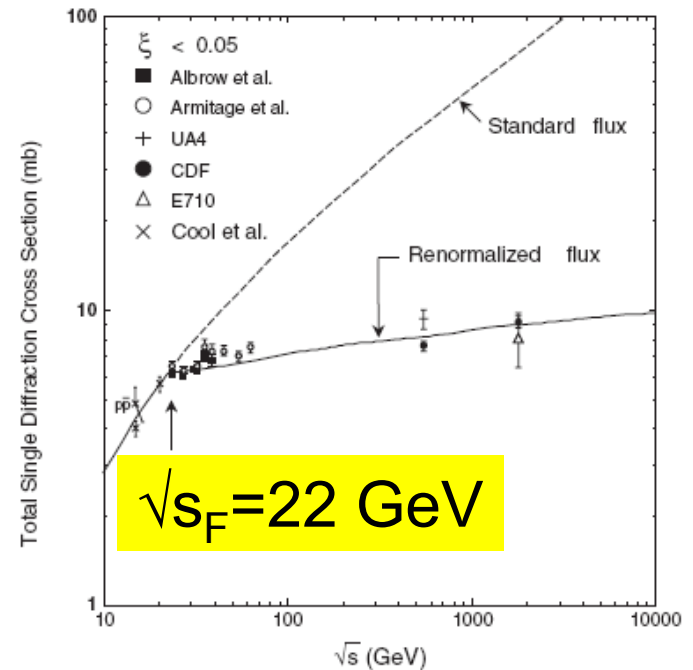
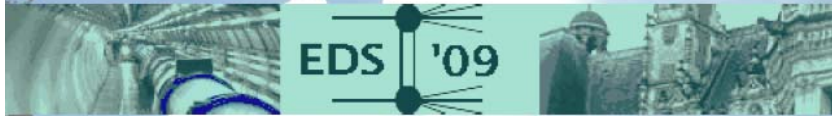
$$S_{2\text{-gap}/1\text{-gap}}^{1\text{-gap}/0\text{-gap}} (1800 \text{ GeV}) \approx 0.23$$

$$S_{2\text{-gap}/1\text{-gap}}^{1\text{-gap}/0\text{-gap}} (630 \text{ GeV}) \approx 0.29$$

Diffractive and Total pp Cross Sections at LHC



Konstantin Goulios
The Rockefeller University



- Use the Froissart formula as a *saturated* cross section

$$\sigma_t(s > s_F) = \sigma_t(s_F) + \frac{\pi}{m^2} \cdot \ln^2 \frac{s}{s_F}$$

- This formula should be valid above the *knee* in σ_{sd} vs. \sqrt{s} at $\sqrt{s_F} = 22$ GeV (Fig. 1) and therefore valid at $\sqrt{s} = 1800$ GeV.
- Use $m^2 = s_o$ in the Froissart formula multiplied by $1/0.389$ to convert it to mb^{-1} .
- Note that contributions from Reggeon exchanges at $\sqrt{s} = 1800$ GeV are negligible, as can be verified from the global fit of Ref. [7].

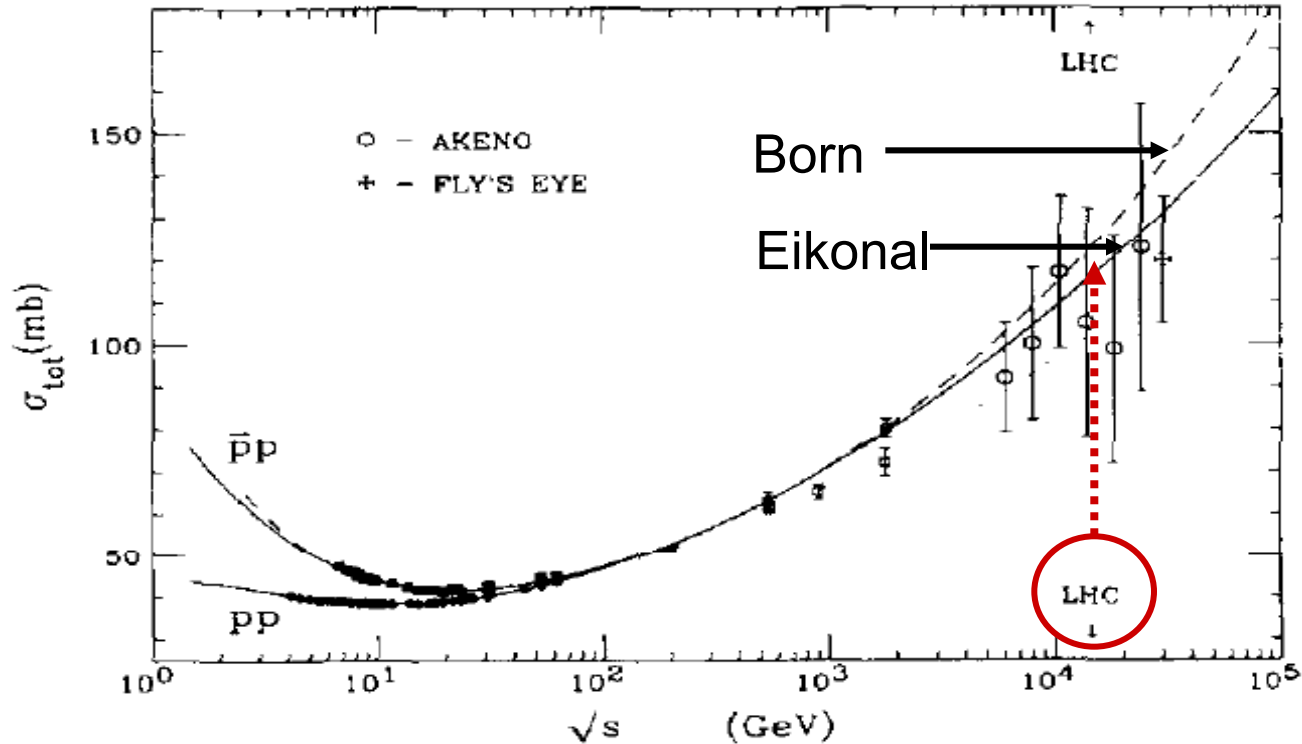
- Obtain the total cross section at the LHC:

$$\sigma_t^{\text{LHC}} = \sigma_t^{\text{CDF}} + \frac{\pi}{s_o} \cdot \left(\ln^2 \frac{s^{\text{LHC}}}{s_F} - \ln^2 \frac{s^{\text{CDF}}}{s_F} \right)$$

SUPERBALL MODEL

98 ± 8 mb at 7 TeV
 109 ± 12 mb at 14 TeV

σ^T at LHC from CMG global fit



✦ σ @ LHC $\sqrt{s}=14$ TeV: 122 ± 5 mb Born, 114 ± 5 mb eikonal
 → error estimated from the error in ε given in CMG-96

Compare with **SUPERBALL** $\sigma(14 \text{ TeV}) = 109 \pm 6$ mb

caveat: $s_0=1 \text{ GeV}^2$ was used in global fit!

σ^{SD} and ratio of α'/ϵ

PHYSICAL REVIEW D **80**, 111901(R) (2009)

Pomeron intercept and slope: A QCD connection

Konstantin Goulianos

$$\frac{d^2 \sigma_{\text{sd}}(s, M^2, t)}{dM^2 dt} = \left[\frac{\sigma_{\circ}}{16\pi} \sigma_{\circ}^{\text{pp}} \right] \frac{s^{2\epsilon}}{N(s)} \frac{1}{(M^2)^{1+\epsilon}} e^{bt}$$

$$\xrightarrow{s \rightarrow \infty} \left[2\alpha' e^{(\epsilon b_0)/\alpha'} \sigma_{\circ}^{\text{pp}} \right] \frac{\ln s^{2\epsilon}}{(M^2)^{1+\epsilon}} e^{bt}$$

$$\sigma_{pp/\bar{p}p}^{\text{tot}} = \sigma_{\circ} \cdot e^{\epsilon \Delta \eta}$$

$$\sigma_{\text{sd}}^{\infty} = 2\sigma_{\circ}^{\text{pp}} \exp\left[\frac{\epsilon b_{\circ}}{2\alpha'}\right] = \sigma_{\circ}^{\text{pp}}$$

$$\sigma_{\circ}^{\text{pp}} = \beta_{\text{pp}}(0) \cdot g(t) = \kappa \sigma_{\circ}^{\text{pp}}$$

$$\kappa = \frac{f_g^{\infty}}{N_c^2 - 1} + \frac{f_q^{\infty}}{N_c}$$

$$b_{\circ} = R_p^2/2 = 1/(2m_{\pi}^2).$$

$$r = \frac{\alpha'}{\epsilon} = -[16m_{\pi}^2 \ln(2\kappa)]^{-1}$$

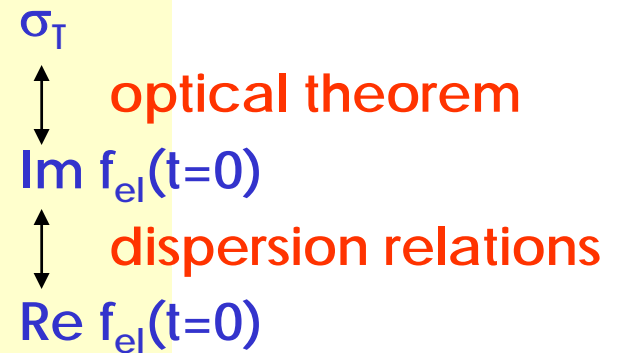
$$r_{\text{pheno}} = 3.2 \pm 0.4 \text{ (GeV}/c)^{-2}$$

$$r_{\text{exp}} = 0.25 \text{ (GeV}/c)^{-2} / 0.08 = 3.13 \text{ (GeV}/c)^{-2}$$

Monte Carlo Strategy for the LHC

MONTE CARLO STRATEGY

- $\sigma^T \rightarrow$ from SUPERBALL model
- optical theorem $\rightarrow \text{Im } f_{el}(t=0)$
- dispersion relations $\rightarrow \text{Re } f_{el}(t=0)$
- differential $\sigma^{SD} \rightarrow$ from RENORM
- use *nested* pp final states for pp collisions at the IP - p sub-energy \sqrt{s}



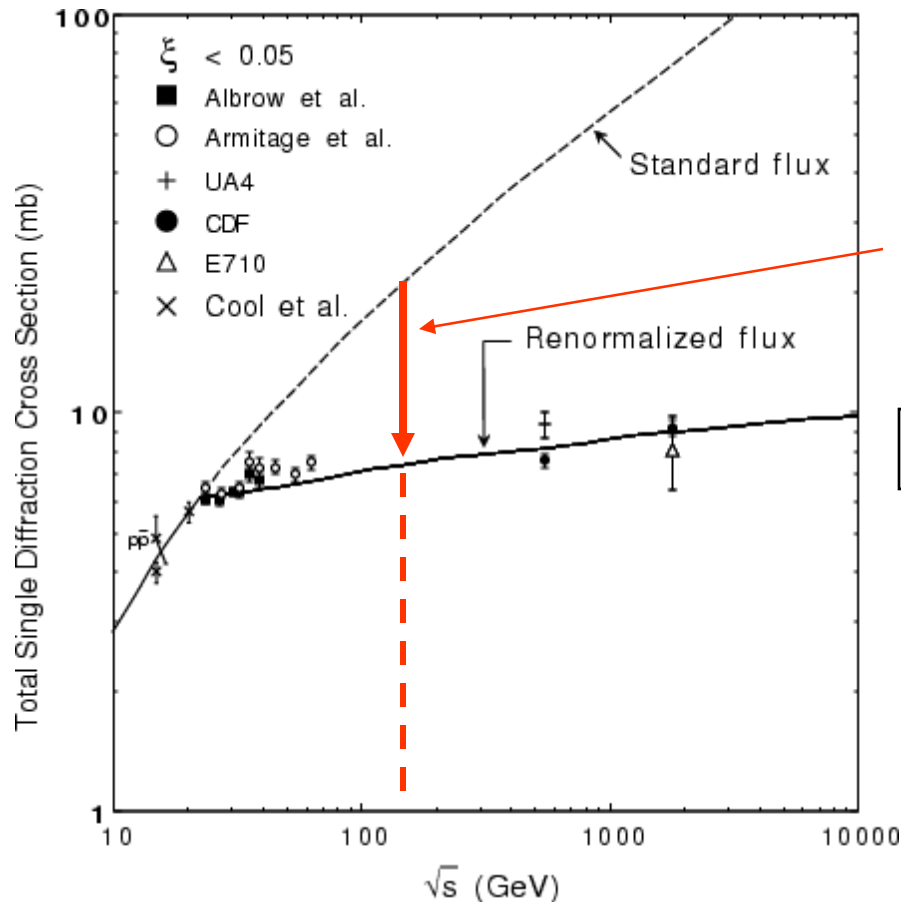
Strategy similar to that employed in the MBR (Minimum Bias Rockefeller) MC used in CDF based on multiplicities from:

K. Goulios, Phys. Lett. B 193 (1987) 151 pp

“A new statistical description of hadronic and e^+e^- multiplicity distributions “

Dijets in γp at HERA from RENORM

K. Goulios, POS (DIFF2006) 055 (p. 8)



Factor of ~ 3 suppression
expected at $W \sim 200$ GeV
(just as in pp collisions)

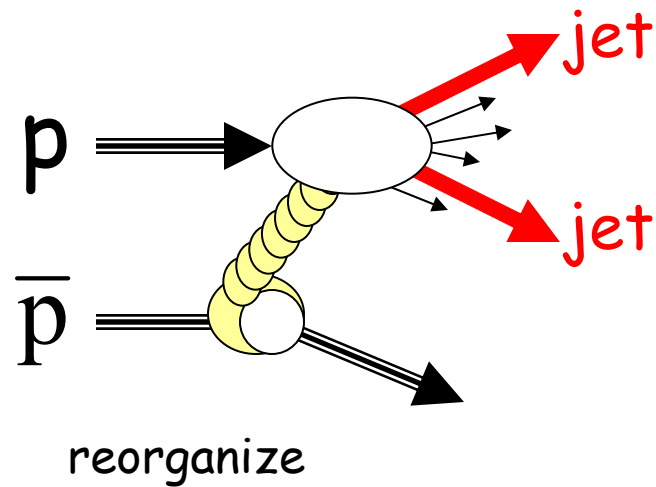
for both direct and resolved components

SUMMARY

- Froissart bound $\sigma \leq (\pi / m^2) \cdot \ln^2 s$
- Valid above the “knee” at $\sqrt{s} = 22$ GeV in σ_T^{SD} vs. \sqrt{s} and therefore valid at $\sqrt{s} = 1.8$ TeV of the CDF measurement
- Use superball scale s_0 (saturated exchange) in the Froissart formula, where $s_0 = 3.7 \pm 1.5$ GeV² as determined from setting the integral of the Pomeron flux to unity at the “knee” of $\sqrt{s} = 22$ GeV
 - $m^2 = s_0 = (3.7 \pm 1.5) \text{ GeV}^2$
- At $\sqrt{s} = 1.8$ TeV Reggeon contributions are negligible (see global fit)
- $\sigma_{14000}^{\text{LHC}} = \sigma_{1800}^{\text{CDF}} + \frac{\pi}{s_0} \cdot \left(\ln^2 \frac{s^{\text{LHC}}}{s_F} - \ln^2 \frac{s^{\text{CDF}}}{s_F} \right) = (80.03 \pm 2.24) + (29 \pm 12) = 109 \pm 12 \text{ mb}$
- compatible with CGM-96 global fit result of $114 \pm 5 \text{ mb}$
- $\sigma_t = (98 \pm 8) \text{ mb}$ at 7 TeV – wait and see!

BACKGROUND

Diffractive dijets @ Tevatron



$$F^D(\xi, x, Q^2) \propto \frac{1}{\xi^{1+2\varepsilon}} \cdot F(x/\xi, Q^2)$$

$F^D_{JJ}(\xi, \beta, Q^2)$ @ Tevatron

$$F^D(\xi, \beta, Q^2) = N_{\text{renorm}} \frac{1}{\xi^{1+2\varepsilon}} \cdot \frac{C(Q^2)}{(x/\xi)^{\lambda(Q^2)}} = \frac{2\varepsilon}{(\beta s)^{2\varepsilon}} \cdot \frac{1}{\xi^{1+2\varepsilon}} \cdot \frac{C(Q^2)}{\beta^{\lambda(Q^2)}}$$

$$N_{\text{renorm}}^{-1} = \int_{\xi_{\min}}^1 \frac{d\xi}{\xi^{1+2\varepsilon}} \xrightarrow{\xi_{\min} = \frac{x_{\min}}{\beta} \approx \frac{1}{\beta s}} \frac{(\beta s)^{2\varepsilon}}{2\varepsilon}$$

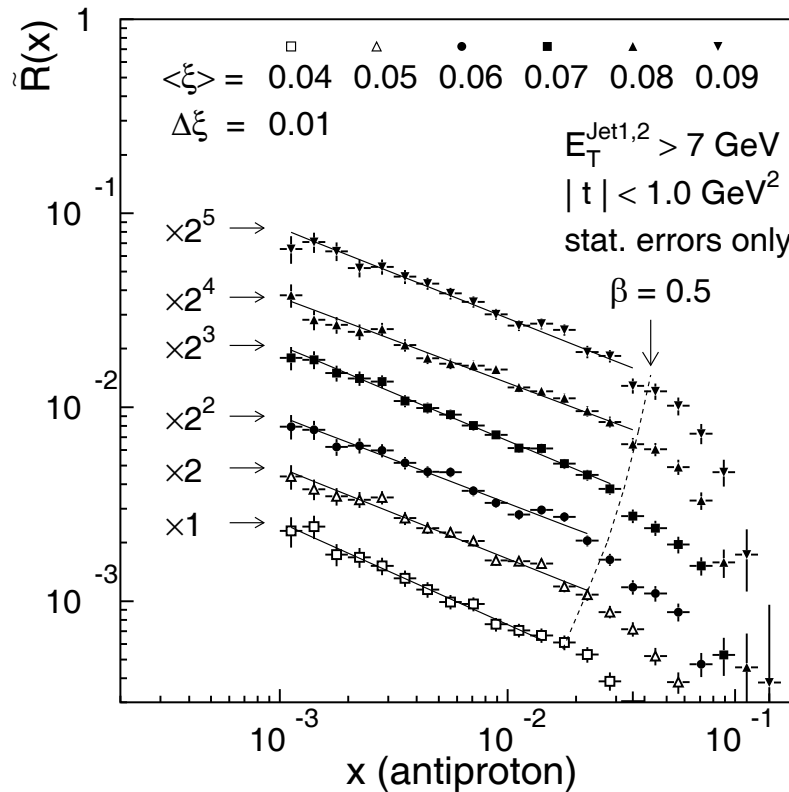
$$\text{RENORM} \Rightarrow R_{ND}^{SD}(x) = \frac{2\varepsilon}{s^{2\varepsilon}} \frac{1}{\xi^{1-\lambda(Q^2)}} \cdot x^{-(2\varepsilon)}$$

$$\varepsilon_g = 0.2 \rightarrow x^{-0.4}$$

SD/ND dijet ratio vs. x_{Bj} @ CDF

CDF Run I

$$R(x) = \frac{F_{jj}^{SD}(x)}{F_{jj}^{ND}(x)}$$



$$0.035 < \xi < 0.095$$

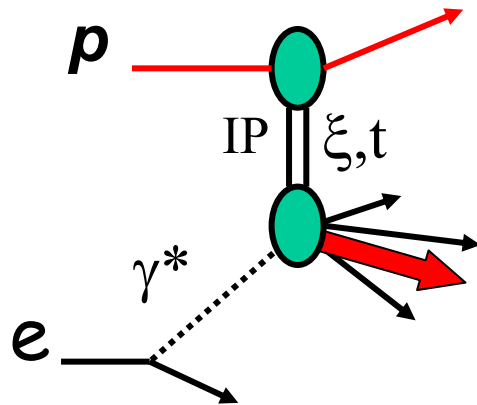
Flat ξ dependence
for $\beta < 0.5$

$$R(x) = x^{-0.45}$$

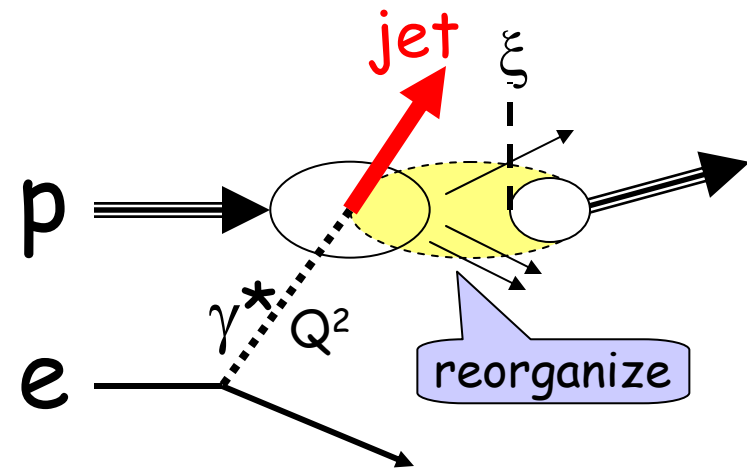
Diffractive DIS @ HERA

J. Collins: factorization holds (but under what conditions?)

Pomeron exchange



Color reorganization

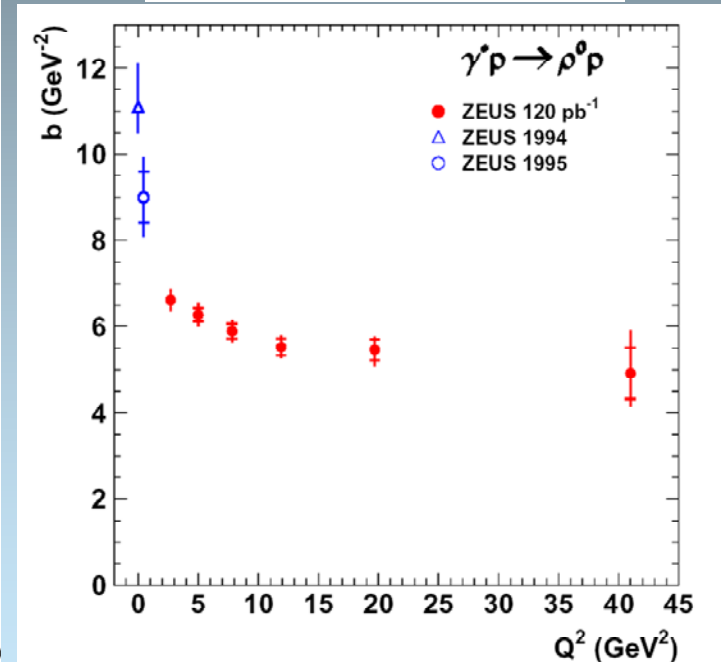
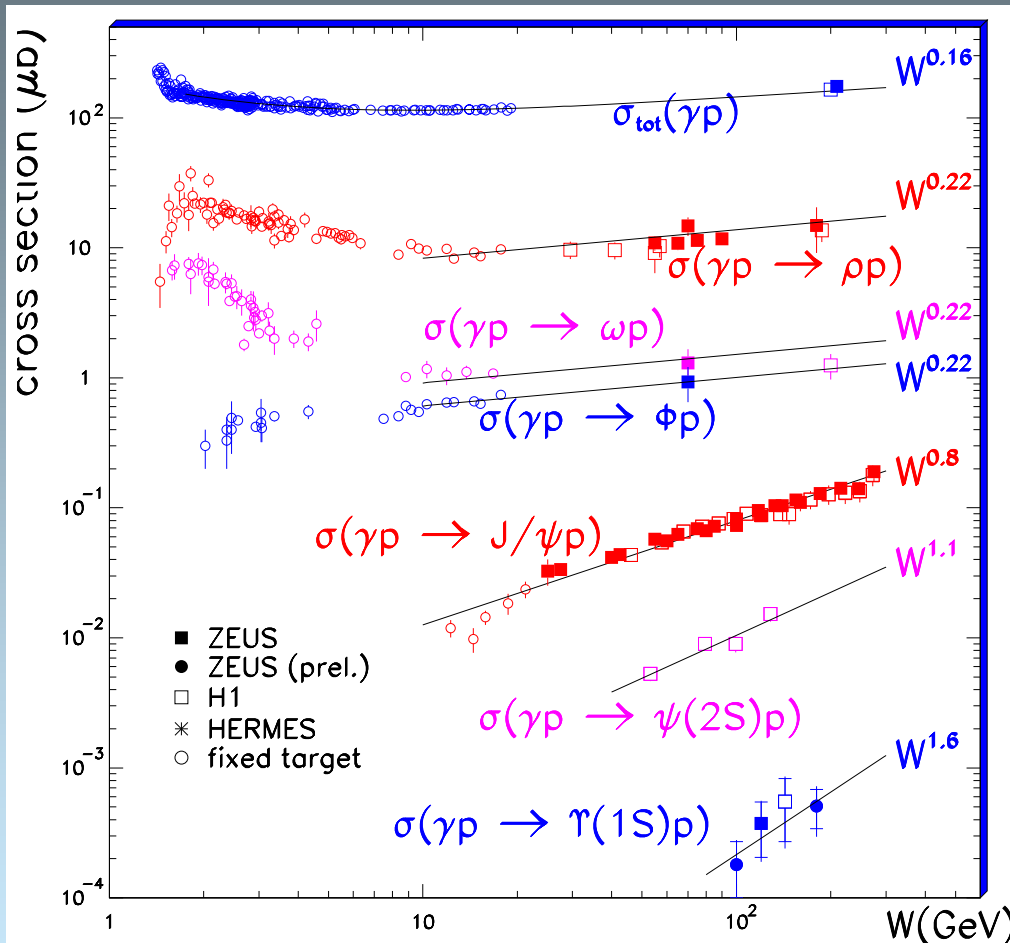
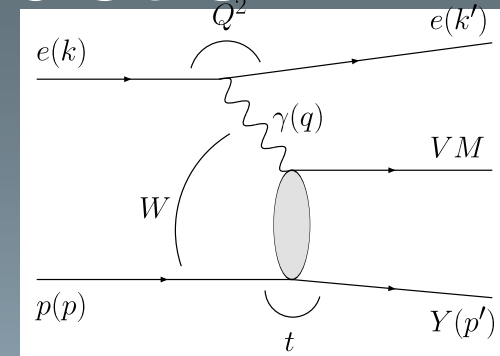


$$F_2^{D(3)}(\xi, x, Q^2) \propto \frac{1}{\xi^{1+\epsilon}} \cdot F_2(x, Q^2)$$

Results favor color reorganization

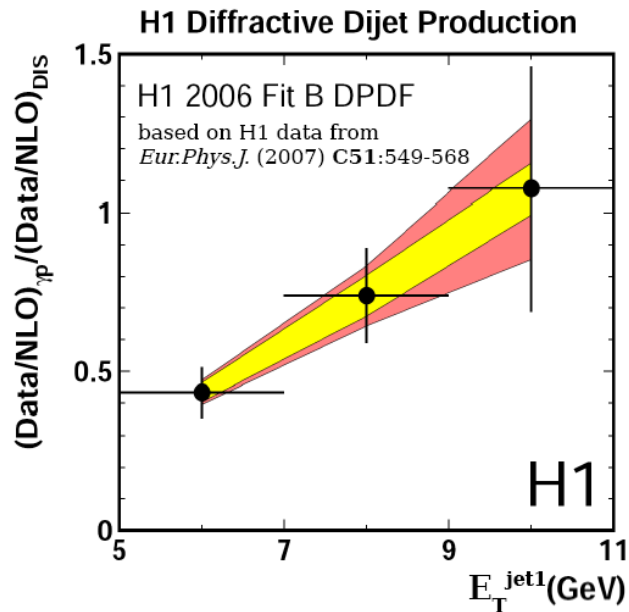
Vector meson production

(Pierre Marage, HERA-LHC 2008)



- *left* - why different σ vs. W slopes? \rightarrow more room for particles
- *right* - why smaller b -slope in γ^*p ? \rightarrow same reason

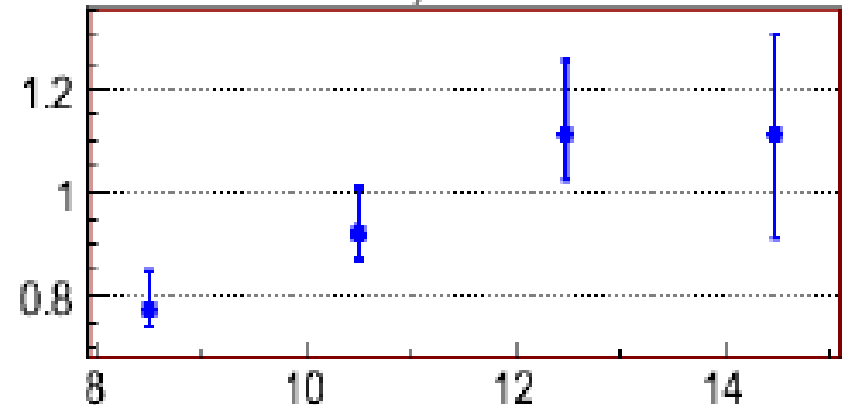
Dijets in γp at HERA - 2008



ZEUS
data
NLO

DIS 2008 talk by W. Slomiński,

H1-2006-B, GRV

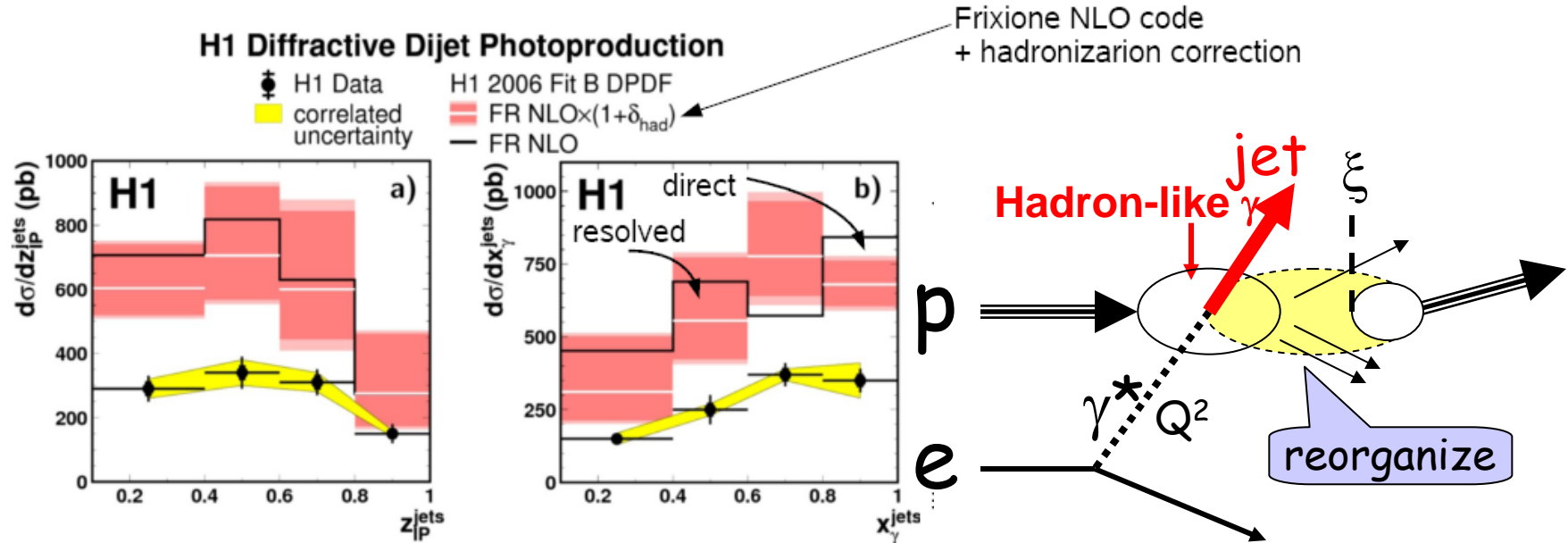


□ 20-50 % apparent rise when E_T^{jet} 5 \rightarrow 10 GeV
 \rightarrow due to suppression at low E_T^{jet} !!!

Dijets in γp at HERA – 2007

Dijets in γp

Direct vs. resolved



□ the reorganization diagram predicts:

- suppression at low $Z_{\text{IP}}^{\text{jets}}$, since larger $\Delta\eta$ is available for particles
- same suppression for direct and resolved processes

The end