

Diffraction x-sections and event final states at the LHC

Expanded talk presenter at DIFFRACTION DAY 7 May 2010 CERN



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CDF → PHENO → CMS
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**Forward physics @ LHC workshop
27-29 May 2010 Elba**

OUTLINE

Describe a phenomenology based on pre-LHC results and use it to:

- make predictions for LHC
- suggest measurements to confirm / modify parameters
- suggest scheme to be implemented in MC simulations
- propose method to measure luminosity

Current MC generators: unreliable for extrapolations to LHC

- MC tuning → based on multi-parameter tuning of ill-defined event topologies
- Solution: use nested x-sections

Contents

- ❑ define diffractive x-section event topologies
→ nested diffractive gaps
- ❑ describe in terms of proton pdf's and QCD color factors
- ❑ normalize to guarantee unitarity → renormalization model

REMARKS

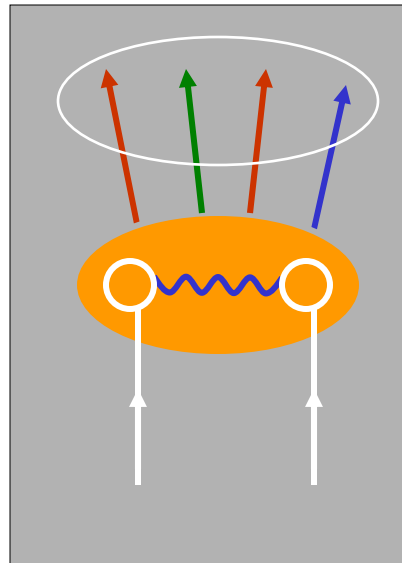
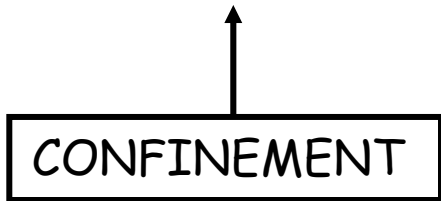
- ❑ MC generators inadequate:
 - e.g. PYTHIA and PHOJET predictions of diffractive processes disagree with each other and with data.
- ❑ Diffractive factorization at HERA? Breakdown observed in, e.g.
 - Vector mesons: σ vs. W , b-slopes of t-distributions
 - Dijets: E_T^{jet} dependence, resolved vs. direct components, ...
- ❑ RENORM model: describes both $p(\text{pbar})-p$ and $\gamma(\gamma^*)-p$
- ❑ Luminosity measurement: requires a known x-section
 - suggest SD – well defined and slowly varying

p-p Interactions

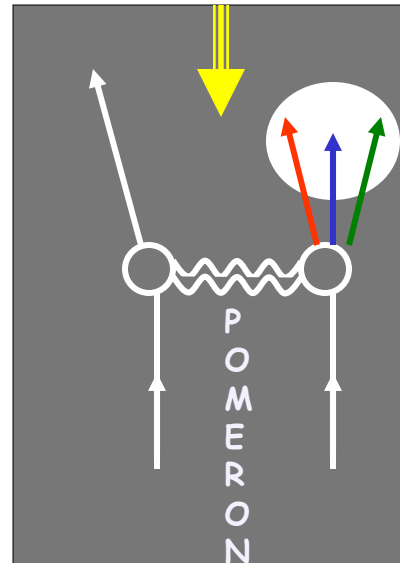
Non-diffractive:
Color-exchange

Diffractive:
Colorless exchange carrying
vacuum quantum numbers

Incident hadrons
acquire color
and break apart



rapidity gap

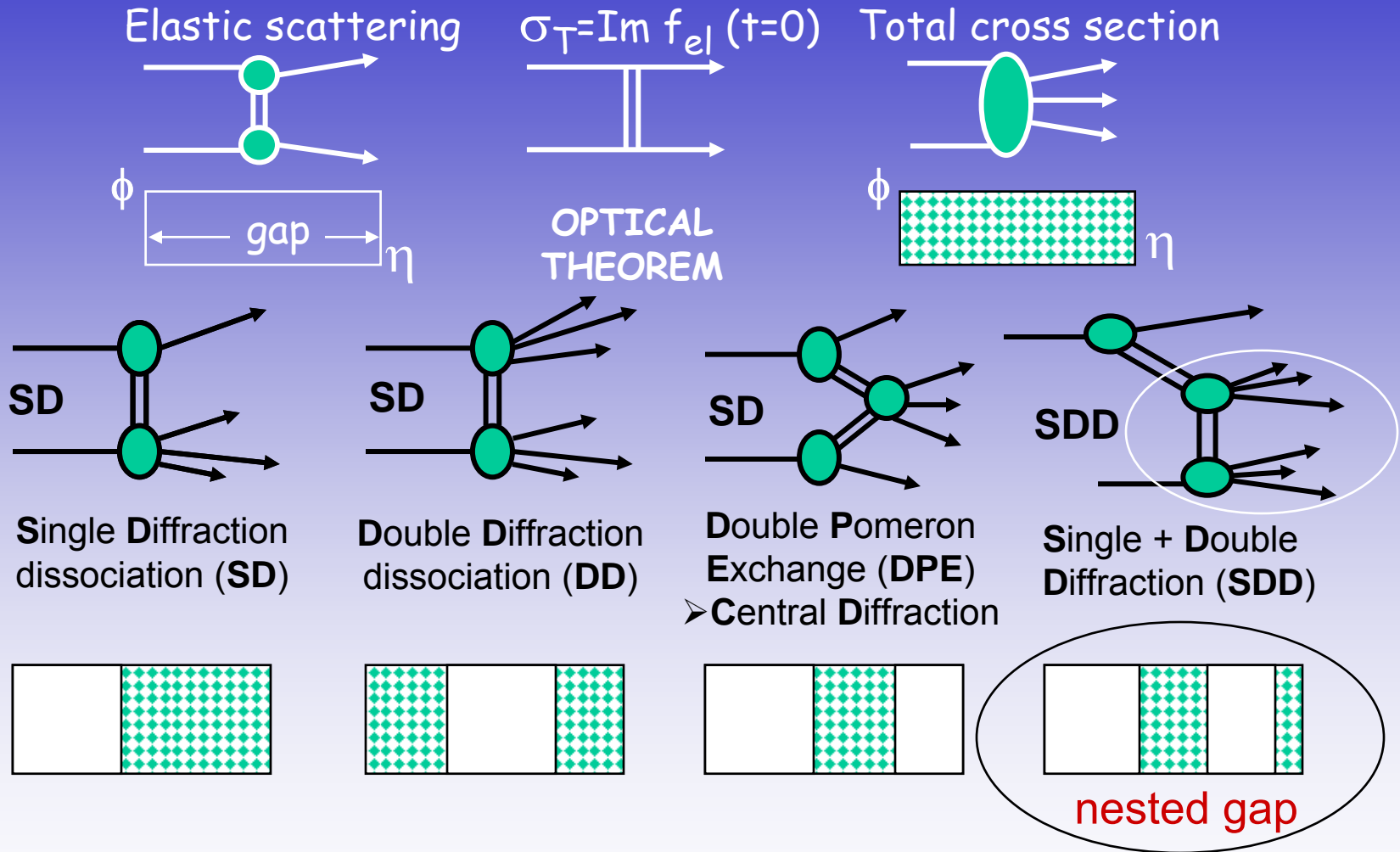


Incident hadrons retain
their quantum numbers
remaining colorless



Goal: understand the QCD nature of the diffractive exchange

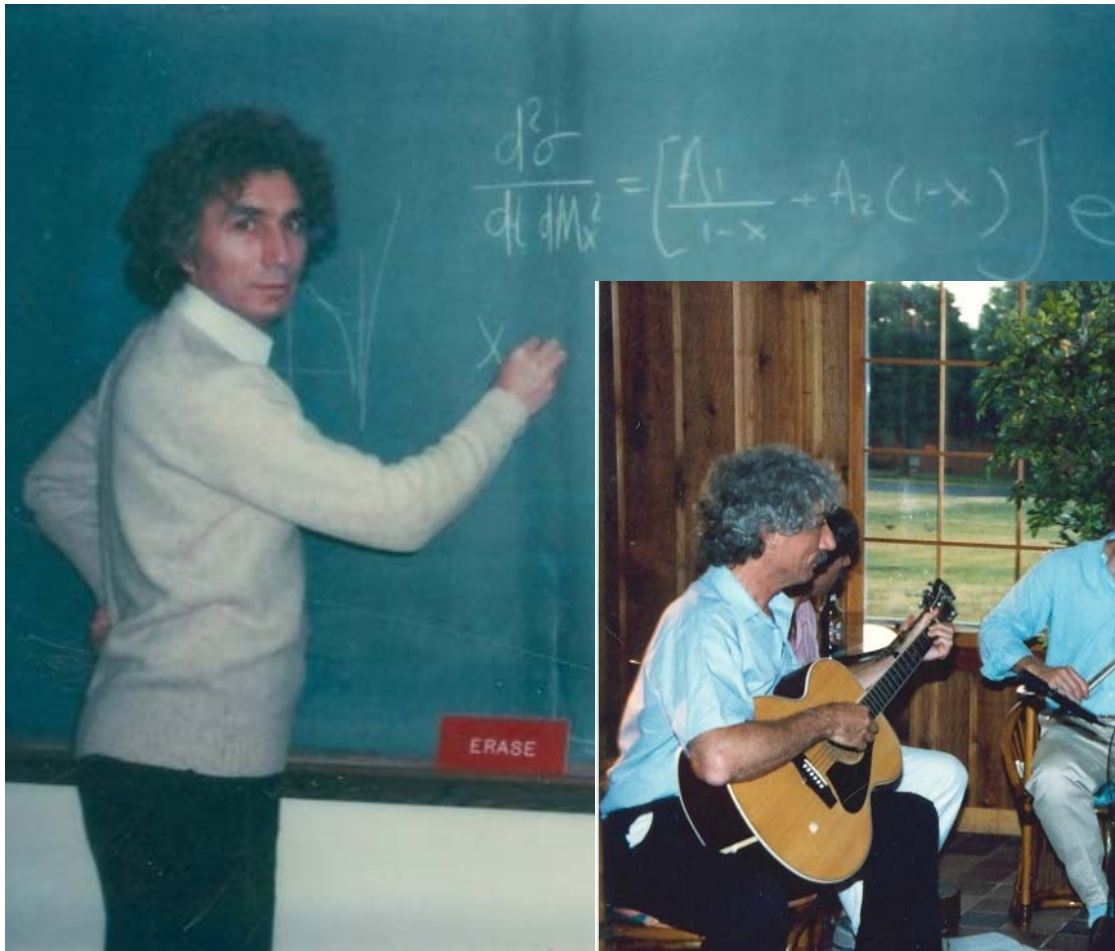
Diffractive pp($\bar{p}p$) processes @ CDF



Use nesting until no diffractive gap fits in \sqrt{s} '

A bit of history...

Diffraction in the 70s → the Pomeron unveiled!

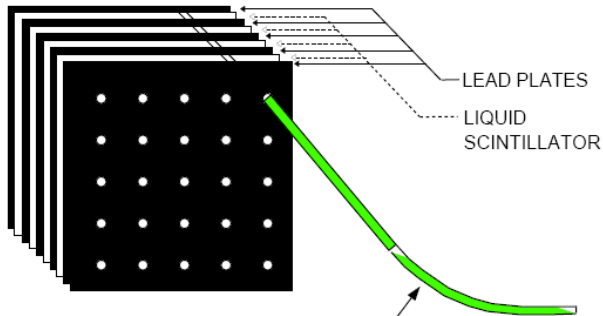


Opening night at Chez Leon
- Fermilab (1989)



(right) → Greg Snow on violin (Ph.D thesis: first observation of diffractive γ dissociation)

More history Elba 2000



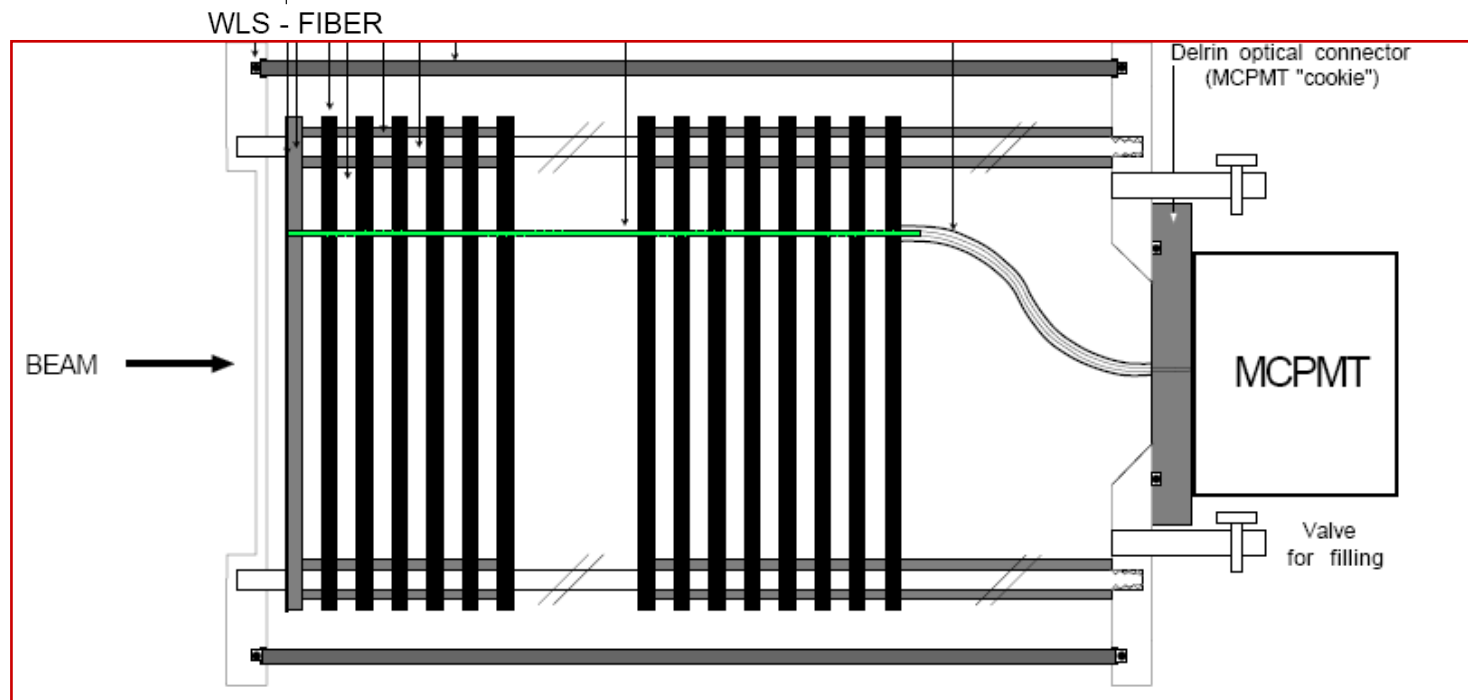
The CDF MiniPlugs

Proposed Forward Calorimeters for CDF-II

K. Goulios^a, S. Lami^a

^a*The Rockefeller University, New York, NY 10021, USA*

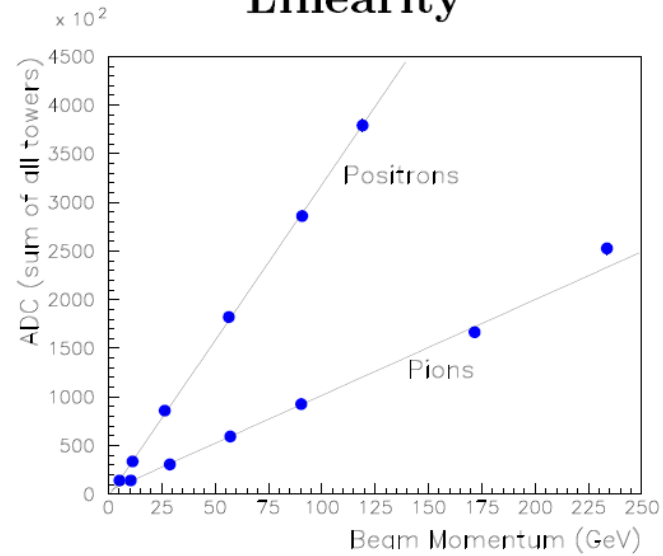
Presented by: K. Goulios



Elba 2000

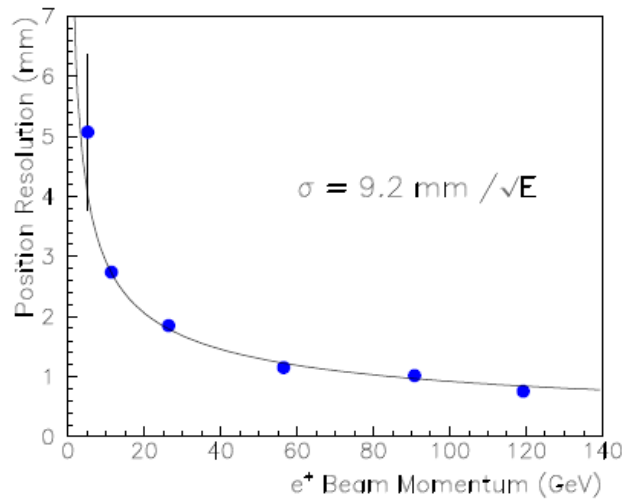
The CDF MiniPlugs

Linearity

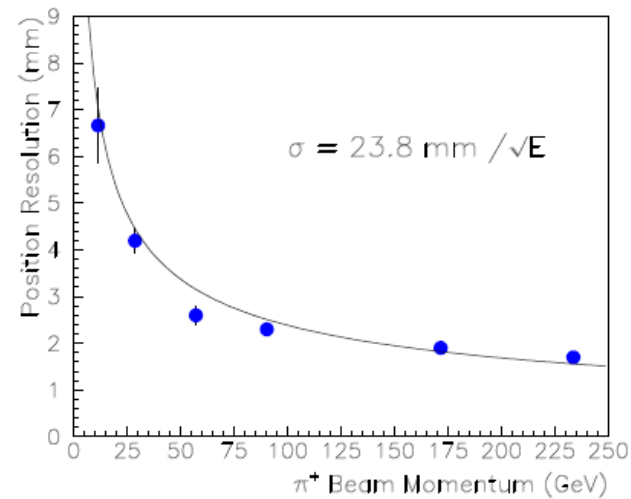


Position Resolution

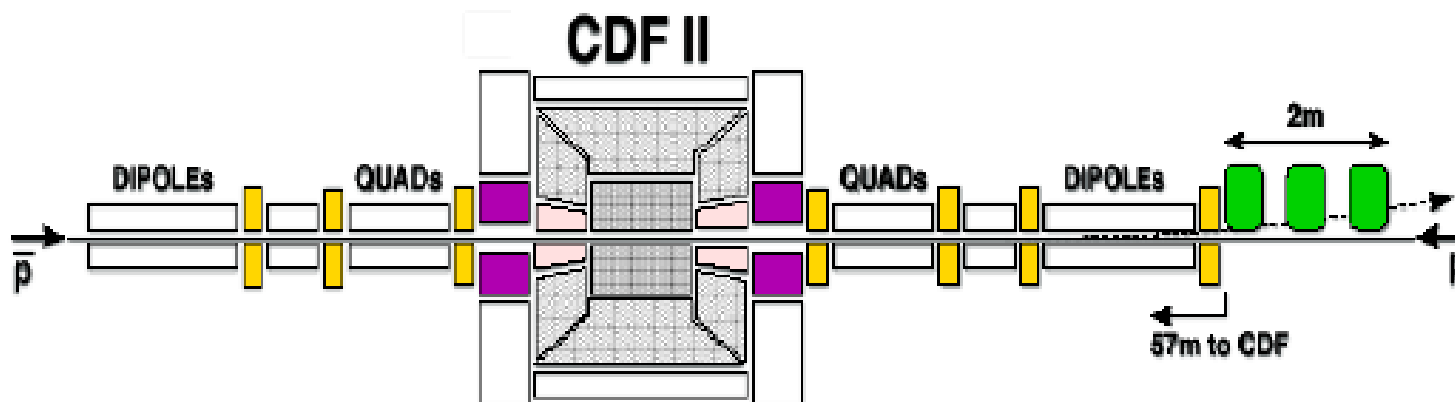
Electrons



Pions



The CDF II Detector

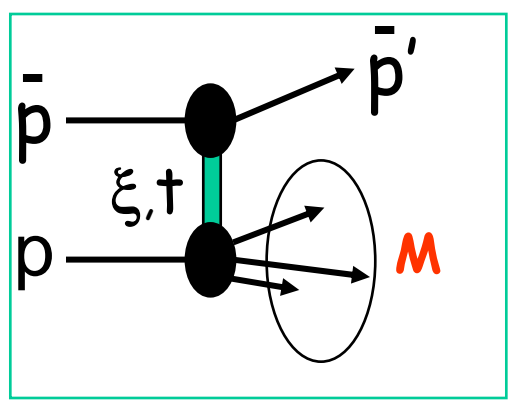


TRACKING SYSTEM
 CCAL
 PCAL
 MPCAL
 CLC
 BSC
 RPS

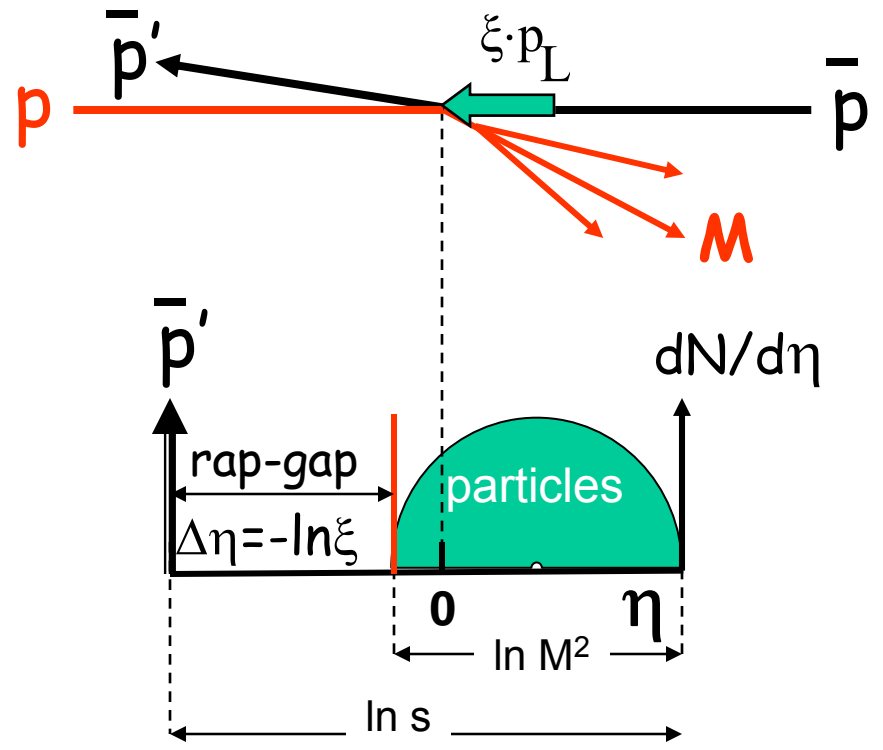
- | | | |
|-----------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------|---------------------------------------------------|
| Tracking | – Tracking Detectors | $ \eta < 2.0$ |
| CCAL, PCAL | – Calorimeters | $ \eta < 3.6$ |
| RPS | – Roman Pot Spectrometers | $0.02 < \xi < 0.1$ $0 < t < 2 \text{ GeV}^2$ |
| BSC | – Beam Shower Counters | $5.4 < \eta < 7.4$ |
| MPCAL | – MiniPlug Calorimeters | $3.5 < \eta < 5.1$ |



Definitions



$$1 - x_L \equiv \xi = \frac{M^2}{s}$$



M² scaling: no price paid for increasing diffractive gap size

$$\left(\frac{d\sigma}{d\Delta\eta} \right)_{t=0} \approx \text{constant} \Rightarrow \frac{d\sigma}{d\xi} \propto \frac{1}{\xi} \Rightarrow \frac{d\sigma}{dM^2} \propto \frac{1}{M^2}$$

M² scaling

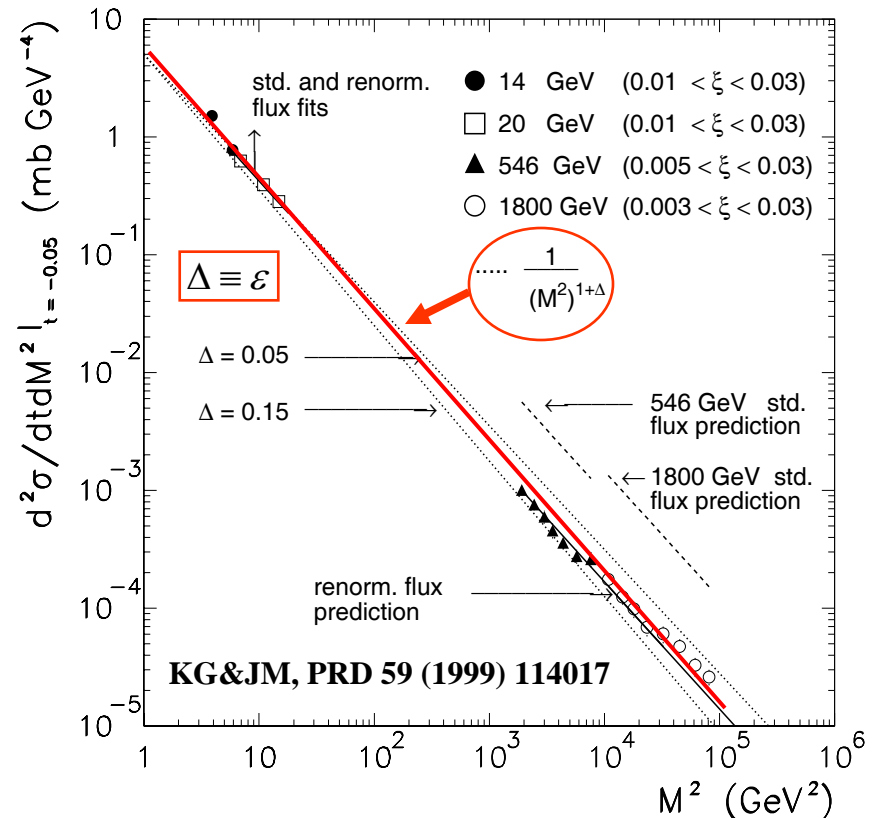
→ $d\sigma/dM^2|_{t=-0.05}$ independent of s over 6 orders of magnitude!

Regge

data

$$\frac{d\sigma}{dM^2} \propto \frac{s^{2\varepsilon} \rightarrow 1}{(M^2)^{1+\varepsilon}}$$

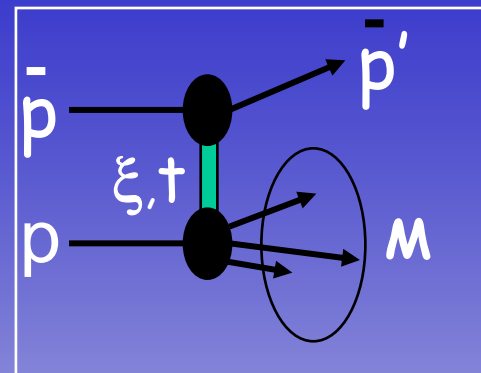
→ Independent of s over 6 orders of magnitude in M^2 !



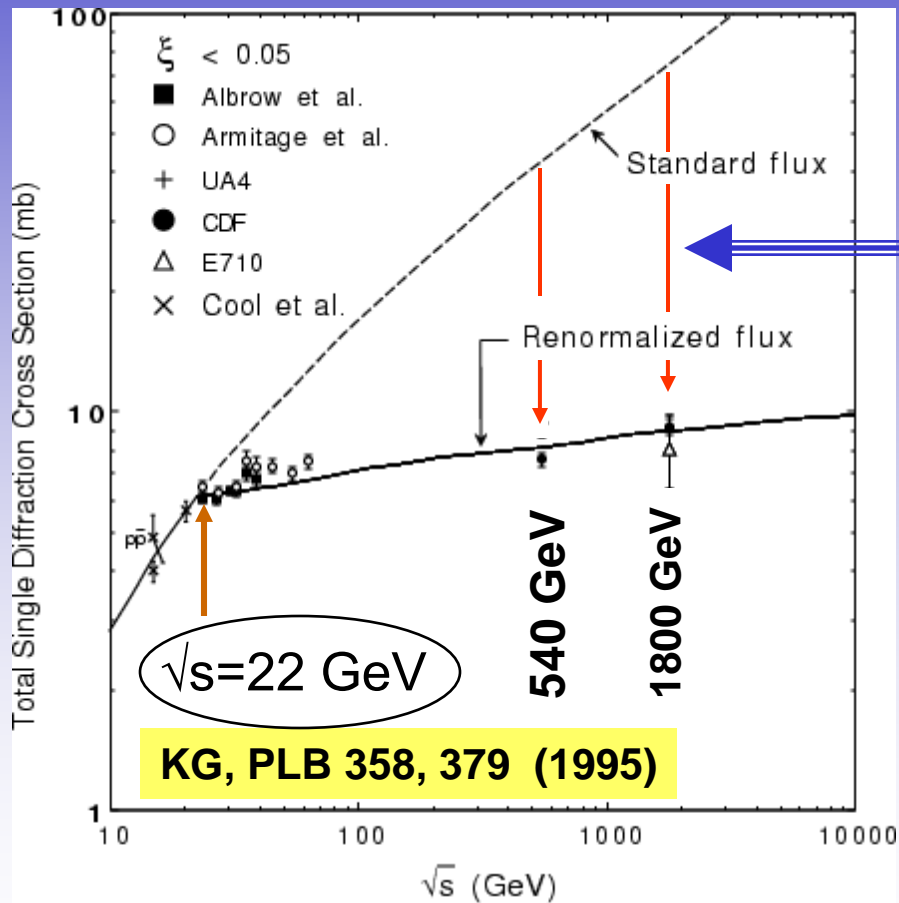
→ factorization breaks down to ensure M^2 scaling - why?

σ_{SD}^T (pp & $\bar{p}p$)

→ suppressed relative to Regge

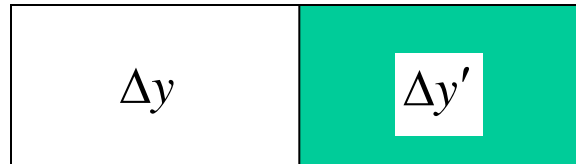
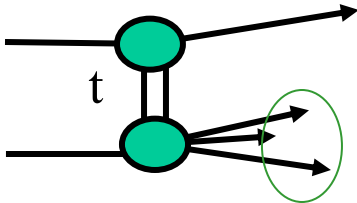


σ_{SD}^T mb



Factor of ~8 (~5)
suppression at
 $\sqrt{s} = 1800$ (540) GeV

Single Diffraction



2 independent variables: $t, \Delta y$

color factor

$$\kappa = \frac{g_{IP-IP-IP}(t)}{\beta_{IP-p-p}(0)} \approx 0.17$$

$$\frac{d^2 \sigma}{dt d\Delta y} = \underbrace{C \cdot F_p^2(t) \cdot \left\{ e^{(\varepsilon + \alpha' t) \Delta y} \right\}^2}_{\text{gap probability}} \cdot \underbrace{\kappa \cdot \left\{ \sigma_o e^{\varepsilon \Delta y'} \right\}}_{\text{sub-energy x-section}}$$

Gap probability MUST be normalized to unity!

Single diffraction (re)normalized

$$\frac{d^2 \sigma}{dt d\Delta y} = N_{gap} \cdot \underbrace{C \cdot F_p^2(t) \cdot \left\{ e^{(\varepsilon + \alpha' t) \Delta y} \right\}^2}_{P_{gap}(\Delta y, t)} \cdot \kappa \cdot \left\{ \sigma_0 e^{\varepsilon \Delta y'} \right\}$$

$$N_{gap}^{-1}(s) = \int_{\Delta y, t} P_{gap}(\Delta y, t) d\Delta y dt \xrightarrow{s \rightarrow \infty} C' \cdot \frac{s^{2\varepsilon}}{\ln s}$$

$$\frac{d^2 \sigma}{dt d\Delta y} = C'' \left[e^{\varepsilon(\Delta y - \ln s)} \cdot \ln s \right] e^{(b_0 + 2\alpha' \Delta y)t}$$

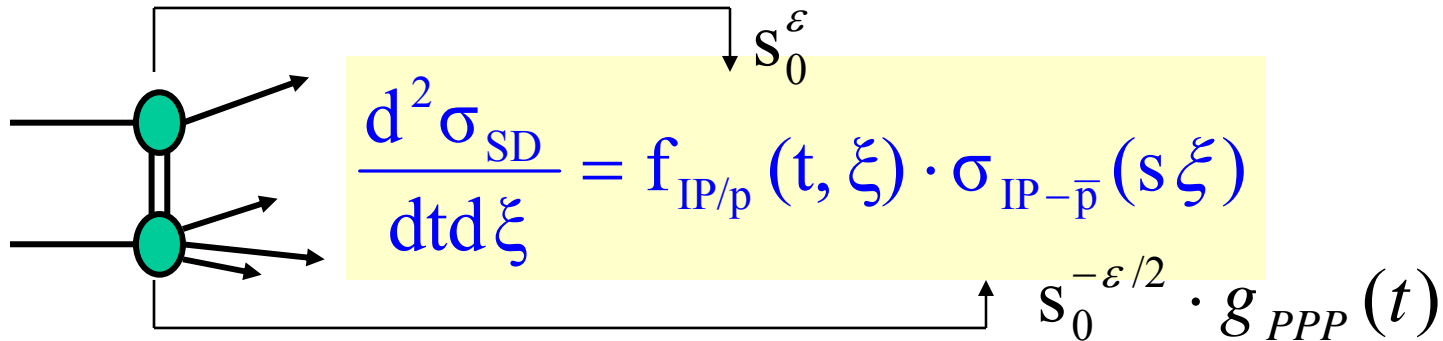
Grows slower than s^ε

→ Pomplun bound obeyed at all impact parameters

Unitarity and Renormalization

Pomeron flux \rightarrow gap probability

Set to unity – determines g_{PPP} and s_0 *KG, PLB 358 (1995) 379*



The diagram shows two incoming lines on the left that split into two outgoing lines on the right. A central yellow box contains the equation:

$$\frac{d^2 \sigma_{SD}}{dt d\xi} = f_{IP/p}(t, \xi) \cdot \sigma_{IP-\bar{p}}(s\xi)$$

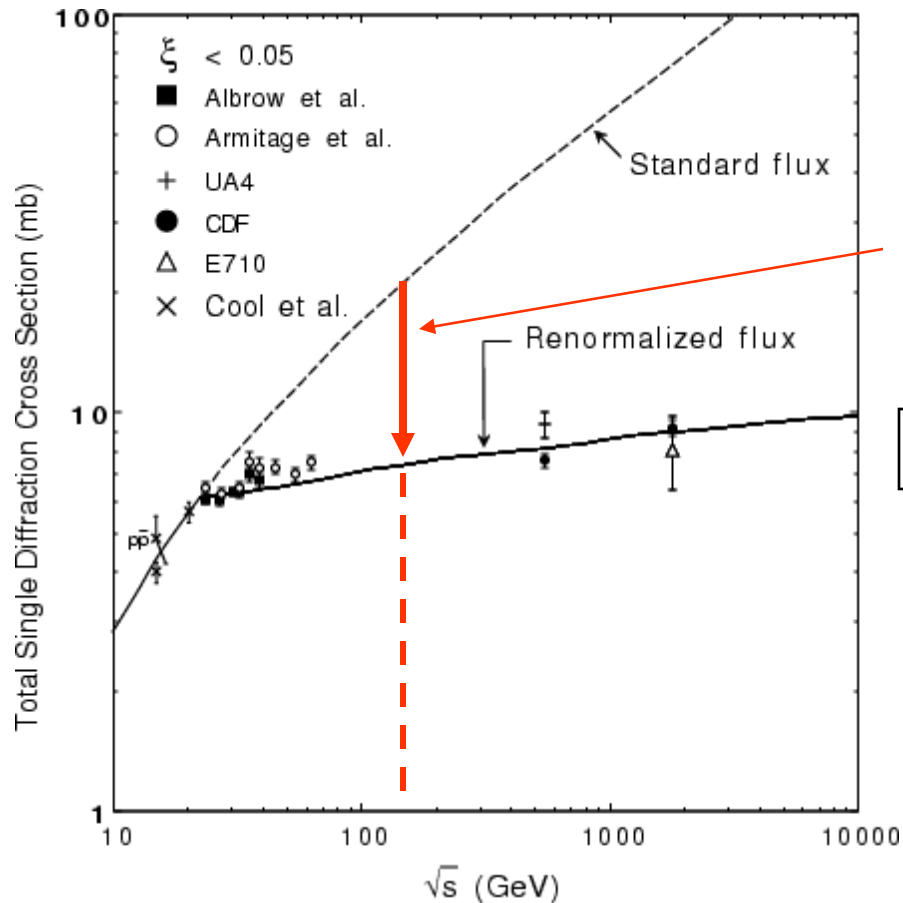
Arrows indicate that s_0^ϵ is multiplied to the right side of the equation, and $s_0^{-\epsilon/2} \cdot g_{PPP}(t)$ is multiplied to the left side.

Pomeron-proton x-section

- Two free parameters: s_0 and g_{PPP}
- Obtain product $g_{PPP} \cdot s_0^{\epsilon/2}$ from σ_{SD}
- Renormalized Pomeron flux determines s_0
- Get unique solution for g_{PPP}

Dijets in γp at HERA from RENORM

K. Goulios, POS (DIFF2006) 055 (p. 8)

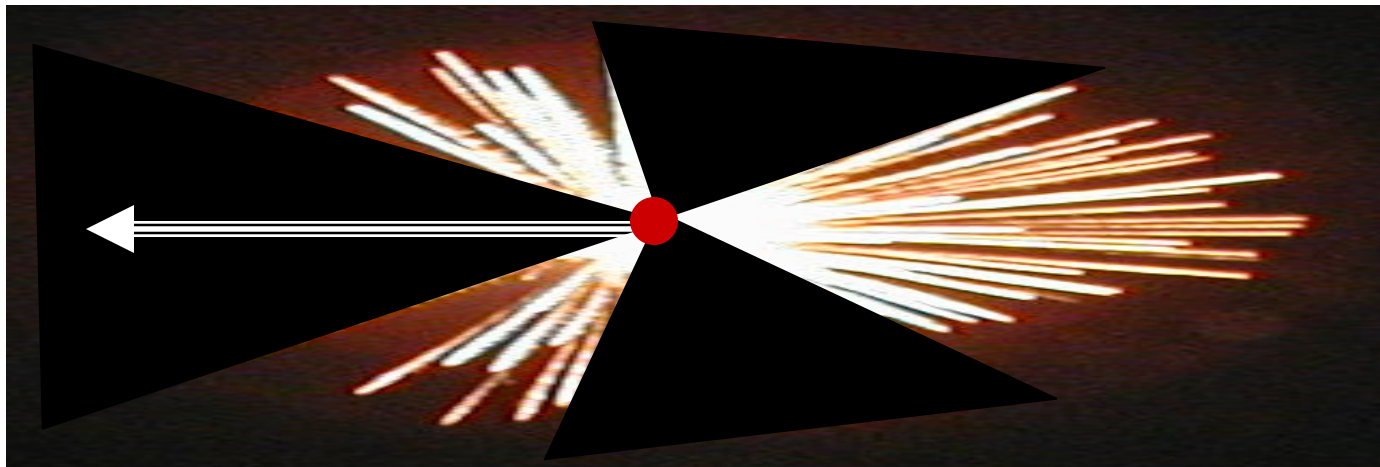
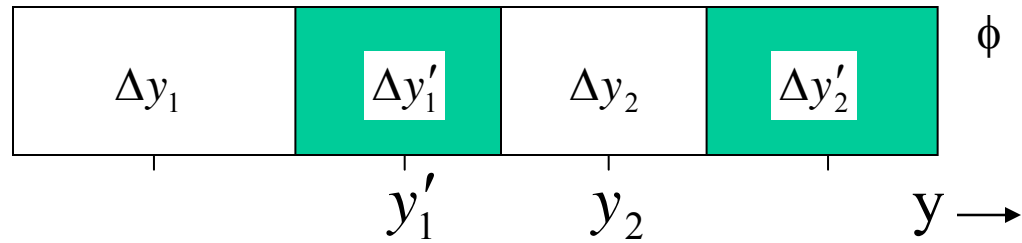
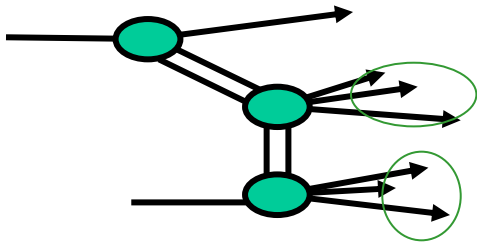


Factor of ~ 3 suppression
expected at $W \sim 200$ GeV
(just as in pp collisions)

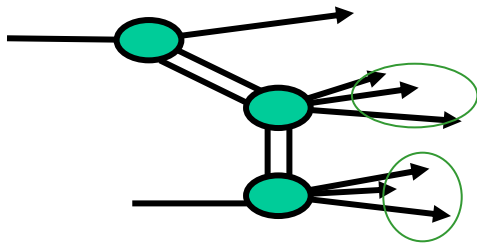
for both direct and resolved components

Multi-gap Diffraction

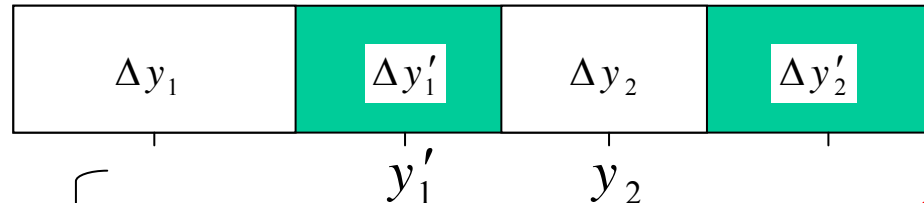
(KG, hep-ph/0205141)



Multi-gap Cross Sections



5 independent variables



$$\left\{ \begin{array}{l} t_1 \\ t_2 \end{array} \right. \Delta y = \Delta y_1 + \Delta y_2$$

color factor

$$\prod_{i=1-5} \frac{d^5 \sigma}{dV_i} = C \times F_p^2(t_1) \prod_{i=1-2} \left\{ e^{(\varepsilon + \alpha' t_i) \Delta y_i} \right\}^2 \times \kappa^2 \left\{ \sigma_o e^{\varepsilon(\Delta y'_1 + \Delta y'_2)} \right\}$$

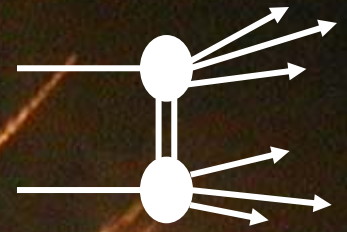
Gap probability

$$\int_{\Delta y, t} \sim s^{2\varepsilon} / \ln s$$

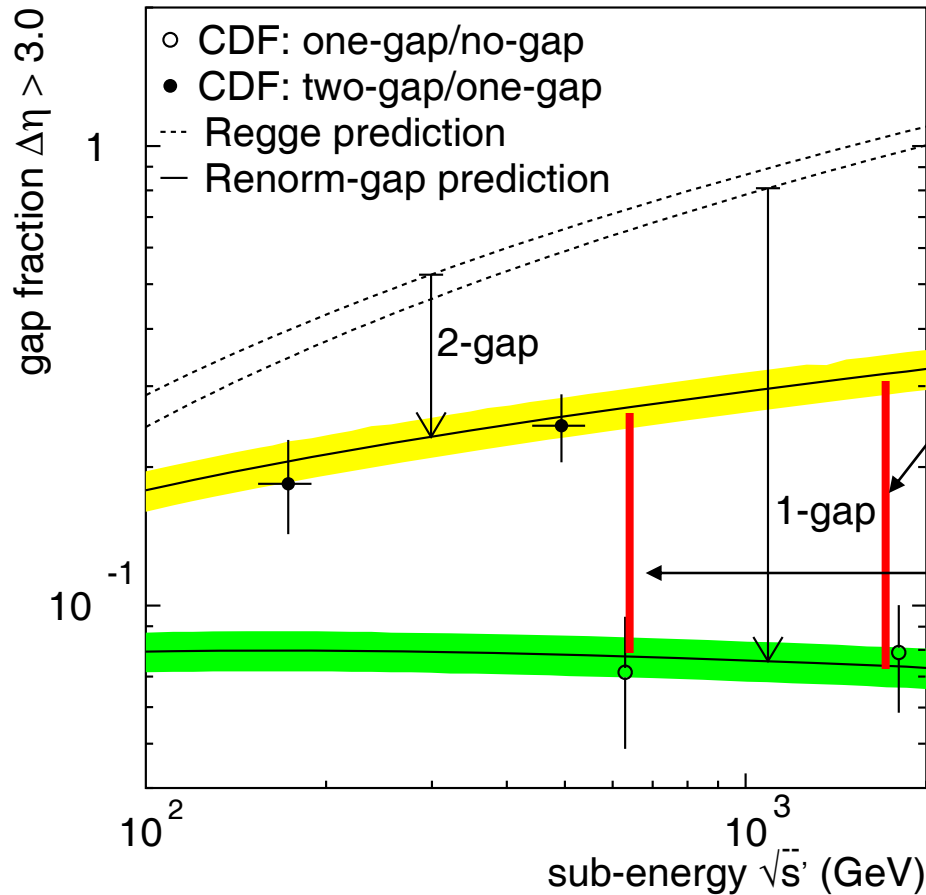
Same suppression
as for single gap!

Sub-energy cross section
(for regions with particles)

Rapidity Gaps in Fireworks



“Gap survival probability”



$$S = \frac{\phi \left[\begin{array}{|c|} \hline \eta \\ \hline \end{array} \right] / \phi \left[\begin{array}{|c|} \hline \eta \\ \hline \end{array} \right]}{\phi \left[\begin{array}{|c|} \hline \eta \\ \hline \end{array} \right] / \phi \left[\begin{array}{|c|} \hline \eta \\ \hline \end{array} \right]}$$

$$S_{2\text{-gap}/1\text{-gap}}^{1\text{-gap}/0\text{-gap}} (1800 \text{ GeV}) \approx 0.23$$

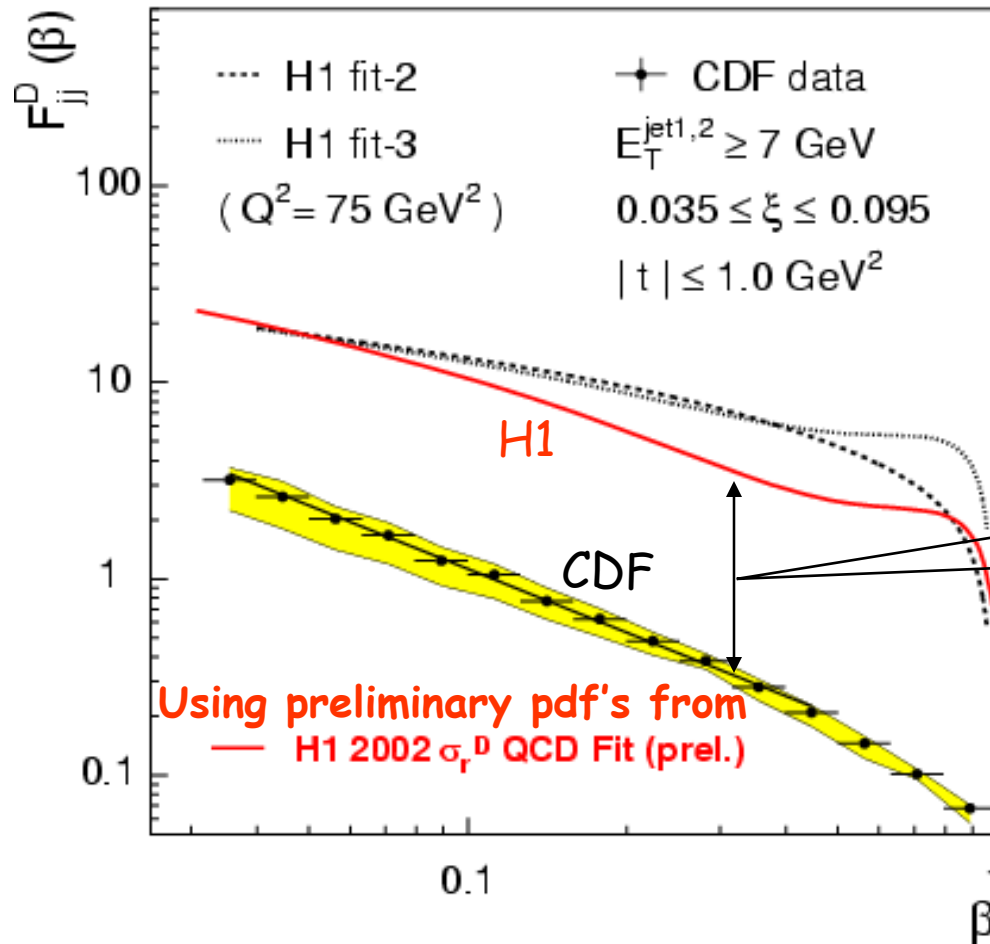
$$S_{2\text{-gap}/1\text{-gap}}^{1\text{-gap}/0\text{-gap}} (630 \text{ GeV}) \approx 0.29$$

Diffractive Structure Function

→ breakdown of QCD factorization !

Diffraction Structure Function

Breakdown of QCD factorization

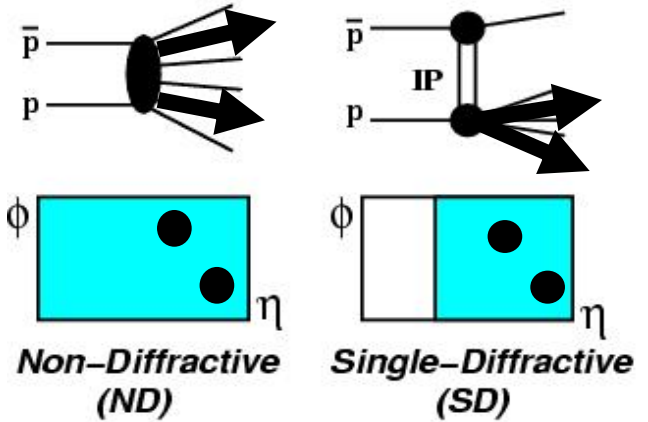


$$\bar{p}p \rightarrow \bar{p} + \text{dijet} + X$$

same suppression
as in soft diffraction - why?

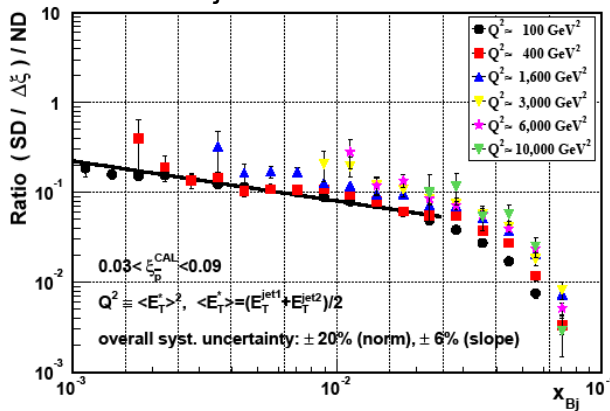
momentum fraction of parton
in "Pomeron" - note quotes

DSF from Dijets in Run II

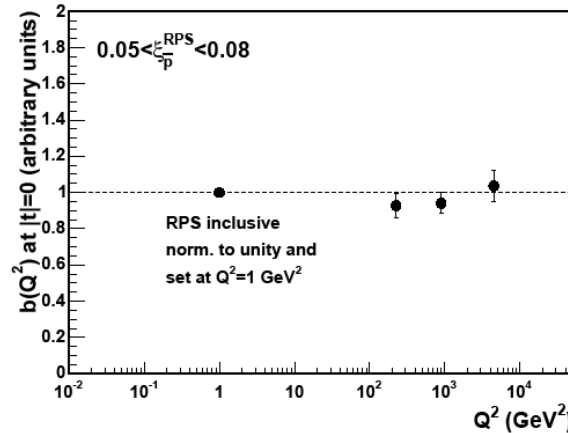


$$R(x_{Bj}) \equiv \frac{\text{Rate}_{jj}^{\text{SD}}(x_{Bj})}{\text{Rate}_{jj}^{\text{ND}}(x_{Bj})} \Rightarrow \frac{F_{jj}^{\text{SD}}(x_{Bj})}{F_{jj}^{\text{ND}}(x_{Bj})}$$

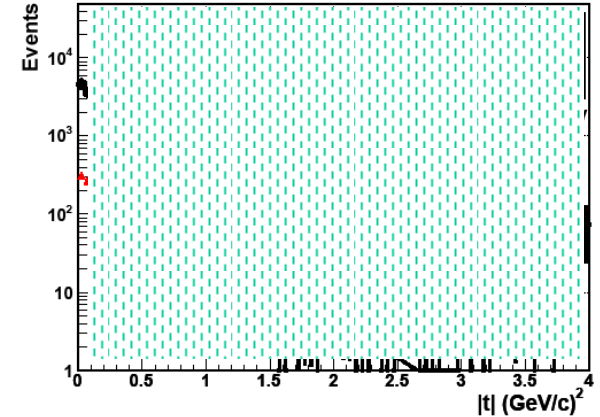
x_{Bj} - distribution



b - slope of t-distribution

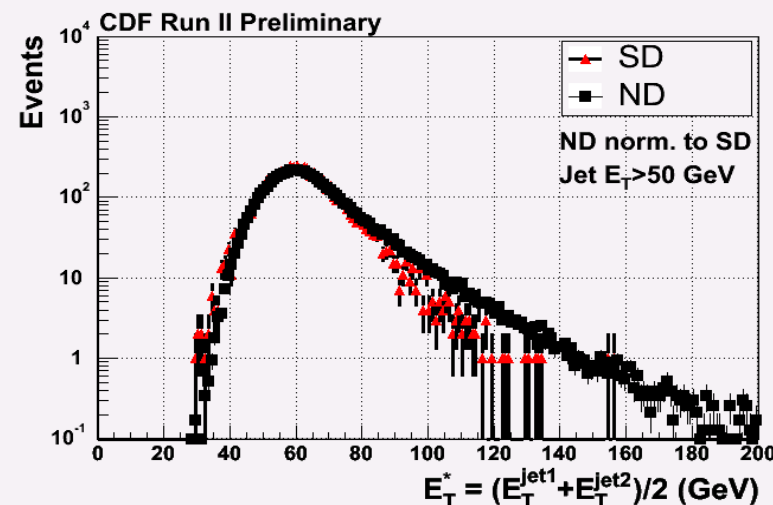
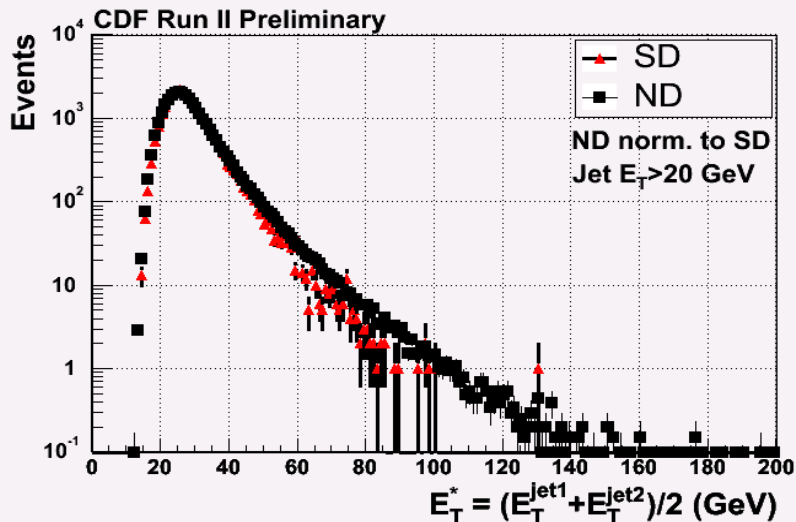
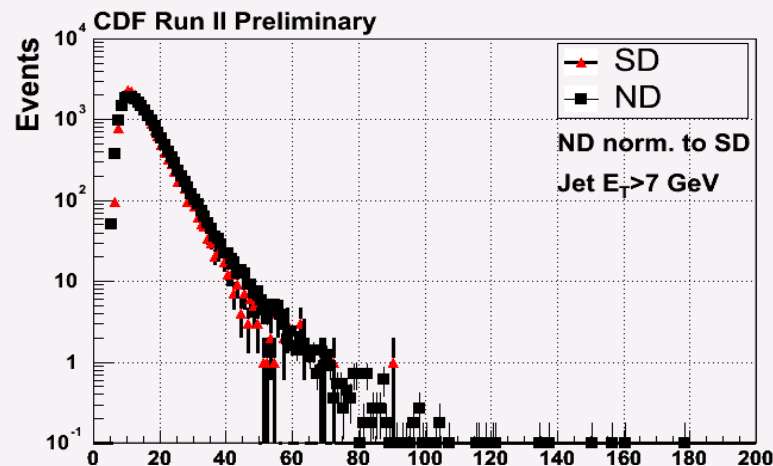
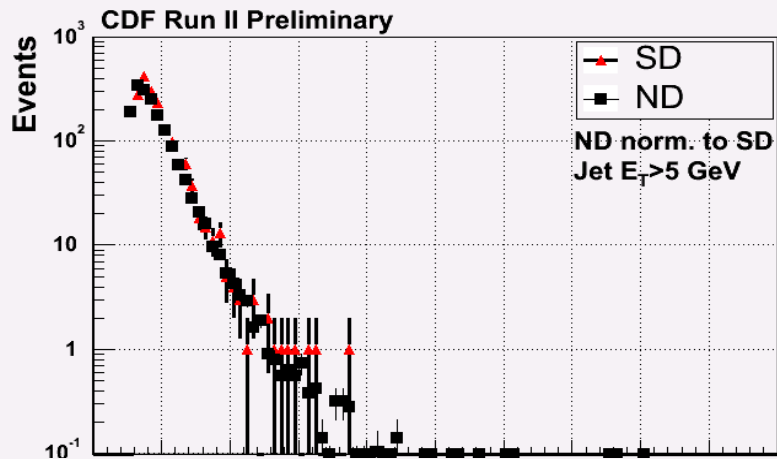


t - distribution



- The x_{Bj} -distribution of the SD/ND ratio has no strong Q^2 dependence
 - the slope of the t-distribution is independent of Q^2
 - the t-distribution $??????$ diffraction minimum $??????$
- all three results → **“first observation”**

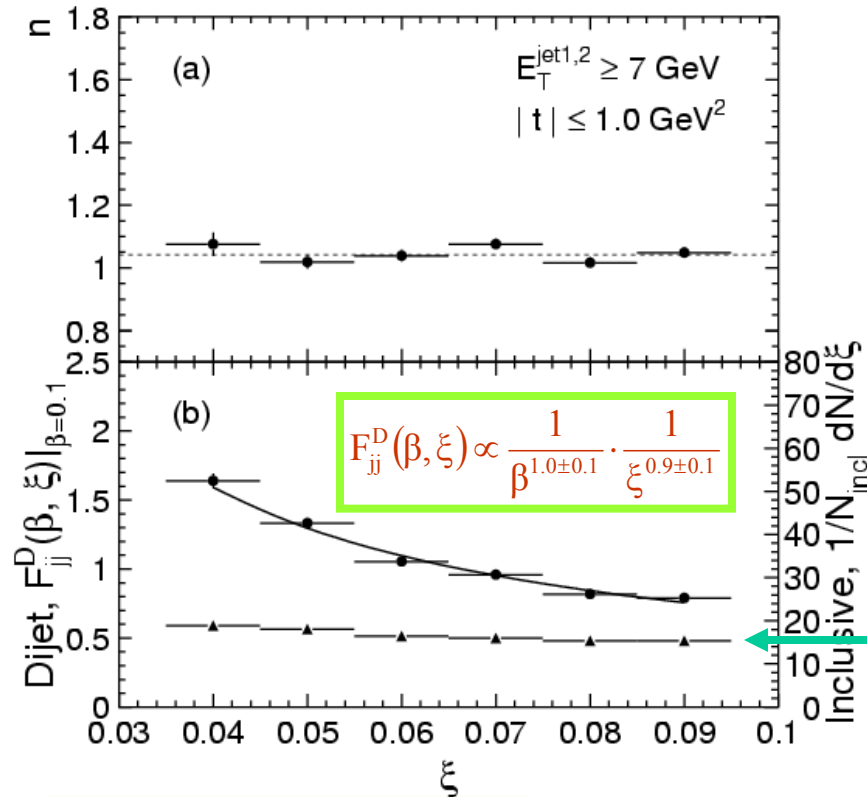
Dijet E_T distributions



→ similar for SD and ND over 4 orders of magnitude

↑ Kinematics

ξ & β dependence of F_{jj}^D – Run I



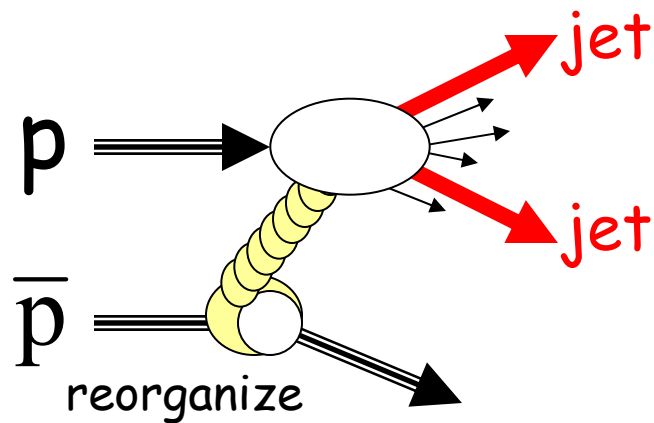
$$\frac{d\sigma_{\text{incl}}}{d\xi} \propto \text{constant}$$

$$F_{jj}^D(\beta, \xi) \sim \frac{1}{\beta} \cdot \frac{1}{\xi}$$

Pomeron dominated

hard diffraction phenomenology
→ for your thought !

Diffractive dijets @ Tevatron



$$F^D(\xi, x, Q^2) \propto \frac{1}{\xi^{1+2\epsilon}} \cdot F(x/\xi, Q^2)$$

$F^D_{JJ}(\xi, \beta, Q^2)$ @ Tevatron

$$F^D(\xi, \beta, Q^2) = N_{\text{renorm}} \frac{1}{\xi^{1+2\varepsilon}} \cdot \frac{C(Q^2)}{(x/\xi)^{\lambda(Q^2)}} = \frac{2\varepsilon}{(\beta s)^{2\varepsilon}} \cdot \frac{1}{\xi^{1+2\varepsilon}} \cdot \frac{C(Q^2)}{\beta^{\lambda(Q^2)}}$$

$$N_{\text{renorm}}^{-1} = \int_{\xi_{\min}}^1 \frac{d\xi}{\xi^{1+2\varepsilon}} \xrightarrow{\xi_{\min} = \frac{x_{\min}}{\beta} \approx \frac{1}{\beta s}} \frac{(\beta s)^{2\varepsilon}}{2\varepsilon}$$

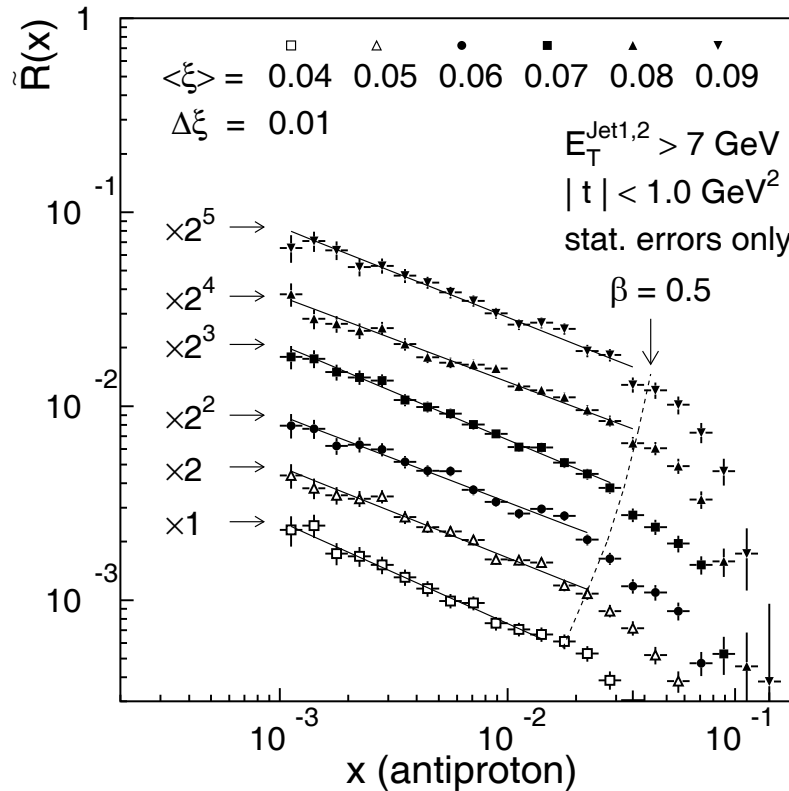
$$\text{RENORM} \Rightarrow R_{ND}^{SD}(x) = \frac{2\varepsilon}{s^{2\varepsilon}} \frac{1}{\xi^{1-\lambda(Q^2)}} \cdot x^{-(2\varepsilon)}$$

$$\varepsilon_g = 0.2 \rightarrow x^{-0.4}$$

SD/ND dijet ratio vs. x_{Bj} @ CDF

CDF Run I

$$R(x) = \frac{F_{jj}^{SD}(x)}{F_{jj}^{ND}(x)}$$



$$0.035 < \xi < 0.095$$

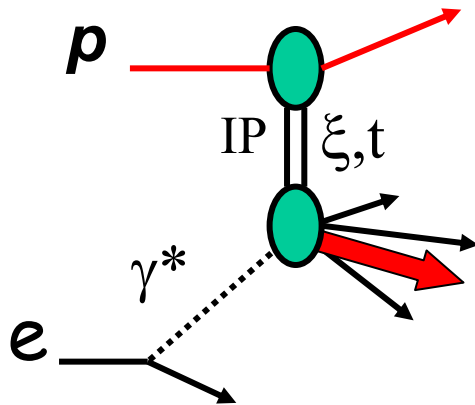
Flat ξ dependence
for $\beta < 0.5$

$$R(x) = x^{-0.45}$$

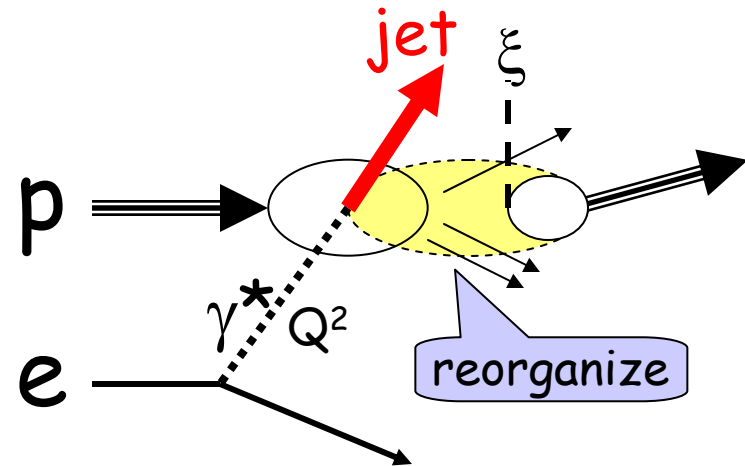
Diffractive DIS @ HERA

J. Collins: factorization holds (but under what conditions?)

Pomeron exchange



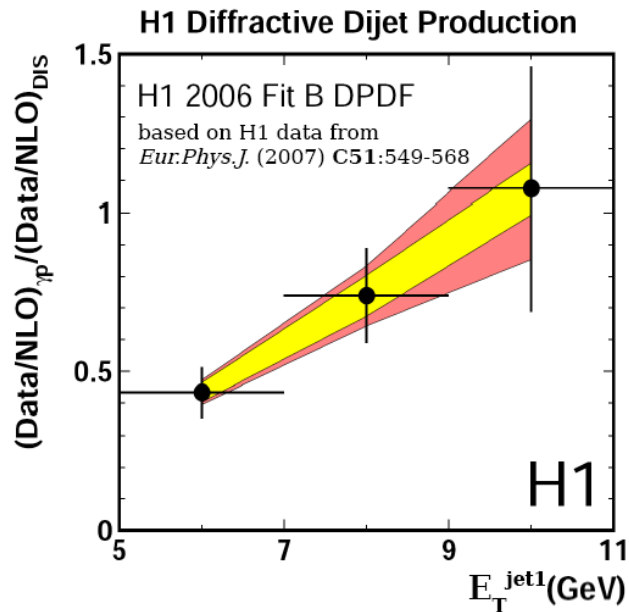
Color reorganization



$$F_2^{D(3)}(\xi, x, Q^2) \propto \frac{1}{\xi^{1+\epsilon}} \cdot F_2(x, Q^2)$$

Results favor color reorganization

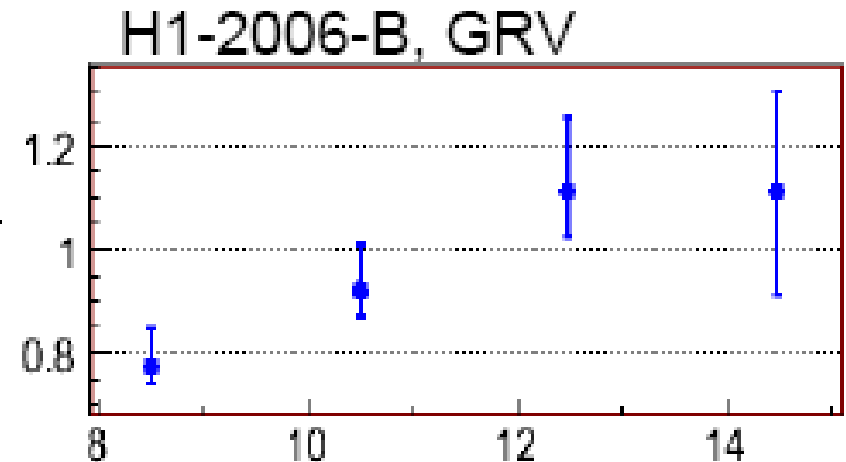
Dijets in γp at HERA - 2008



ZEUS
data

NLO

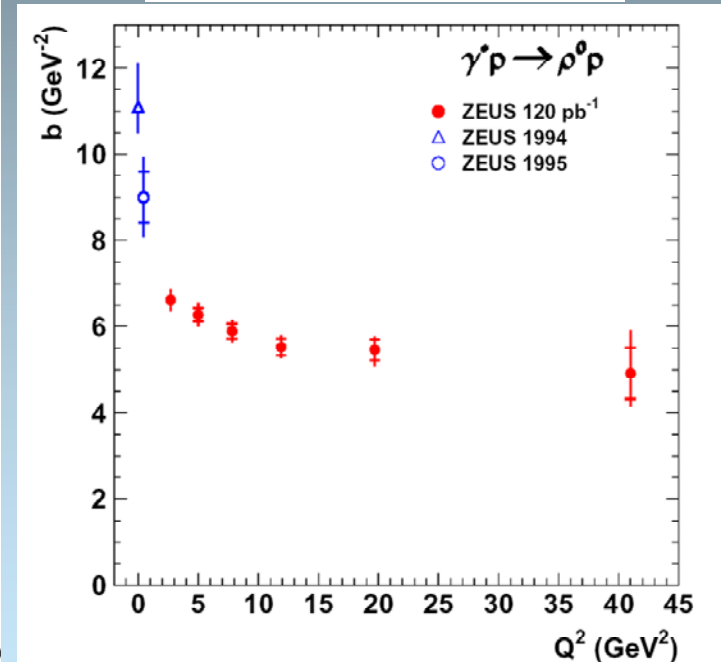
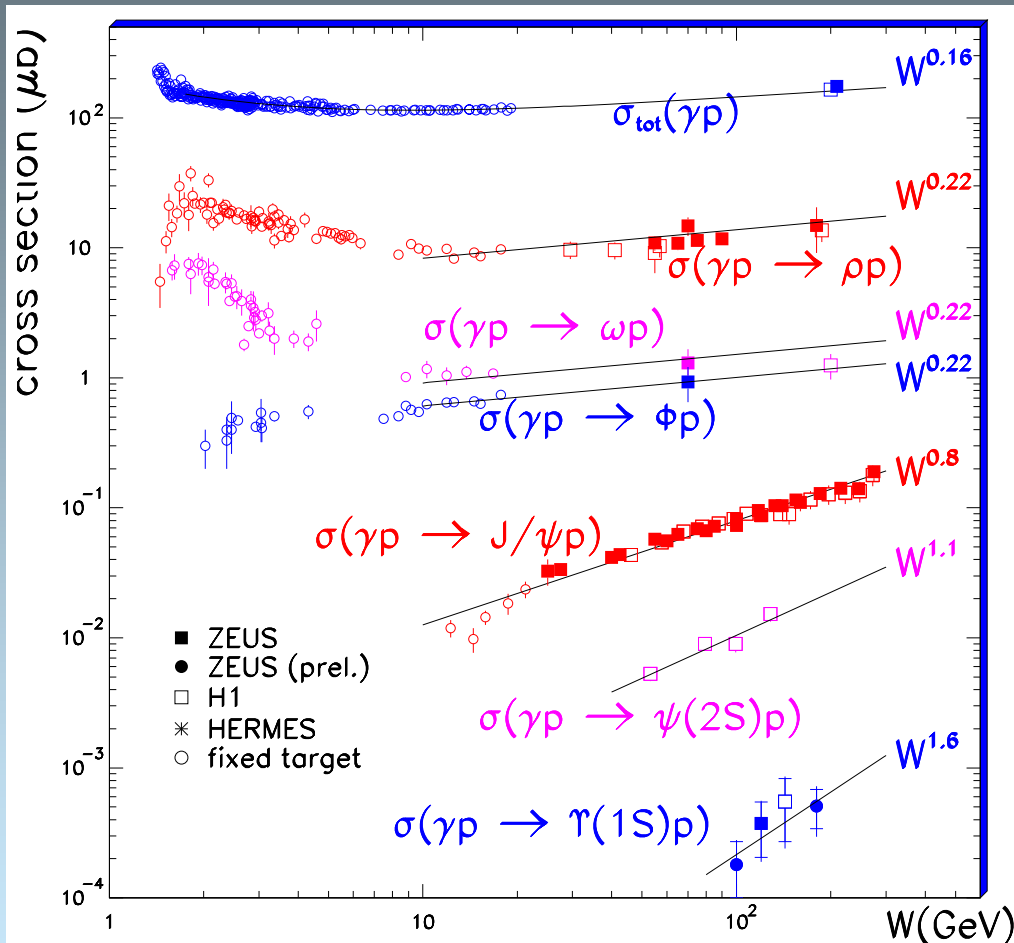
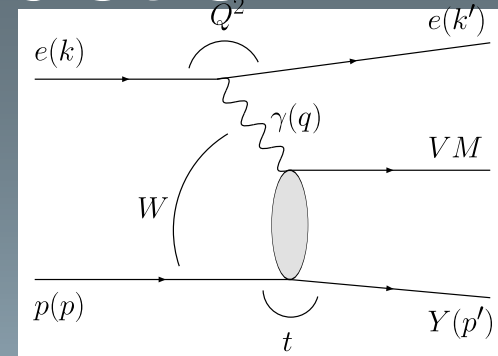
DIS 2008 talk by W. Slomiński,



- 20-50 % apparent rise when E_T^{jet} 5 \rightarrow 10 GeV
- due to suppression at low E_T^{jet} !!!

Vector meson production

(Pierre Marage, HERA-LHC 2008)

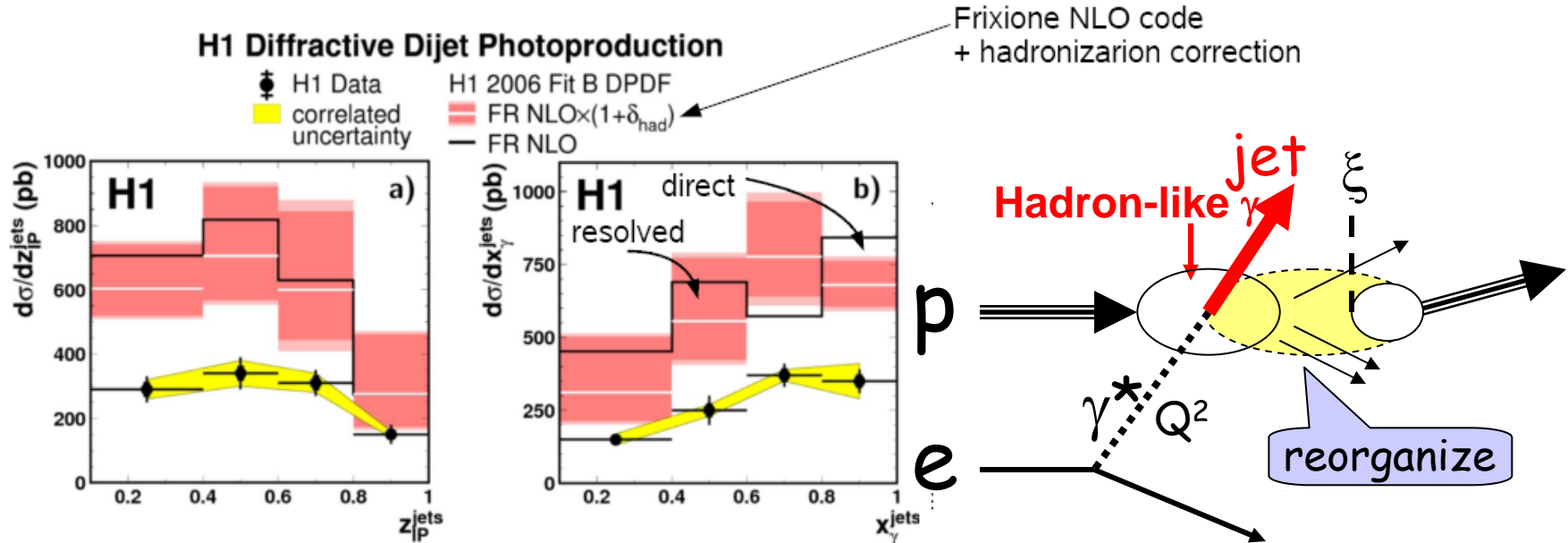


- *left* - why different σ vs. W slopes? \rightarrow more room for particles
- *right* - why smaller b -slope in γ^*p ? \rightarrow same reason

Dijets in γp at HERA – 2007

Dijets in γp

Direct vs. resolved



□ the reorganization diagram predicts:

- suppression at low $Z_{\text{IP}}^{\text{jets}}$, since larger $\Delta\eta$ is available for particles
- same suppression for direct and resolved processes

more phenomenology
→ for your thought, again!

σ^{SD} and ratio of α'/ϵ

PHYSICAL REVIEW D 80, 111901(R) (2009)

Pomeron intercept and slope: A QCD connection

Konstantin Goulianos

$$\frac{d^2 \sigma_{\text{sd}}(s, M^2, t)}{dM^2 dt} = \left[\frac{\sigma_{\circ}}{16\pi} \sigma_{\circ}^{\text{pp}} \right] \frac{s^{2\epsilon}}{N(s)} \frac{1}{(M^2)^{1+\epsilon}} e^{bt}$$

$$\xrightarrow{s \rightarrow \infty} \left[2\alpha' e^{(\epsilon b_0)/\alpha'} \sigma_{\circ}^{\text{pp}} \right] \frac{\ln s^{2\epsilon}}{(M^2)^{1+\epsilon}} e^{bt}$$

$$\sigma_{pp/\bar{p}p}^{\text{tot}} = \sigma_{\circ} \cdot e^{\epsilon \Delta \eta}$$

$$\sigma_{\text{sd}}^{\infty} = 2\sigma_{\circ}^{\text{pp}} \exp\left[\frac{\epsilon b_0}{2\alpha'}\right] = \sigma_{\circ}^{\text{pp}}$$

$$\sigma_{\circ}^{\text{pp}} = \beta_{\text{pp}}(0) \cdot g(t) = \kappa \sigma_{\circ}^{\text{pp}}$$

$$\kappa = \frac{f_g^{\infty}}{N_c^2 - 1} + \frac{f_q^{\infty}}{N_c}$$

$$b_0 = R_p^2/2 = 1/(2m_{\pi}^2).$$

$$r = \frac{\alpha'}{\epsilon} = -[16m_{\pi}^2 \ln(2\kappa)]^{-1}$$

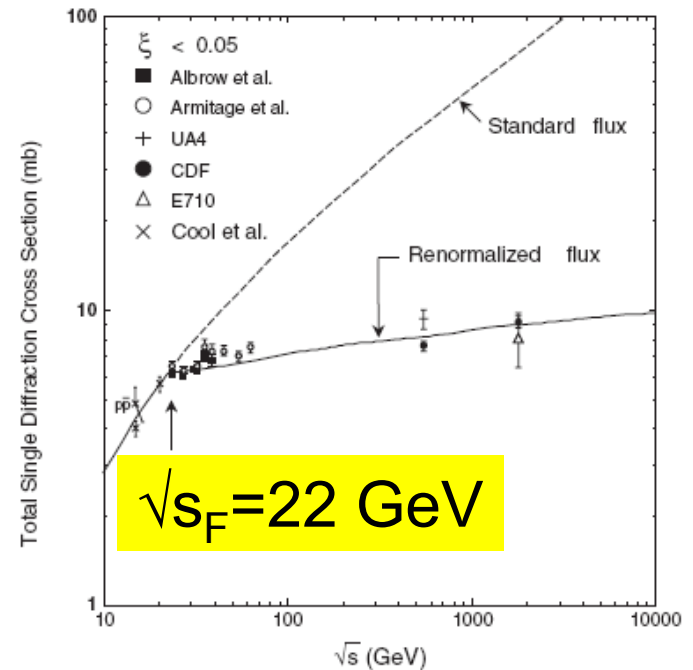
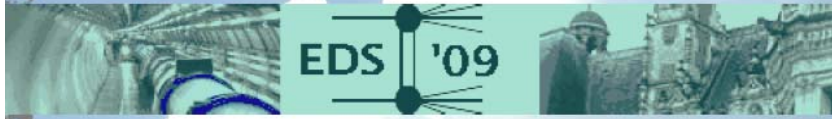
$$r_{\text{pheno}} = 3.2 \pm 0.4 \text{ (GeV/c)}^{-2}$$

$$r_{\text{exp}} = 0.25 \text{ (GeV/c)}^{-2} / 0.08 = 3.13 \text{ (GeV/c)}^{-2}$$

Diffractive and Total pp Cross Sections at LHC



Konstantin Goulios
The Rockefeller University



$\sqrt{s_F} = 22 \text{ GeV}$

- Use the Froissart formula as a *saturated* cross section

$$\sigma_t(s > s_F) = \sigma_t(s_F) + \frac{\pi}{m^2} \cdot \ln^2 \frac{s}{s_F}$$

- This formula should be valid above the *knee* in σ_{sd} vs. \sqrt{s} at $\sqrt{s_F} = 22 \text{ GeV}$ (Fig. 1) and therefore valid at $\sqrt{s} = 1800 \text{ GeV}$.
- Use $m^2 = s_o$ in the Froissart formula multiplied by $1/0.389$ to convert it to mb^{-1} .
- Note that contributions from Reggeon exchanges at $\sqrt{s} = 1800 \text{ GeV}$ are negligible, as can be verified from the global fit of Ref. [7].
- Obtain the total cross section at the LHC:

SUPERBALL MODEL

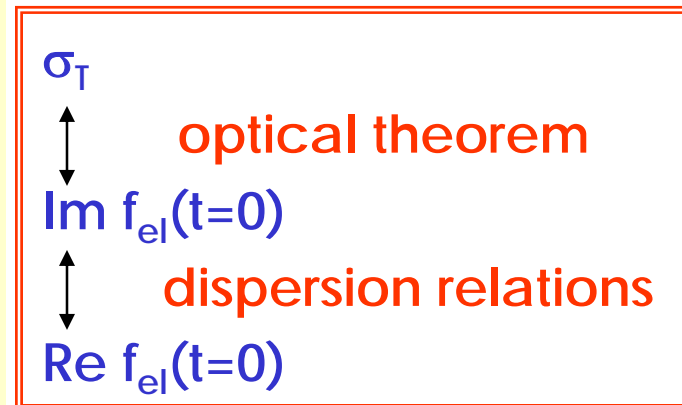
$$\sigma_t^{\text{LHC}} = \sigma_t^{\text{CDF}} + \frac{\pi}{s_o} \cdot \left(\ln^2 \frac{s^{\text{LHC}}}{s_F} - \ln^2 \frac{s^{\text{CDF}}}{s_F} \right)$$

$$\sigma_{14000 \text{ GeV}}^{\text{LHC}} = (80 \pm 3) + (29 \pm 12) = 109 \pm 12 \text{ mb}$$

Strategy and Conclusion

STRATEGY

- σ^T from SUPERBALL model
- optical theorem $\rightarrow \text{Im } f_{el}(t=0)$
- dispersion relations $\rightarrow \text{Re } f_{el}(t=0)$
- differential σ^{SD} from RENORM
- use nested pp final states for Pomeron-proton collisions at \sqrt{s}



For a phenomenological approach see: K. Goulianos, Phys. Lett. B 193 (1987) 151 pp

CONCUSION

more to come...

First CMS event

