

# Diffractive Cross Sections Implemented in PYTHIA8-MBR vs LHC Results



Konstantin Goulios  
The Rockefeller University

<http://physics.rockefeller.edu/dino/my.html>

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<http://www.weizmann.ac.il/conferences/lowX/>

# CONTENTS ♥

- ❑ **Total pp cross section:** predicted in a unitarized parton model approach, which does not employ eikonalization and does not depend on the  $\rho$ -value.
  - ❑ **Diffractive cross sections:**
    - ❑ SD - single dissociation: one of the protons dissociates.
    - ❑ DD - double dissociation: both protons dissociate.
    - ❑ CD – central diffraction: neither proton dissociates, but there is central diffractive production of particles.
  - ❑ **Triple-Pomeron coupling:** uniquely determined.
- ➔ For details see ICHEP 2012, 6 July 2012, **arXiv:1205.1446** (talk by Robert Ciesielski and KG).

♥ This is an updated version of a talk presented in DIS-2013.

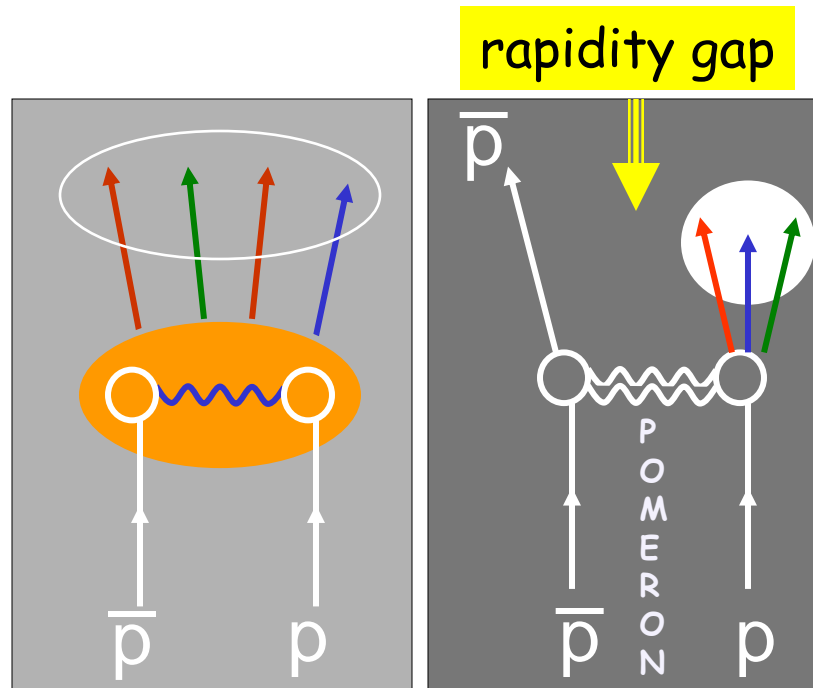
# DIFFRACTION IN QCD

## Non-diffractive events

- ❖ color-exchange  $\rightarrow$   $\eta$ -gaps exponentially suppressed

## Diffractive events

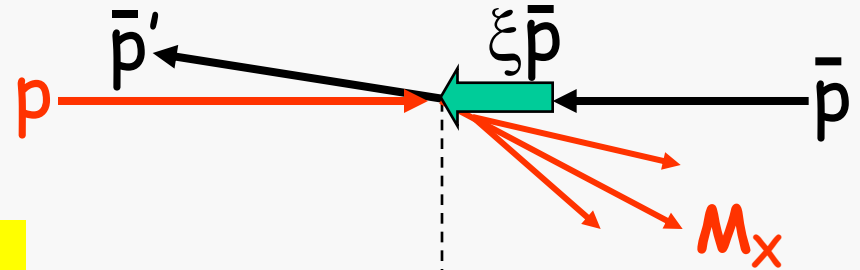
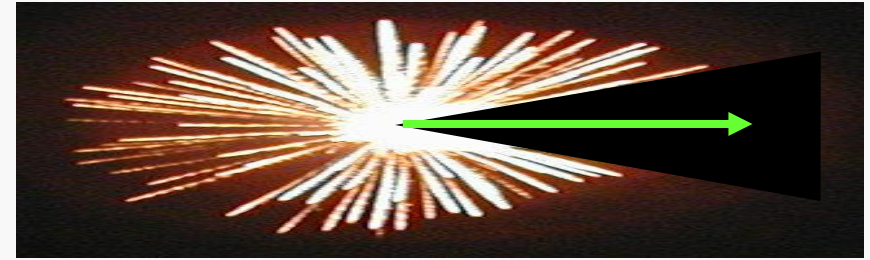
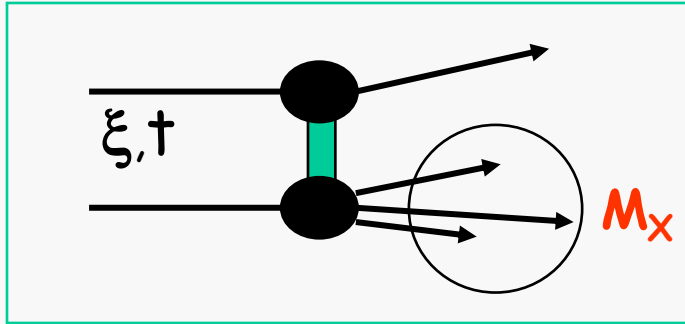
- ❖ Colorless vacuum exchange  $\rightarrow$   $\eta$ -gaps not suppressed



Goal: probe the QCD nature of the diffractive exchange

# DEFINITIONS

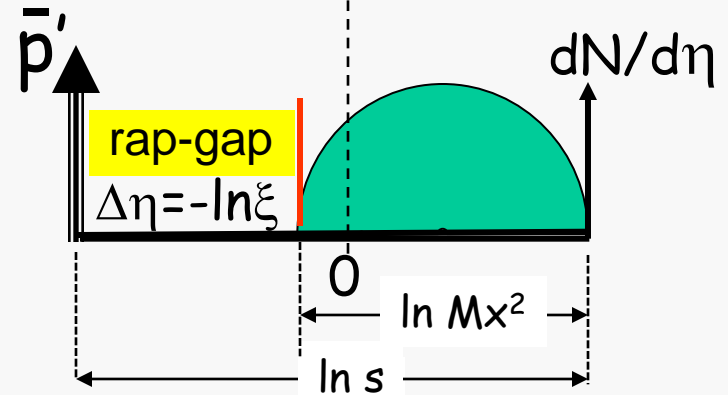
## SINGLE DIFFRACTION



$$1 - x_L \equiv \xi = \frac{M_X^2}{s}$$

Forward momentum loss

$$\xi^{\text{CAL}} = \frac{\sum_{i=1}^{\text{all}} E_T^{i\text{-tower}} e^{-\eta_i}}{\sqrt{s}}$$



**since no radiation**  $\rightarrow$   
no price paid for increasing  
diffractive-gap width

$$\left( \frac{d\sigma}{d\Delta\eta} \right)_{t=0} \approx \text{constant} \Rightarrow \frac{d\sigma}{d\xi} \propto \frac{1}{\xi} \Rightarrow \frac{d\sigma}{dM^2} \propto \frac{1}{M^2}$$

# DIFFRACTION AT CDF

Elastic scattering

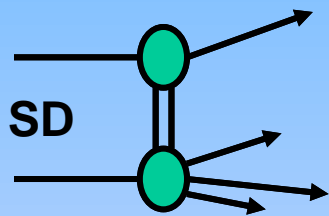


$\sigma_T = \text{Im } f_{el}(t=0)$

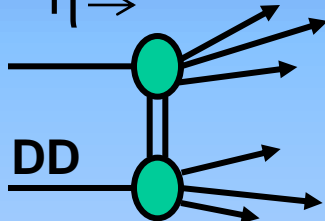
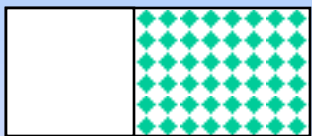


OPTICAL THEOREM

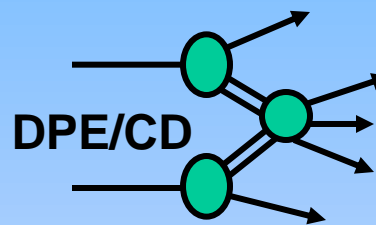
Total cross section



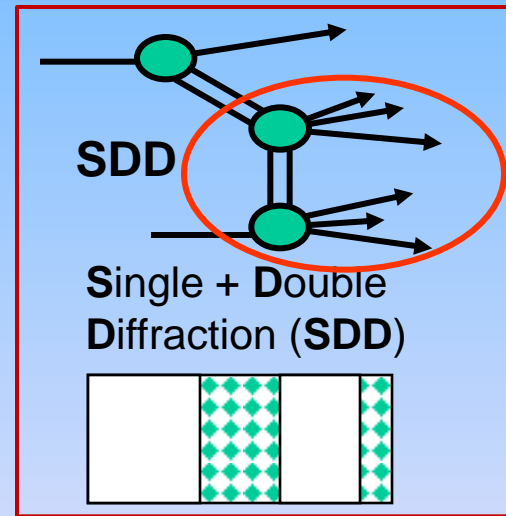
Single Diffraction or Single Dissociation



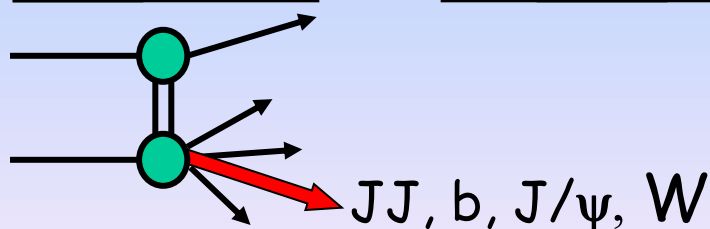
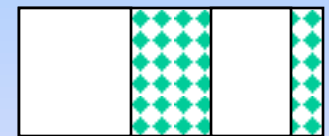
Double Diffraction or Double Dissociation



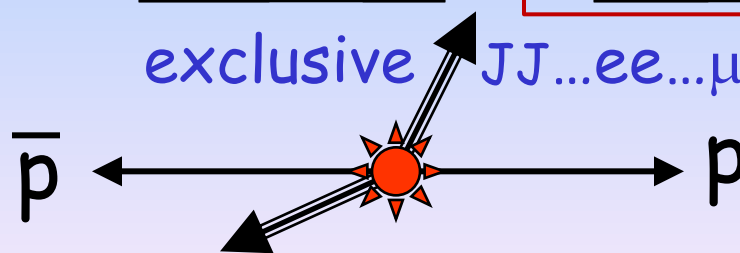
Double Pom. Exchange or Central Dissociation



Single + Double Diffraction (SDD)

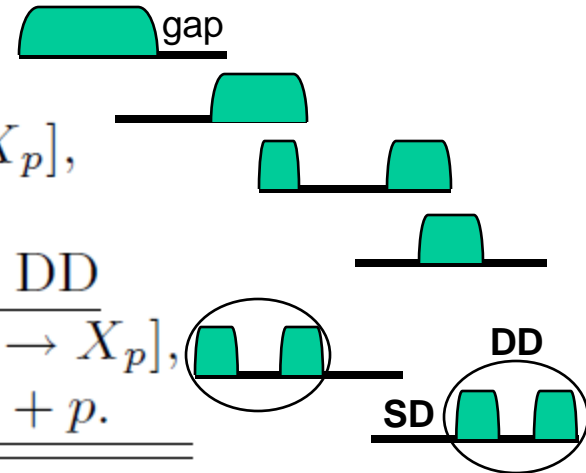


exclusive  $JJ \dots ee \dots \mu\mu \dots \gamma\gamma$

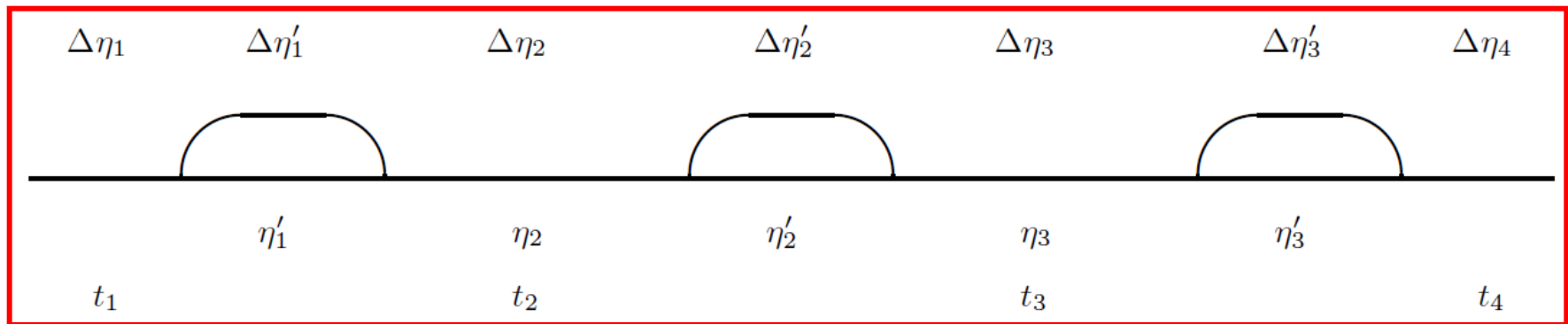


# Basic and combined diffractive processes

acronym	basic diffractive processes
$SD_{\bar{p}}$	$\bar{p}p \rightarrow \bar{p} + \text{gap} + [p \rightarrow X_p],$
$SD_p$	$\bar{p}p \rightarrow [\bar{p} \rightarrow X_{\bar{p}}] + \text{gap} + p,$
$DD$	$\bar{p}p \rightarrow [\bar{p} \rightarrow X_{\bar{p}}] + \text{gap} + [p \rightarrow X_p],$
$DPE$	$\bar{p}p \rightarrow \bar{p} + \text{gap} + X_c + \text{gap} + p,$ 2-gap combinations of SD and DD
$SDD_{\bar{p}}$	$\bar{p}p \rightarrow \bar{p} + \text{gap} + X_c + \text{gap} + [p \rightarrow X_p],$
$SDD_p$	$\bar{p}p \rightarrow [\bar{p} \rightarrow X_{\bar{p}}] \text{gap} + X_c + \text{gap} + p.$

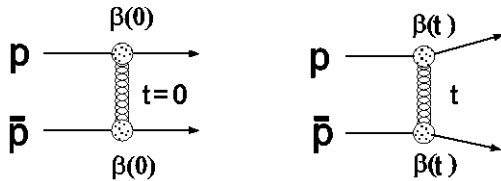


4-gap diffractive process-Snowmass 2001- <http://arxiv.org/pdf/hep-ph/0110240>

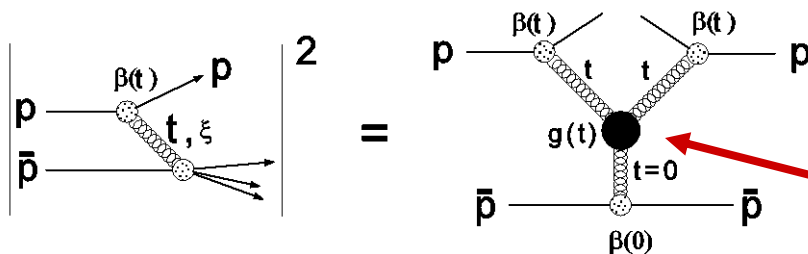


# Regge theory – values of $s_0$ & $g_{PPP}$ ?

KG-PLB 358, 379 (1995)



SINGLE DIFFRACTION DISSOCIATION



Parameters:

- $s_0, s_0'$  and  $g(t)$
- set  $s_0' = s_0$  (universal  $IP$ )
- determine  $s_0$  and  $g_{PPP}$  – **how?**

$$\alpha(t) = \alpha(0) + \alpha' t \quad \alpha(0) = 1 + \epsilon$$

$$\sigma_T = \beta_1(0) \beta_2(0) \left( \frac{s}{s_0} \right)^{\alpha(0)-1} = \sigma_0^{p\bar{p}} \left( \frac{s}{s_0} \right)^\epsilon \quad (1)$$

$$\begin{aligned} \frac{d\sigma_{el}}{dt} &= \frac{\beta_1^2(t) \beta_2^2(t)}{16\pi} \left( \frac{s}{s_0} \right)^{2[\alpha(t)-1]} \\ &= \frac{\sigma_T^2}{16\pi} \left( \frac{s}{s_0} \right)^{2\alpha' t} F^4(t) \approx \frac{\sigma_T^2}{16\pi} e^{b_{el}(s)t} \end{aligned} \quad (2)$$

$$F^4(t) \approx e^{b_{0,el} t} \Rightarrow b_{el}(s) = b_{0,el} + 2\alpha' \ln \left( \frac{s}{s_0} \right) \quad (3)$$

$$\frac{d^2 \sigma_{sd}}{dt d\xi}$$

$$\begin{aligned} &= \frac{\beta_1^2(t)}{16\pi} \xi^{1-2\alpha(t)} \left[ \beta_2(0) g(t) \left( \frac{s'}{s'_0} \right)^{\alpha(0)-1} \right] \\ &= f_{p/p}(\xi, t) \sigma_T^{p\bar{p}}(s', t) \end{aligned} \quad (4)$$

# A complication ... → Unitarity!

$$\left(\frac{d\sigma_{el}}{dt}\right)_{t=0} \sim \left(\frac{s}{s_0}\right)^{2\epsilon}, \quad \sigma_t \sim \left(\frac{s}{s_0}\right)^\epsilon, \quad \text{and} \quad \sigma_{sd} \sim \left(\frac{s}{s_0}\right)^{2\epsilon}$$

□  $\sigma_{sd}$  grows faster than  $\sigma_t$  as  $s$  increases \*

→ **unitarity violation at high  $s$**

(similarly for partial x-sections in impact parameter space)

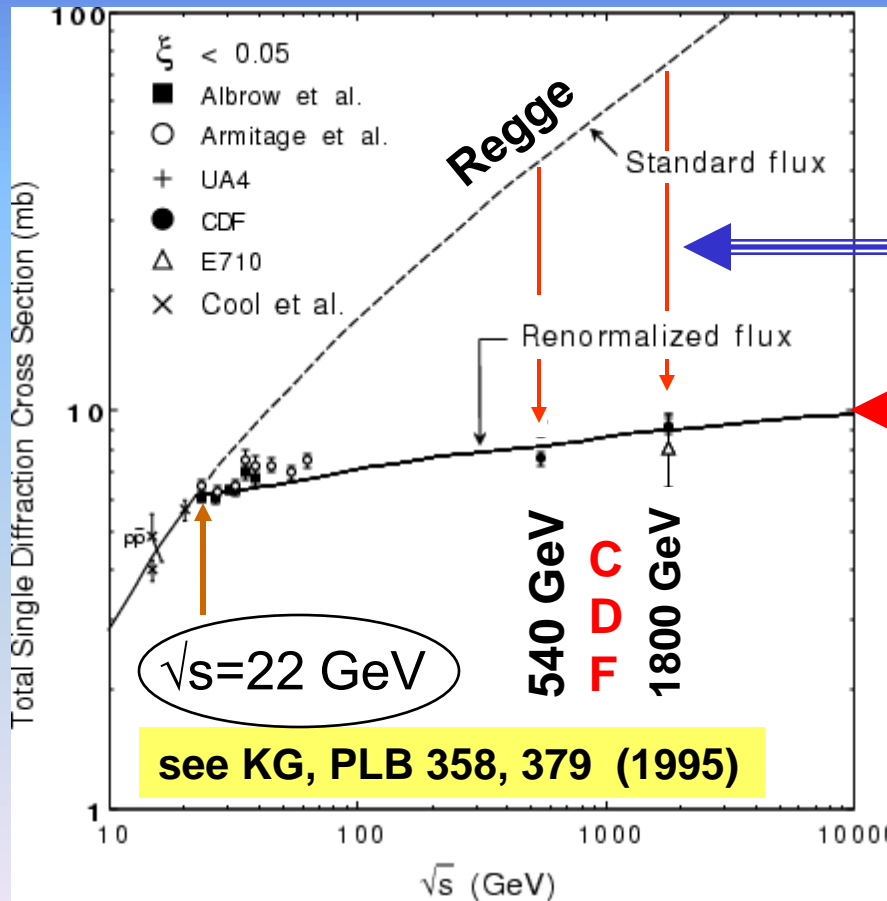
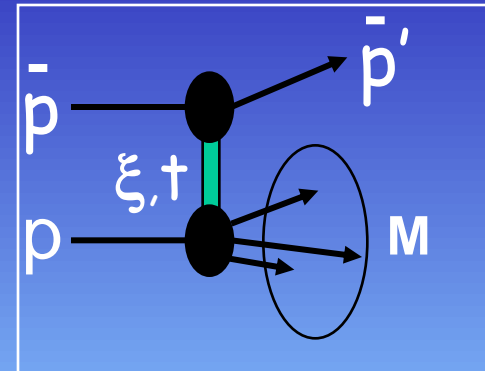
□ **the unitarity limit is already reached at  $\sqrt{s} \sim 2 \text{ TeV}$  !**

□ **need unitarization**



# FACTORIZATION BREAKING IN SOFT DIFFRACTION

→ diffractive x-section suppressed relative to Regge prediction as  $\sqrt{s}$  increases



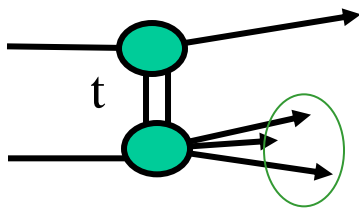
Factor of  $\sim 8$  ( $\sim 5$ )  
suppression at  
 $\sqrt{s} = 1800$  ( $540$ ) GeV

**RENORMALIZATION**

Interpret flux as gap  
formation probability  
that saturates when it  
reaches unity

# Single diffraction renormalized - 1

KG → CORFU-2001: <http://arxiv.org/abs/hep-ph/0203141>



2 independent variables:  $t, \Delta y$

color factor  $\kappa = \frac{g_{IP-IP-IP}(t)}{\beta_{IP-p-p}(0)} \approx 0.17$

$$\frac{d^2 \sigma}{dt d\Delta y} = C \cdot F_p^2(t) \cdot \left\{ e^{(\varepsilon + \alpha' t) \Delta y} \right\}^2 \cdot \kappa \cdot \left\{ \sigma_0 e^{\varepsilon \Delta y'} \right\}$$

gap probability

sub-energy x-section

Gap probability → (re)normalize to unity

# Single diffraction renormalized - 2

color factor

$$\kappa = \frac{g_{IP-IP-IP}(t)}{\beta_{IP-p-p}(0)} \approx 0.17$$

Experimentally:

KG&JM, PRD 59 (114017) 1999

$$\kappa = \frac{g_{IP-IP-IP}}{\beta_{IP-p}} = 0.17 \pm 0.02, \quad \varepsilon = 0.104$$

QCD:  $\kappa = f_g \times \frac{1}{N_c^2 - 1} + f_q \times \frac{1}{N_c} \xrightarrow{Q^2 = 1} \approx 0.75 \times \frac{1}{8} + 0.25 \times \frac{1}{3} = 0.18$

# Single diffraction renormalized - 3

$$\frac{d^2 \sigma_{sd}(s, M^2, t)}{dM^2 dt} = \left[ \frac{\sigma_o}{16\pi} \sigma_o^{IPp} \right] \frac{s^{2\epsilon}}{N(s, s_o)} \frac{e^{bt}}{(M^2)^{1+\epsilon}}$$

$$b = b_0 + 2\alpha' \ln \frac{s}{M^2} \quad s_o^{\text{CMG}} = (3.7 \pm 1.5) \text{ GeV}^2$$

$$N(s, s_o) \equiv \int_{\xi_{\min}}^{\xi_{\max}} d\xi \int_{t=0}^{-\infty} dt f_{\mathbb{P}/p}(\xi, t) \xrightarrow{s \rightarrow \infty} \sim s_o^\epsilon \frac{s^{2\epsilon}}{\ln s}$$

$$\frac{d^2 \sigma_{sd}(s, M^2, t)}{dM^2 dt} \xrightarrow{s \rightarrow \infty} \sim \ln s \frac{e^{bt}}{(M^2)^{1+\epsilon}}$$

$$\sigma_{sd} \xrightarrow{s \rightarrow \infty} \sim \frac{\ln s}{b \rightarrow \ln s} \Rightarrow \text{const}$$

set to unity  
 $\rightarrow$  determines  $s_o$

# M<sup>2</sup> distribution: data

→  $d\sigma/dM^2|_{t=-0.05} \sim$  independent of  $s$  over 6 orders of magnitude!

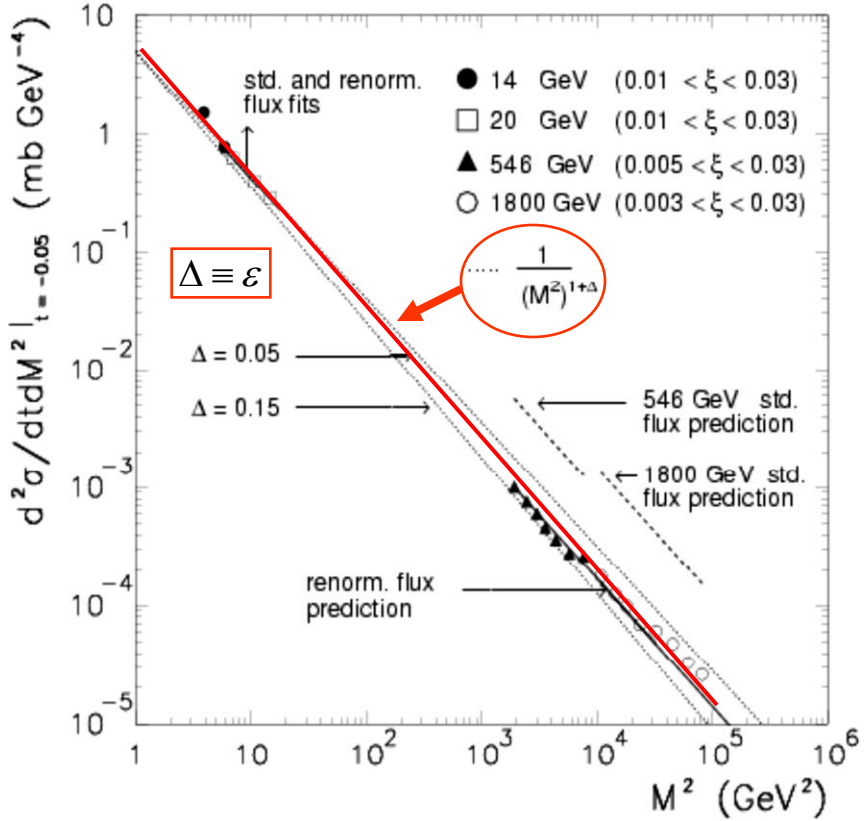
Regge

data

$$\frac{d\sigma}{dM^2} \propto \frac{s^{2\epsilon} \rightarrow 1}{(M^2)^{1+\epsilon}}$$

Independent of  $s$  over 6 orders of magnitude in  $M^2$   
 →  $M^2$  scaling

KG&JM, PRD 59 (1999) 114017



→ factorization breaks down to ensure  $M^2$  scaling!

# Scale $s_0$ and $PPP$ coupling

Pomeron flux: interpret as gap probability

→ set to unity: determines  $g_{PPP}$  and  $s_0$  KG, PLB 358 (1995) 379

$$\frac{d^2 \sigma_{SD}}{dt d\xi} = f_{IP/p}(t, \xi) \sigma_{IP/p}(s\xi)$$

$\downarrow s_0^\varepsilon$   
 $\uparrow s_0^{-\varepsilon/2} \cdot g_{PPP}(t)$

Pomeron-proton x-section

- Two free parameters:  $s_0$  and  $g_{PPP}$
- Obtain product  $g_{PPP} \cdot s_0^{\varepsilon/2}$  from  $\sigma_{SD}$
- Renormalized Pomeron flux determines  $s_0$
- Get unique solution for  $g_{PPP}$

# Saturation at low $Q^2$ and small- $x$

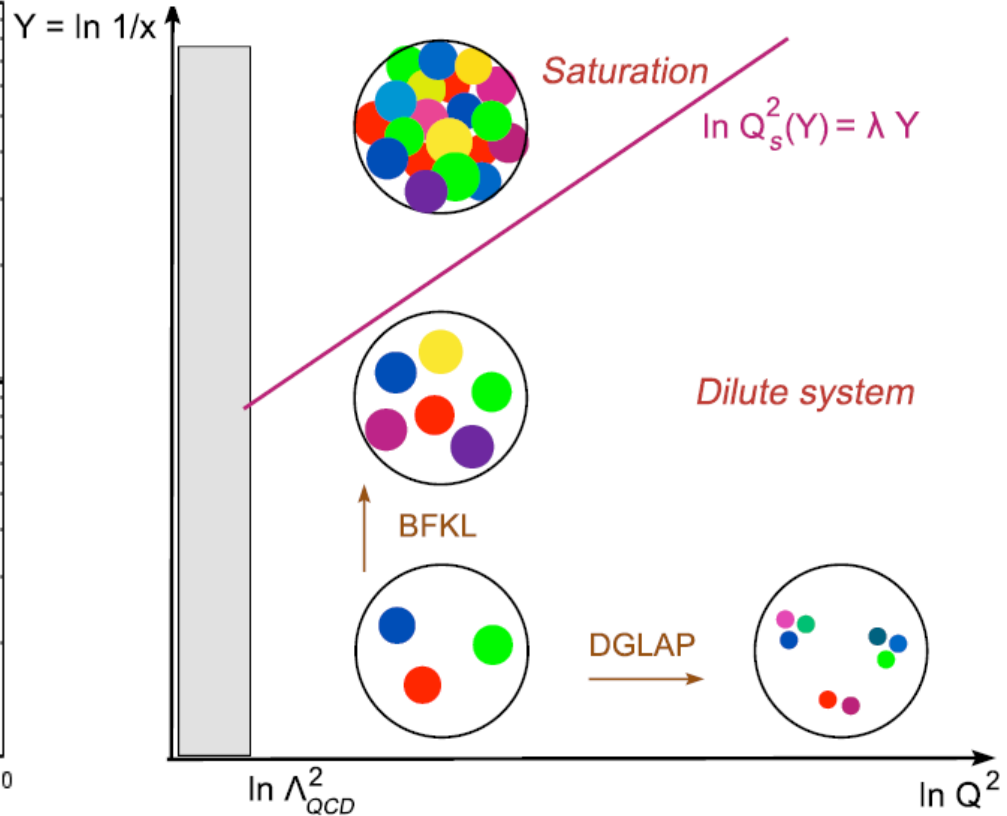
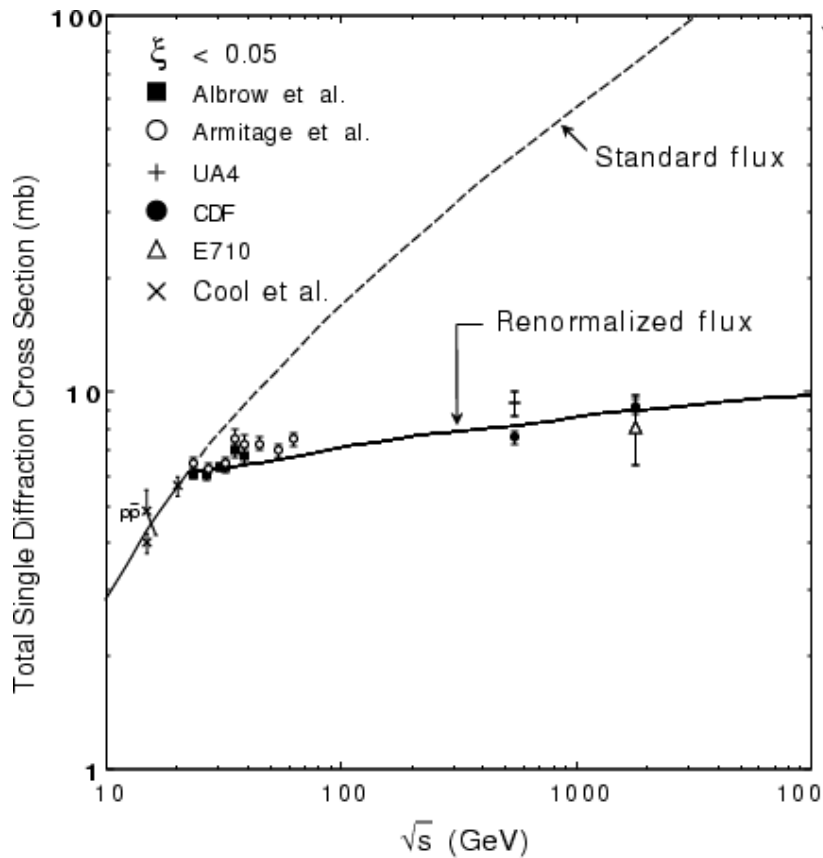
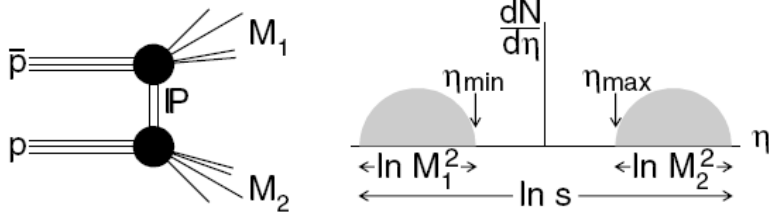


figure from a talk by Edmond Iancu

# DD at CDF

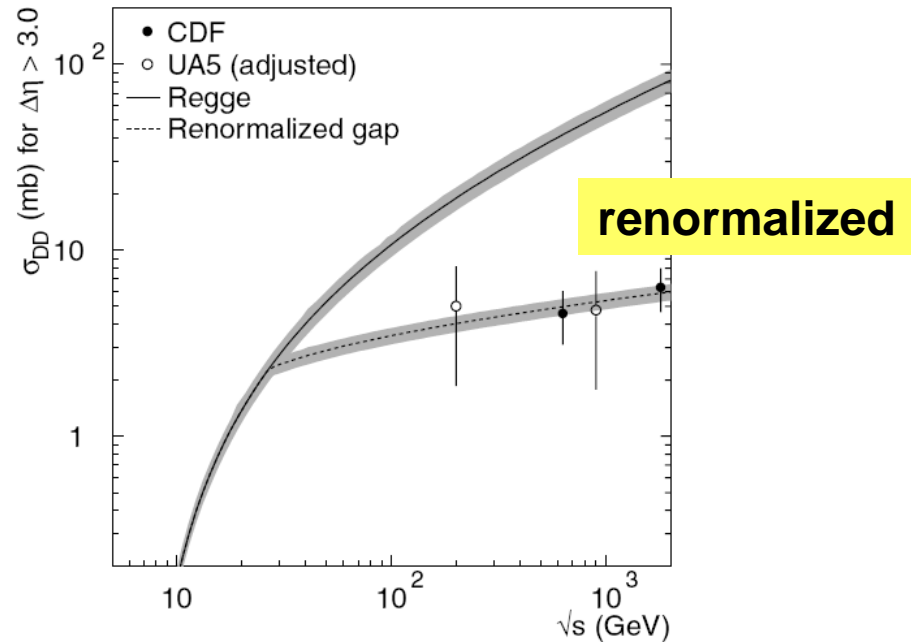
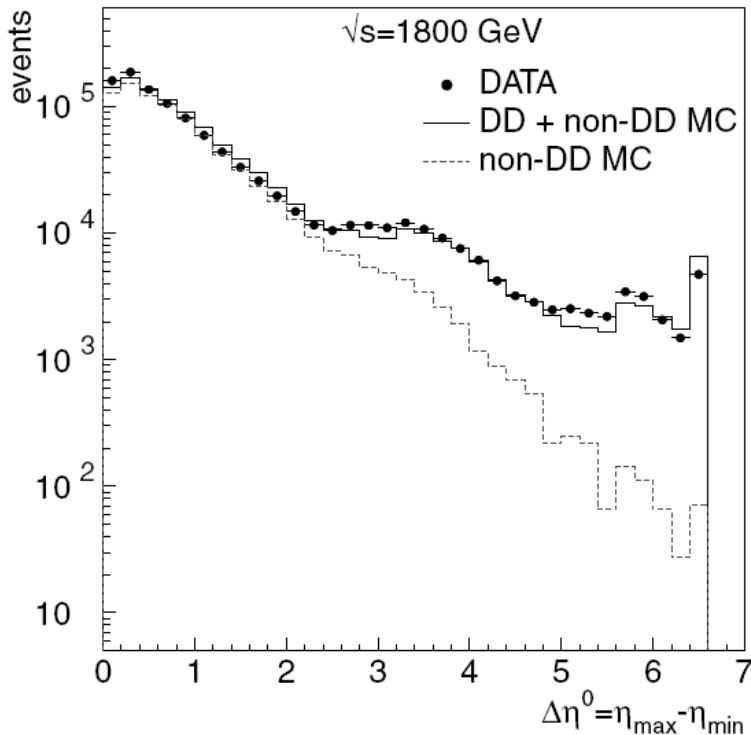


$$\frac{d^3\sigma_{DD}}{dt dM_1^2 dM_2^2} = \frac{d^2\sigma_{SD}}{dt dM_1^2} \frac{d^2\sigma_{SD}}{dt dM_2^2} / \frac{d\sigma_{el}}{dt}$$

$$= \frac{[\kappa \beta_1(0) \beta_2(0)]^2}{16\pi} \frac{s^{2\epsilon} e^{b_{DD}t}}{(M_1^2 M_2^2)^{1+2\epsilon}}$$

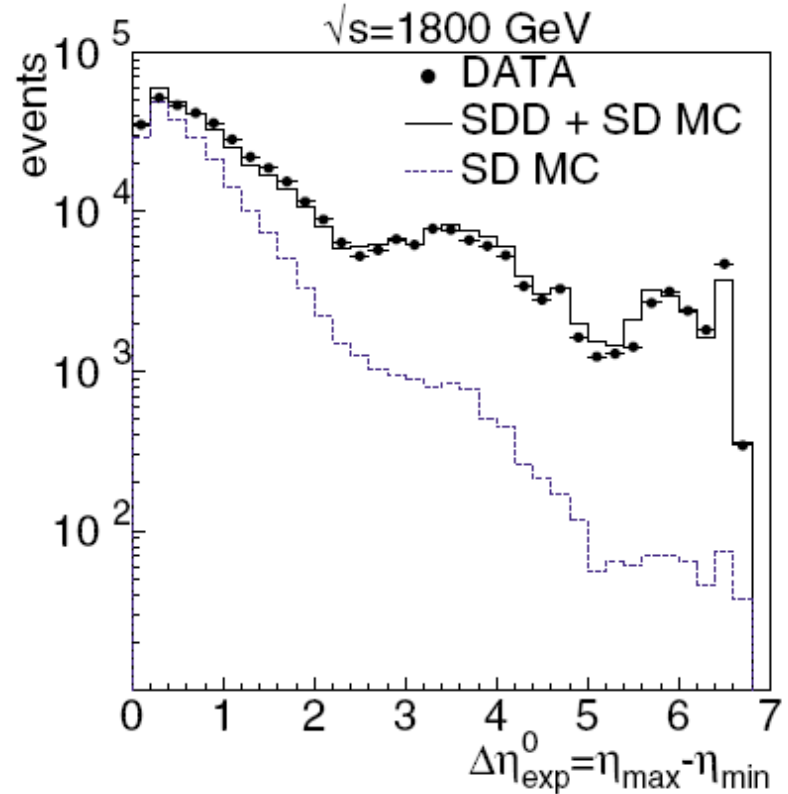
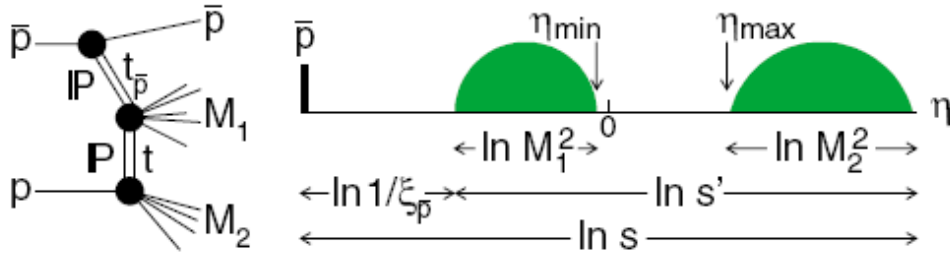
$$\frac{d^3\sigma_{DD}}{dt d\Delta\eta d\eta_c} = \left[ \frac{\kappa \beta^2(0)}{16\pi} e^{2[\alpha(t)-1]\Delta\eta} \right] \left[ \kappa \beta^2(0) \left( \frac{s'}{s_0} \right)^\epsilon \right]$$

gap probability                      x-section





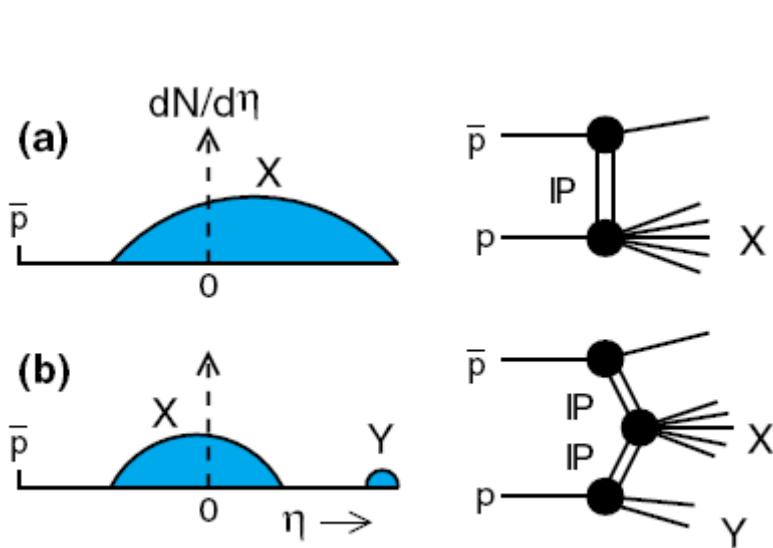
# SDD at CDF



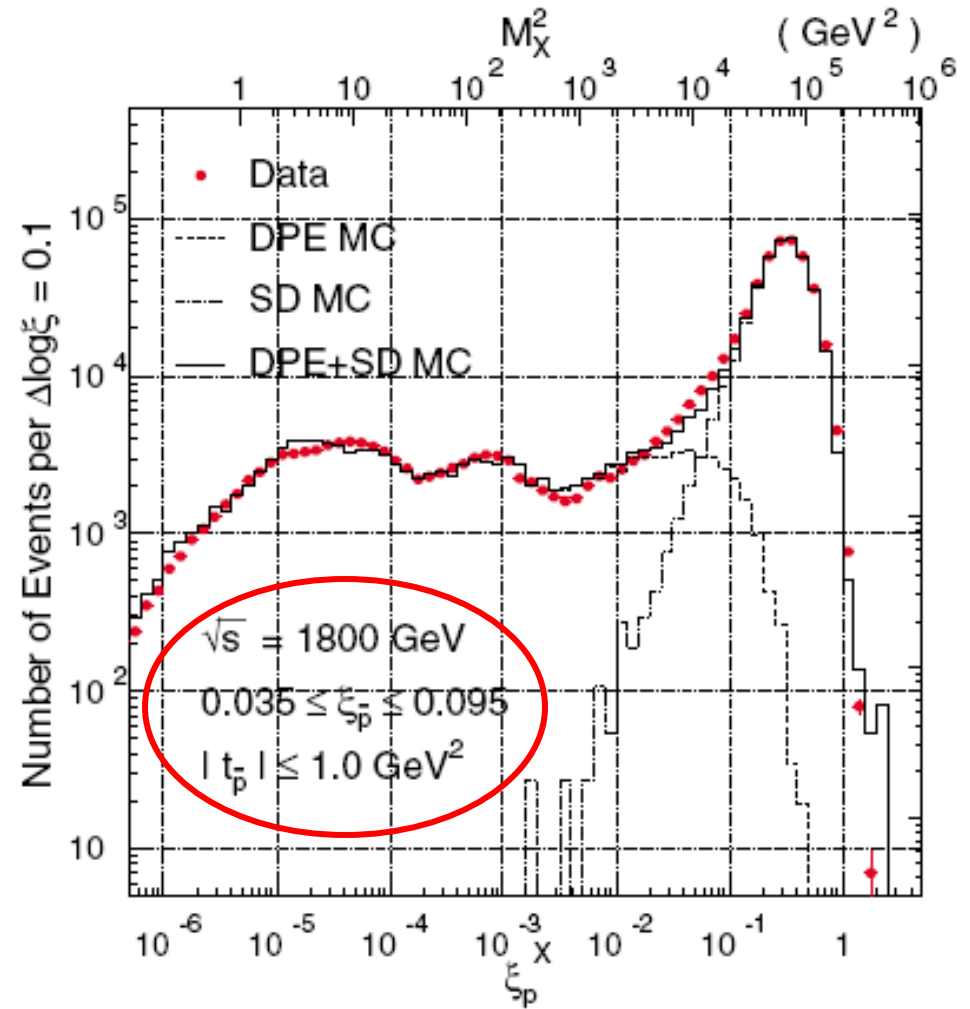
■ Excellent agreement between data and MBR (MinBiasRockefeller) MC

$$\frac{d^5\sigma}{dt_{\bar{p}} dt d\xi_{\bar{p}} d\Delta\eta d\eta_c} = \left[ \frac{\beta(t)}{4\sqrt{\pi}} e^{[\alpha(t_{\bar{p}})-1]\ln(1/\xi)} \right]^2 \times \kappa \left\{ \kappa \left[ \frac{\beta(0)}{4\sqrt{\pi}} e^{[\alpha(t)-1]\Delta\eta} \right]^2 \kappa \left[ \beta^2(0) \left( \frac{s''}{s_0} \right)^\epsilon \right] \right\}$$

# CD/DPE at CDF



■ Excellent agreement between data and MBR  
 → low and high masses are correctly implemented



# Diffractive x-sections

$$\begin{aligned} \frac{d^2\sigma_{SD}}{dt d\Delta y} &= \frac{1}{N_{\text{gap}}(s)} \left[ \frac{\beta^2(t)}{16\pi} e^{2[\alpha(t)-1]\Delta y} \right] \cdot \left\{ \kappa \beta^2(0) \left( \frac{s'}{s_0} \right)^\epsilon \right\}, \\ \frac{d^3\sigma_{DD}}{dt d\Delta y dy_0} &= \frac{1}{N_{\text{gap}}(s)} \left[ \frac{\kappa \beta^2(0)}{16\pi} e^{2[\alpha(t)-1]\Delta y} \right] \cdot \left\{ \kappa \beta^2(0) \left( \frac{s'}{s_0} \right)^\epsilon \right\}, \\ \frac{d^4\sigma_{DPE}}{dt_1 dt_2 d\Delta y dy_c} &= \frac{1}{N_{\text{gap}}(s)} \left[ \prod_i \left[ \frac{\beta^2(t_i)}{16\pi} e^{2[\alpha(t_i)-1]\Delta y_i} \right] \right] \cdot \kappa \left\{ \kappa \beta^2(0) \left( \frac{s'}{s_0} \right)^\epsilon \right\} \end{aligned}$$

$$\beta^2(t) = \beta^2(0) F^2(t)$$

$$F^2(t) = \left[ \frac{4m_p^2 - 2.8t}{4m_p^2 - t} \left( \frac{1}{1 - \frac{t}{0.71}} \right)^2 \right]^2 \approx a_1 e^{b_1 t} + a_2 e^{b_2 t}$$

$$\alpha_1=0.9, \alpha_2=0.1, b_1=4.6 \text{ GeV}^{-2}, b_2=0.6 \text{ GeV}^{-2}, s'=s e^{-\Delta y}, \kappa=0.17, \kappa\beta^2(0)=\sigma_0, s_0=1 \text{ GeV}^2, \sigma_0=2.82 \text{ mb or } 7.25 \text{ GeV}^{-2}$$

# Total, elastic, and inelastic x-sections

$$\sigma_{\text{ND}} = (\sigma_{\text{tot}} - \sigma_{\text{el}}) - (2\sigma_{\text{SD}} + \sigma_{\text{DD}} + \sigma_{\text{CD}})$$

**CMG**

R. J. M. Covolan, K. Goulios, J. Montanha, Phys. Lett. B **389**, 176 (1996)

$$\sigma_{\text{tot}}^{p\pm p} = \begin{cases} 16.79s^{0.104} + 60.81s^{-0.32} \mp 31.68s^{-0.54} & \text{for } \sqrt{s} < 1.8 \\ \sigma_{\text{tot}}^{\text{CDF}} + \frac{\pi}{s_0} \left[ \left( \ln \frac{s}{s_F} \right)^2 - \left( \ln \frac{s^{\text{CDF}}}{s_F} \right)^2 \right] & \text{for } \sqrt{s} \geq 1.8 \end{cases}$$

KG Moriond 2011, arXiv:1105.1916

$$\sqrt{s^{\text{CDF}}} = 1.8 \text{ TeV}, \sigma_{\text{tot}}^{\text{CDF}} = 80.03 \pm 2.24 \text{ mb}$$

$$\sqrt{s_F} = 22 \text{ GeV} \quad s_0 = 3.7 \pm 1.5 \text{ GeV}^2$$

$$\sigma_{\text{el}}^{p\pm p} = \sigma_{\text{tot}} \times (\sigma_{\text{el}}/\sigma_{\text{tot}}), \text{ with } \sigma_{\text{el}}/\sigma_{\text{tot}} \text{ from CMG}$$

small extrapol. from 1.8 to 7 and up to 50 TeV )

# Diffractive and Total pp Cross Sections at LHC



Konstantin Goulios  
The Rockefeller University



- Use the Froissart formula as a *saturated* cross section

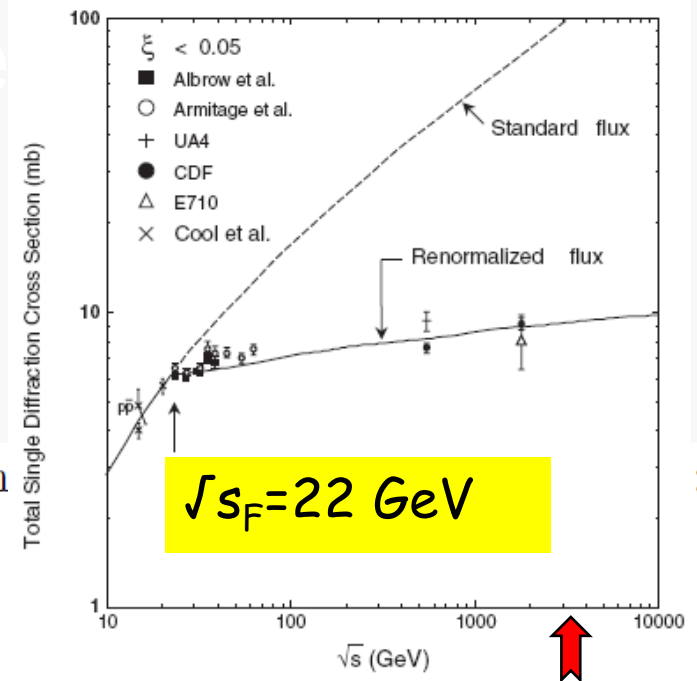
$$\sigma_t(s > s_F) = \sigma_t(s_F) + \frac{\pi}{m^2} \cdot \ln^2 \frac{s}{s_F}$$

- This formula should be valid above the *knee* in  $\sigma_{sd}$  vs.  $\sqrt{s}$  at  $\sqrt{s}_F = 22$  GeV (Fig. 1) and therefore valid at  $\sqrt{s} = 1800$  GeV.
- Use  $m^2 = s_0$  in the Froissart formula multiplied by  $1/0.389$  to convert it to  $\text{mb}^{-1}$ .
- Note that contributions from Reggeon exchanges at  $\sqrt{s} = 1800$  GeV are negligible, as can be verified from the global fit of Ref. [7].
- Obtain the total cross section at the LHC:

$$\sigma_t^{\text{LHC}} = \sigma_t^{\text{CDF}} + \frac{\pi}{s_0} \cdot \left( \ln^2 \frac{s^{\text{LHC}}}{s_F} - \ln^2 \frac{s^{\text{CDF}}}{s_F} \right)$$

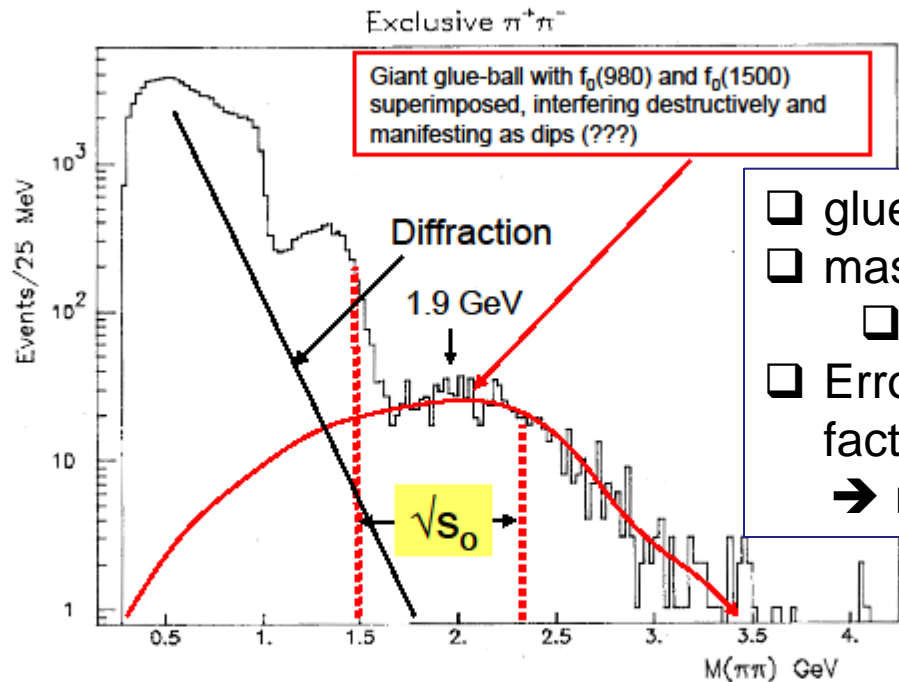
**$98 \pm 8$  mb at 7 TeV  
 $109 \pm 12$  mb at 14 TeV**

Main error from  $s_0$



# Reduce the uncertainty in $s_0$

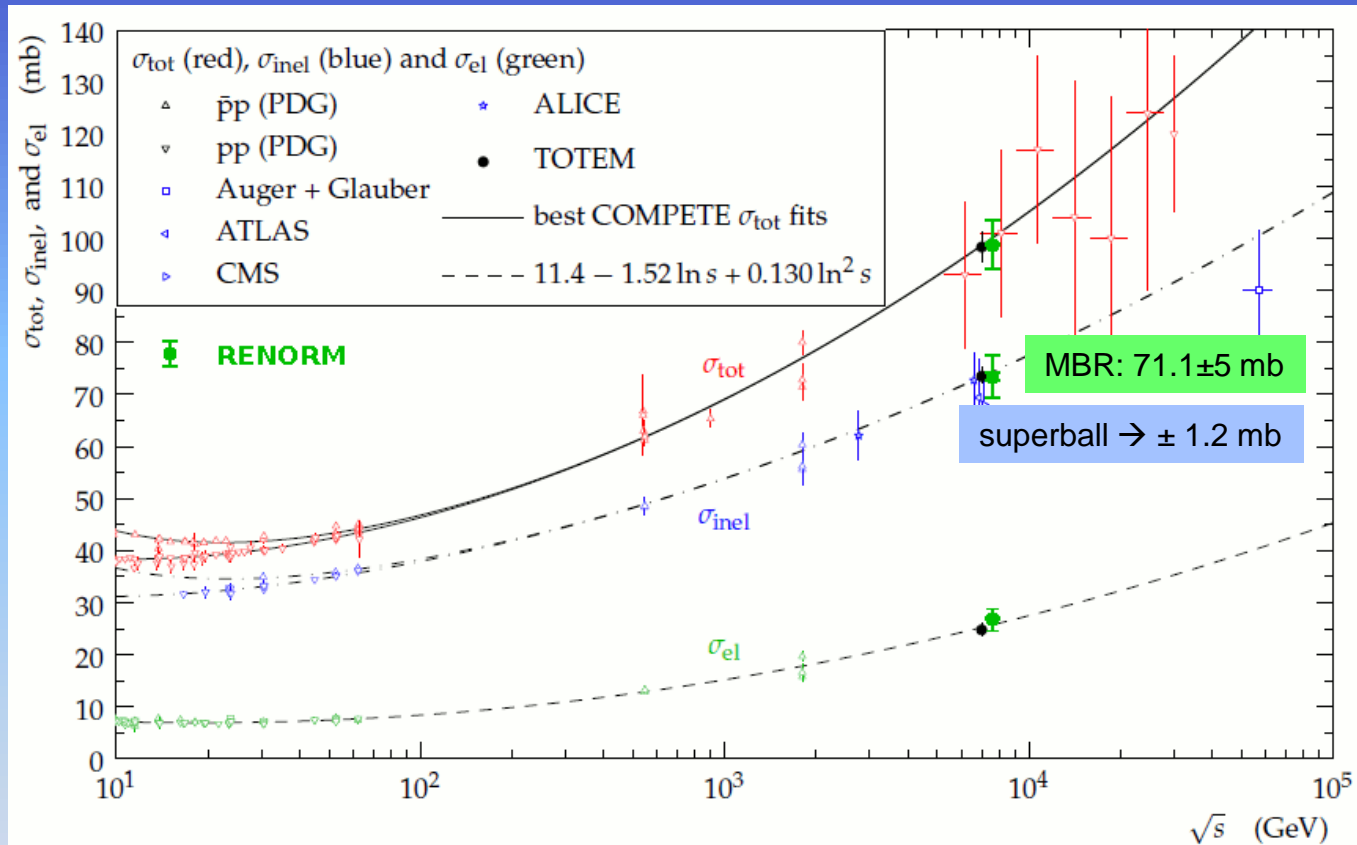
## Saturation glueball?



- ❑ glue-ball-like object → “superball”
- ❑ mass → 1.9 GeV →  $m_s^2 = 3.7$  GeV
  - ❑ agrees with RENORM  $s_0 = 3.7$
- ❑ Error in  $s_0$  can be reduced by factor  $\sim 4$  from a fit to these data!
  - ➔ reduces error in  $\sigma_t$ .

Figure 8:  $M_{\pi^+\pi^-}$  spectrum in *DPE* at the ISR (Axial Field Spectrometer, R807 [97, 98]). Figure from Ref. [98]. See M.G.Albrow, T.D. Goughlin, J.R. Forshaw, [hep-ph>arXiv:1006.1289](https://arxiv.org/abs/hep-ph/1006.1289)

# TOTEM vs PYTHIA8-MBR



$$\sigma_{\text{inrl}}^{7 \text{ TeV}} = 72.9 \pm 1.5 \text{ mb}$$

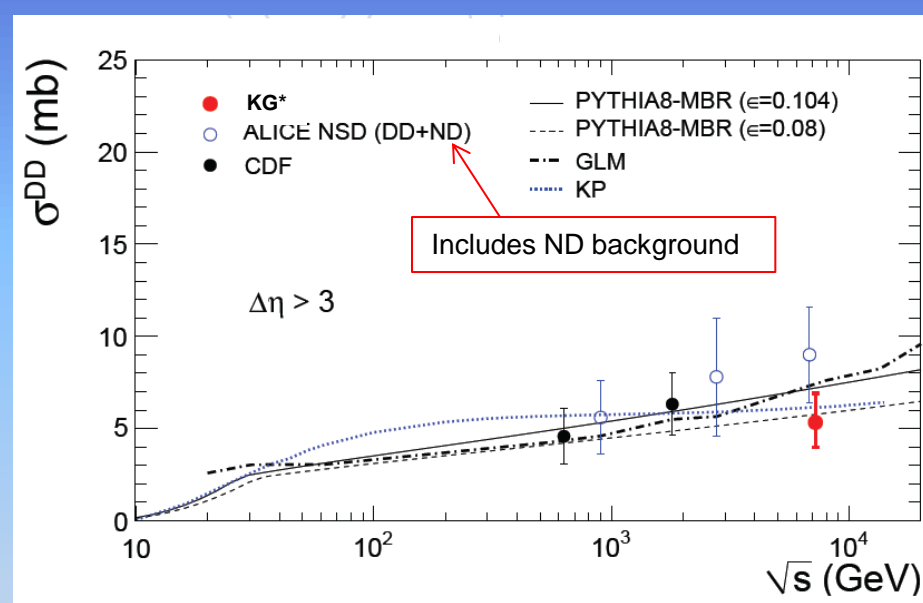
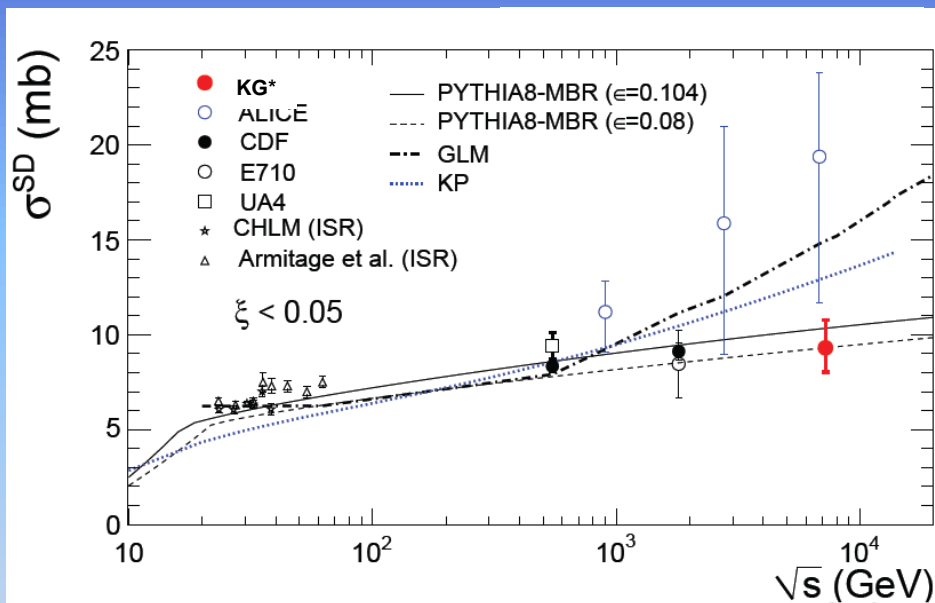
$$\sigma_{\text{inrl}}^{8 \text{ TeV}} = 74.7 \pm 1.7 \text{ mb}$$

*TOTEM, G. Latino talk at MPI@LHC, CERN 2012*

$$\text{RENORM: } 71.1 \pm 1.2 \text{ mb}$$

$$\text{RENORM: } 72.3 \pm 1.2 \text{ mb}$$

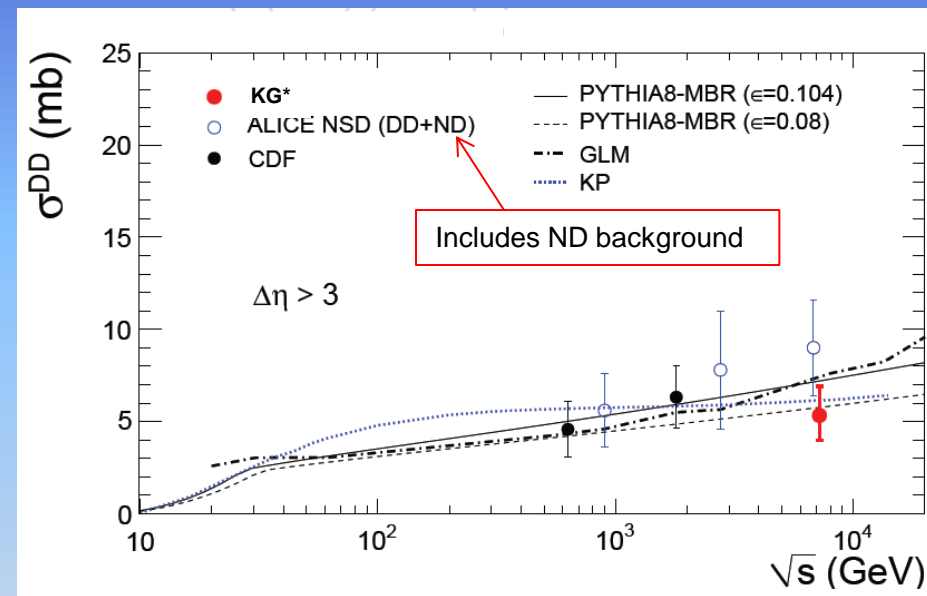
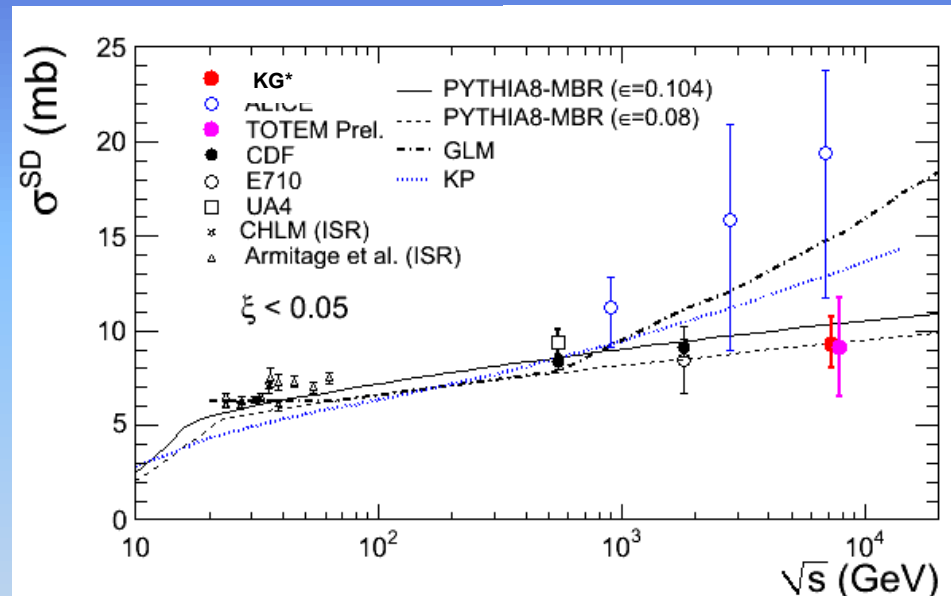
# CMS SD and DD x-sections vs ALICE: measurements and theory models



□ KG\*: after extrapolation into low  $\xi$  from measured CMS data using the MBR model:  
 find details on data in Benoit Roland's talk on Sunday at 09:05.

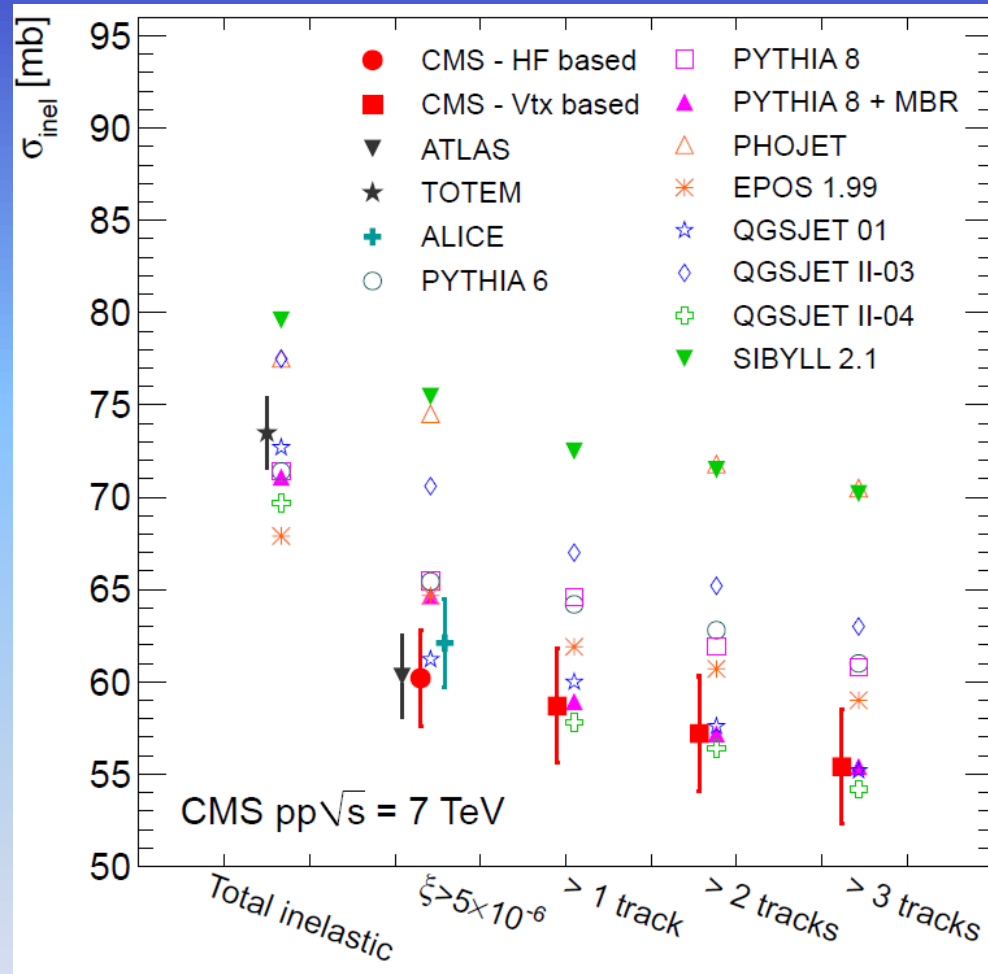


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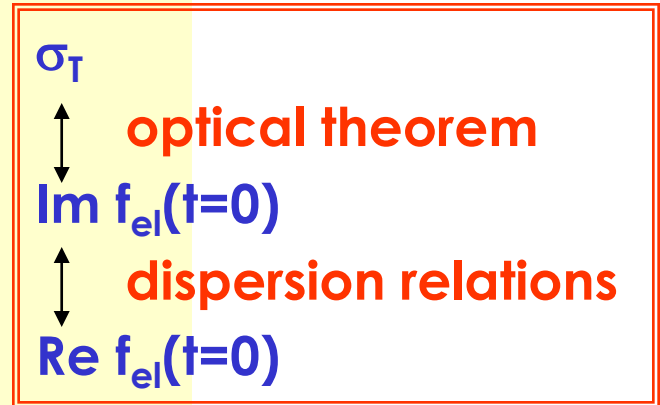
# Total-Inelastic Cross Sections vs model predictions



# Monte Carlo Strategy for the LHC ...

## MONTE CARLO STRATEGY

- $\sigma_{\text{tot}} \rightarrow$  from SUPERBALL model
- optical theorem  $\rightarrow \text{Im } f_{\text{el}}(t=0)$
- dispersion relations  $\rightarrow \text{Re } f_{\text{el}}(t=0)$
- $\sigma_{\text{el}} \leftarrow$  using global fit
- $\sigma_{\text{inel}} = \sigma_{\text{tot}} - \sigma_{\text{el}}$
- differential  $\sigma_{\text{SD}} \rightarrow$  from RENORM
- use *nesting* of final states for  $pp$  collisions at the  $P$ - $p$  sub-energy  $\sqrt{s}'$

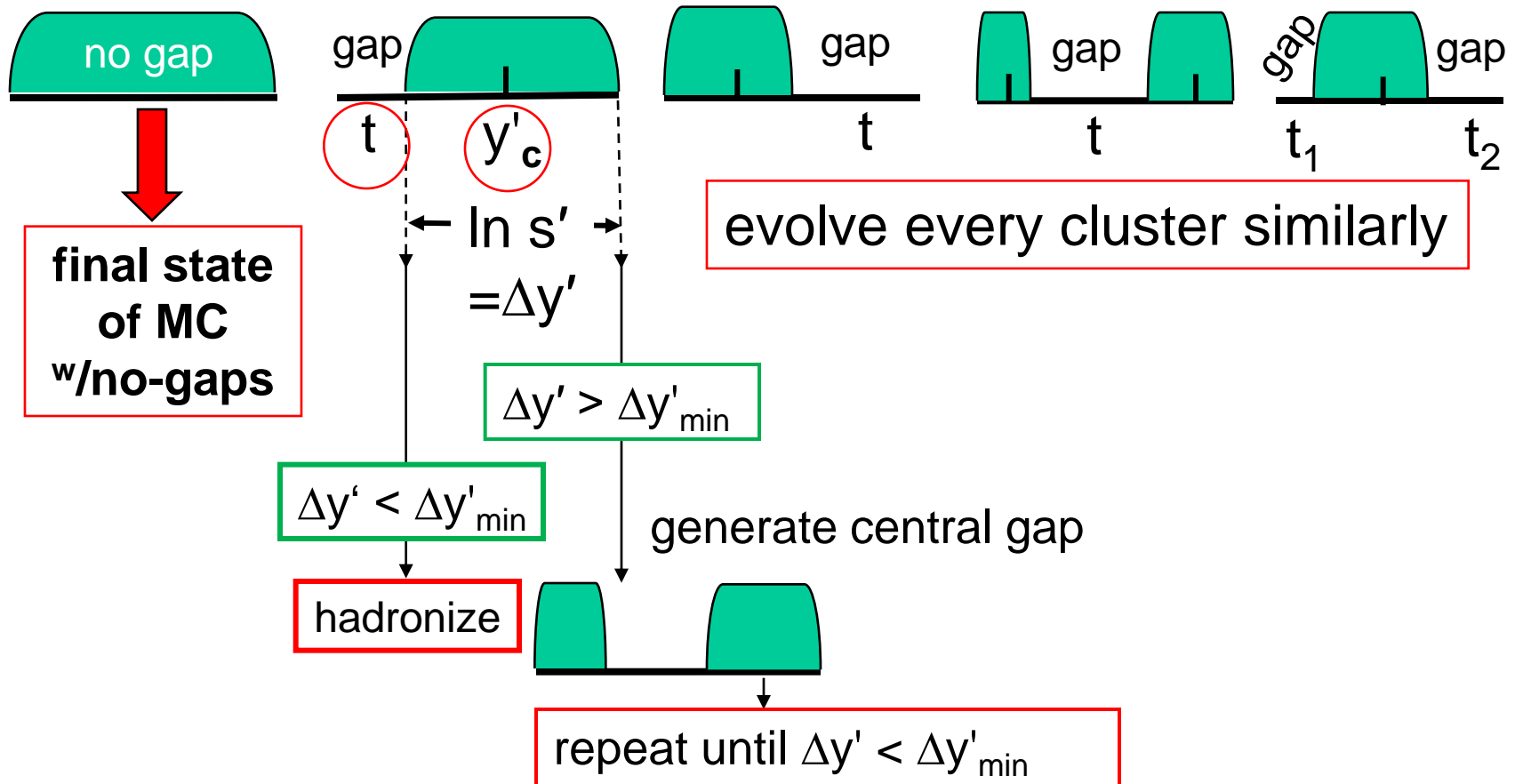


*Strategy similar to that of MBR used in CDF based on multiplicities from:*  
*K. Goulios, Phys. Lett. B 193 (1987) 151 pp*

*“A new statistical description of hadronic and  $e^+e^-$  multiplicity distributions”*

# Monte Carlo algorithm - nesting

## Profile of a $pp$ inelastic collision



# SUMMARY

- Introduction

- Diffractive cross sections:

- basic: SD1, SD2, DD, CD (DPE)
  - combined: multigap x-sections
- } **derived from ND and QCD color factors**
- ND → no diffractive gaps:

- ❖ **this is the only final state to be tuned**

- Total, elastic, and total inelastic cross sections

- Monte Carlo strategy for the LHC – “nesting”

*Thank you for your attention*