



# Diffraction at CDF and cross sections at the LHC

K. Goulianos

The University  
of Manchester

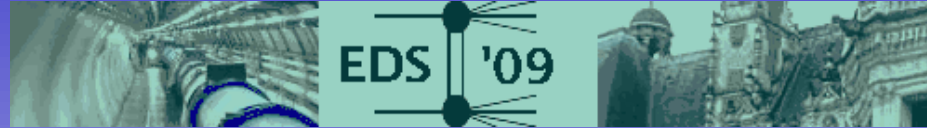


Forward Physics At The LHC  
9-12 Dec 2009



# ...some recent references

Presented @



CERN, 29th June - 3rd July 2009

- Factorization Breaking in Diffraction  
[http://physics.rockefeller.edu/dino/myhtml/talks/goulios\\_konstantin\\_eds09\\_factorization.pdf](http://physics.rockefeller.edu/dino/myhtml/talks/goulios_konstantin_eds09_factorization.pdf)
- The Forward Detectors of CDF and D0  
[...goulios\\_konstantin\\_eds09\\_detectors.pdf](...goulios_konstantin_eds09_detectors.pdf)
- Diffractive and Total pp Cross Sections at LHC  
[...goulios\\_konstantin\\_eds09\\_sigma.pdf](...goulios_konstantin_eds09_sigma.pdf)
- What can we Learn / Expect on Elastic and Diffractive Scattering from the LHC Experiments? (discussion session - see K. Eggert's talk)  
[...goulios\\_konstantin\\_eds09\\_discussion.pdf](...goulios_konstantin_eds09_discussion.pdf)

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## 2 Diffraction at CDF: 17 PRLs / PRDs

<http://physics.rockefeller.edu/publications.html>

## 3 **Current data analyses**

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DSF in DPE.....	- final stage of analysis
Diffractive W/Z.....	- under internal review
Central gaps.....	- towards internal review

## 4 Cross sections at the LHC

# 1

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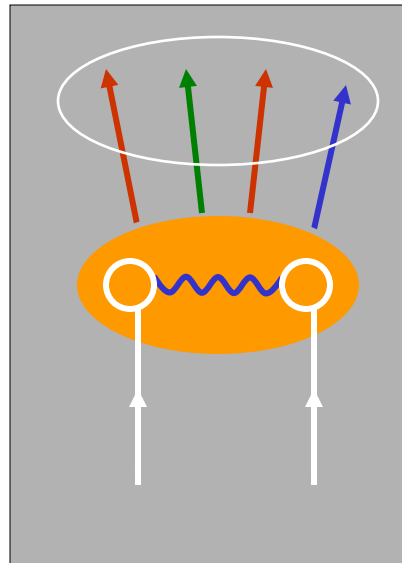
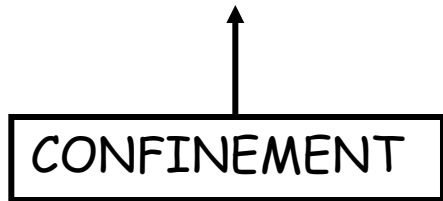
## 4 Cross sections at the LHC

# p-p Interactions

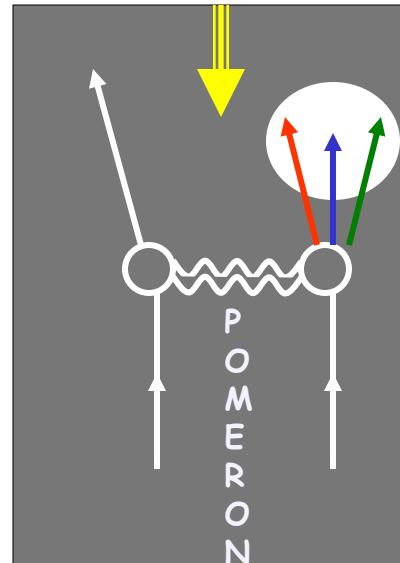
Non-diffractive:  
Color-exchange

Diffractive:  
Colorless exchange carrying  
vacuum quantum numbers

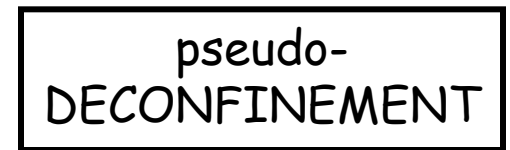
Incident hadrons  
acquire color  
and break apart



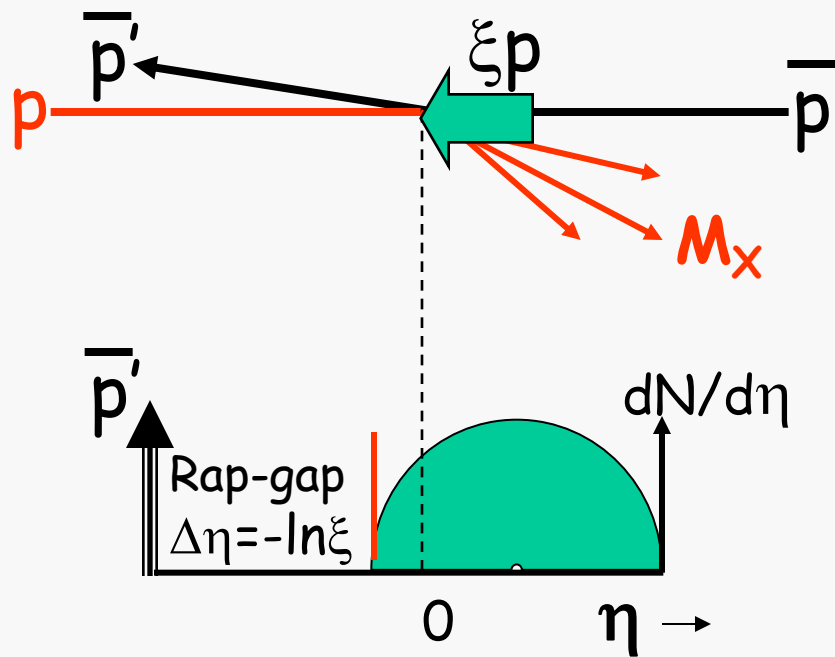
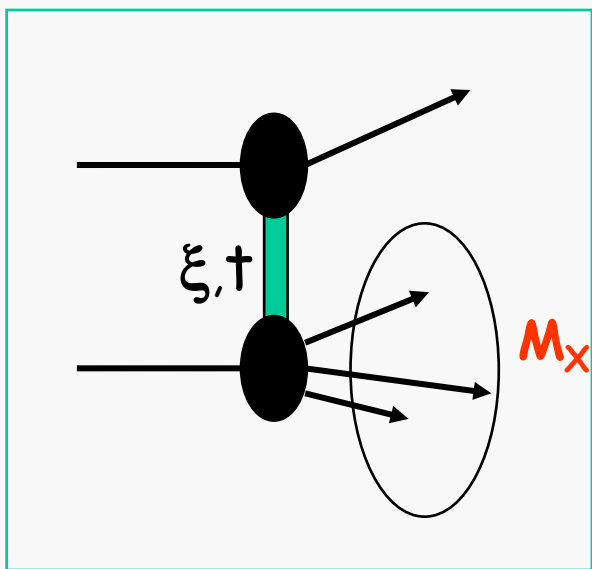
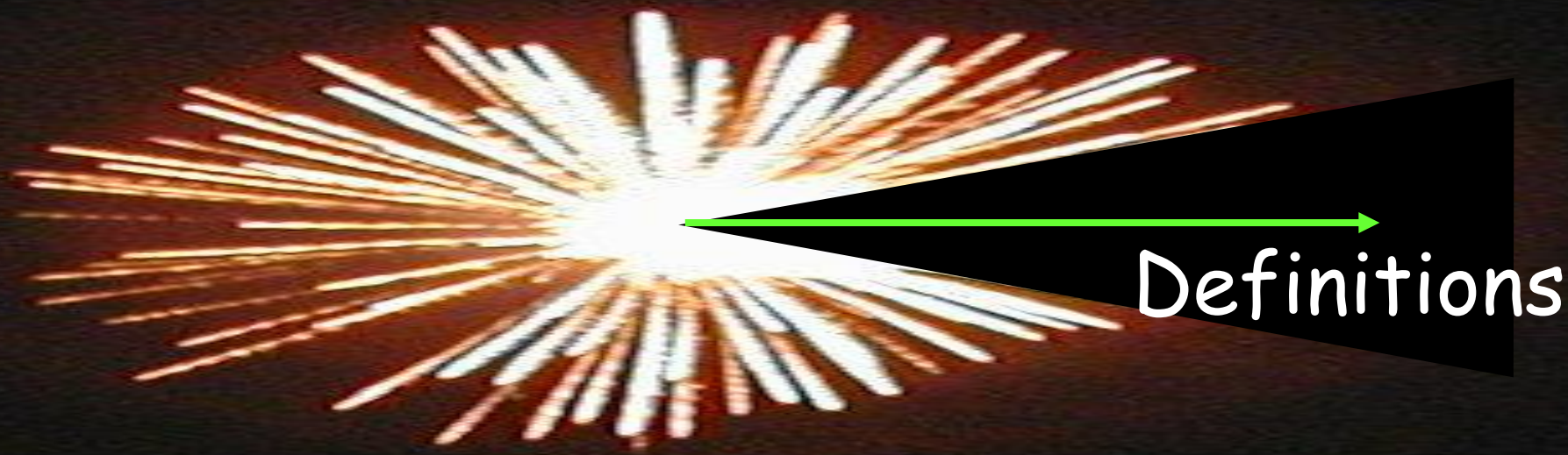
rapidity gap



Incident hadrons retain  
their quantum numbers  
remaining colorless

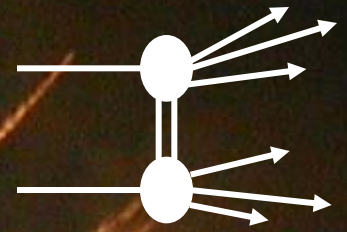


Goal: understand the QCD nature of the diffractive exchange





# Rapidity Gaps in Fireworks



# 2

1 Introduction

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3 **Current data analyses**

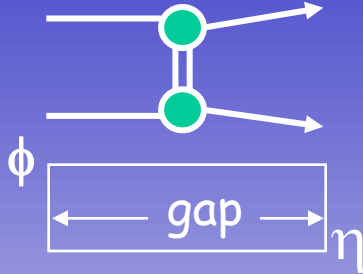
Diffraction dijet SF..	- under internal review
DSF in DPE.....	- final stage of analysis
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Central gaps.....	- towards internal review

4 Cross sections at the LHC



# Diffraction at CDF

Elastic scattering

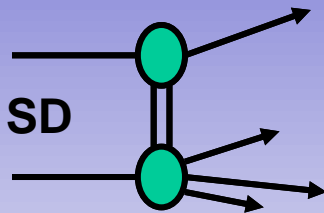
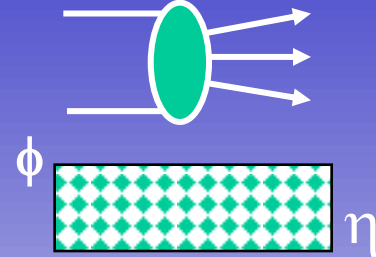


$\sigma_T = \text{Im } f_{el}(t=0)$

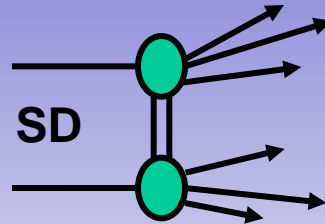
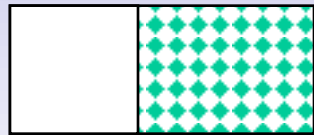


OPTICAL THEOREM

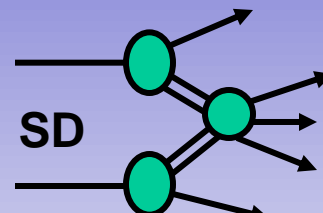
Total cross section



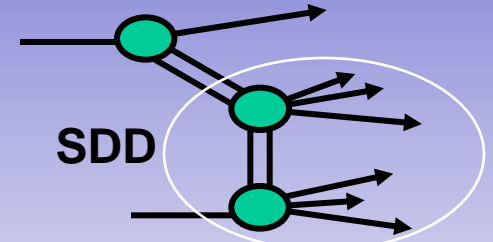
Single Diffraction dissociation (SD)



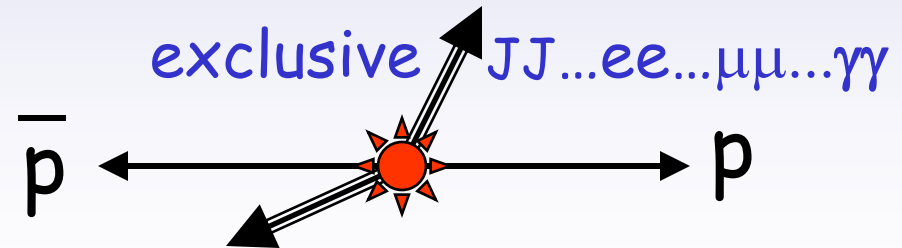
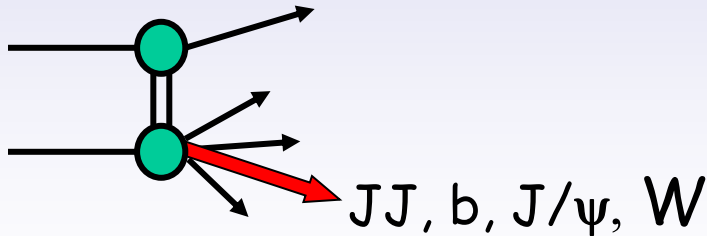
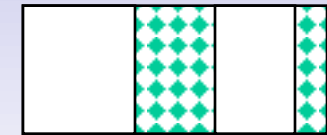
Double Diffraction dissociation (DD)



Double Pomeron Exchange (DPE)

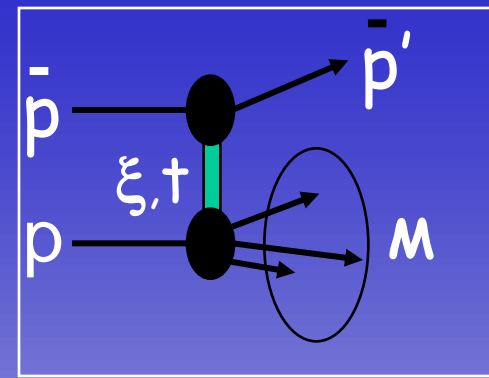


Single + Double Diffraction (SDD)

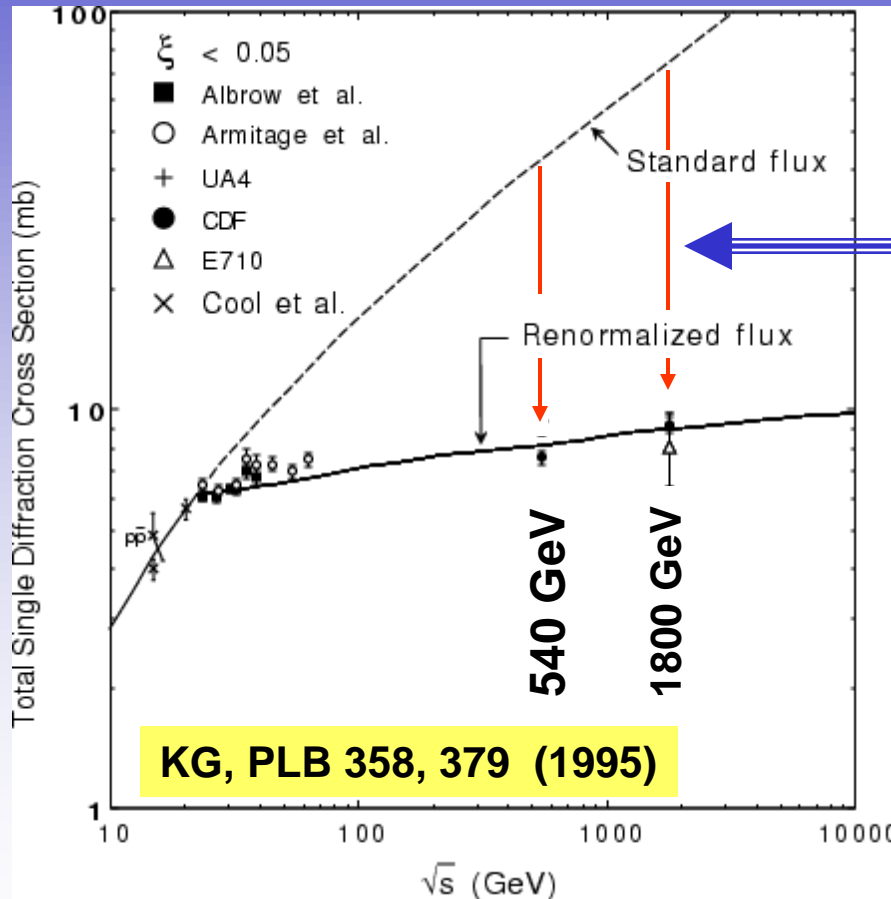


# $\sigma_{SD}^T$ ( $pp$ & $p\bar{p}$ )

→ suppressed relative to Regge prediction



$\sigma_{SD}^T$  mb



Factor of  $\sim 8$  ( $\sim 5$ )  
suppression at  
 $\sqrt{s} = 1800$  (540) GeV

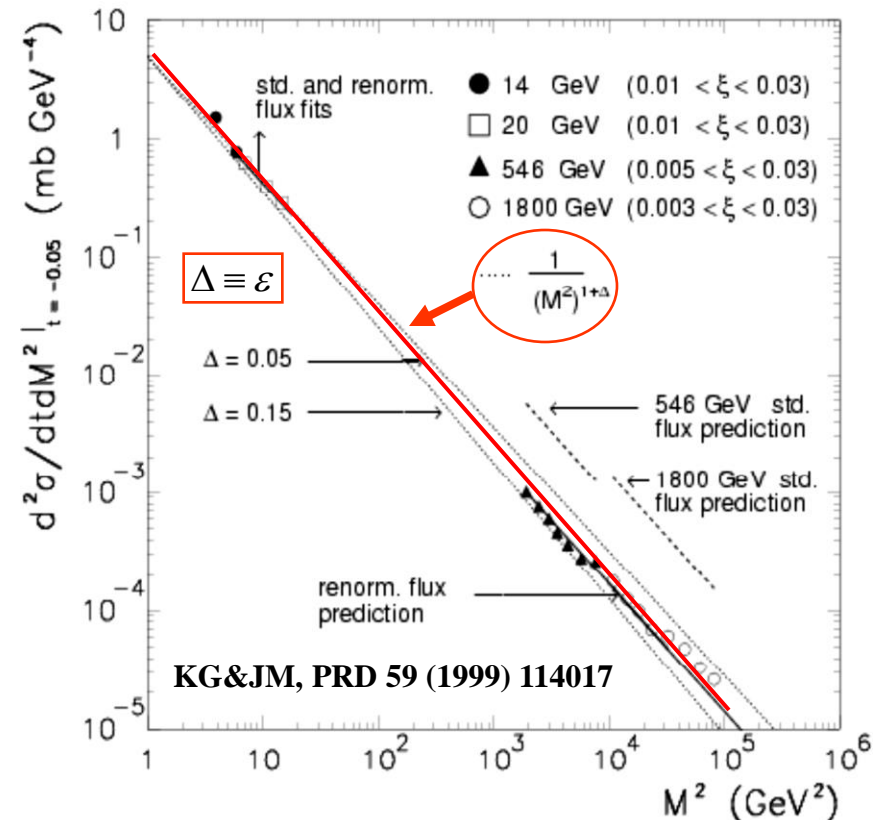
# $M^2$ scaling

→  $ds/dM^2$  independent of  $s$  over 6 orders of magnitude!

renormalization

$$\frac{d\sigma}{dM^2} \propto \frac{s^{2\varepsilon} \rightarrow 1}{(M^2)^{1+\varepsilon}}$$

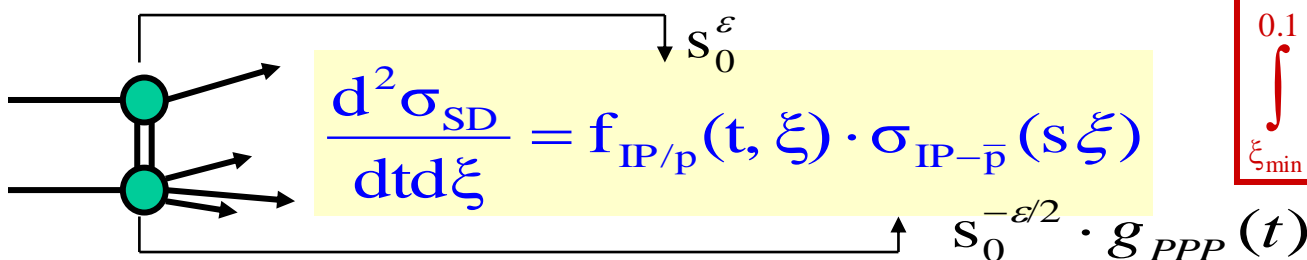
→ Independent of  $s$  over 6 orders of magnitude in  $M^2$ !



→ factorization breaks down to ensure  $M^2$  scaling!

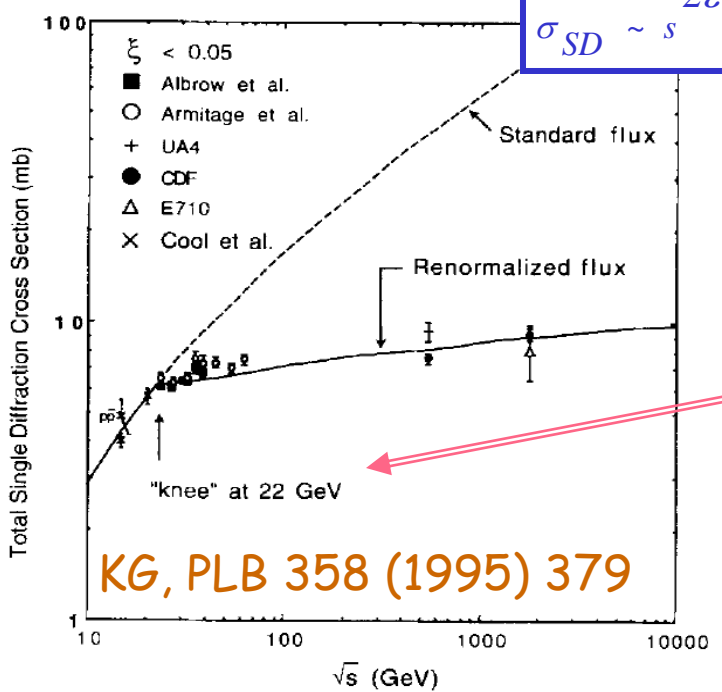
# Saturation / Single Diffraction

Pomeron flux



$$\int_{\xi_{\min}}^{0.1} \int_{t=-\infty}^0 f_{IP/p}(t, \xi) d\xi dt \Rightarrow 1$$

$$\sigma_{SD} \sim s^{2\epsilon}$$

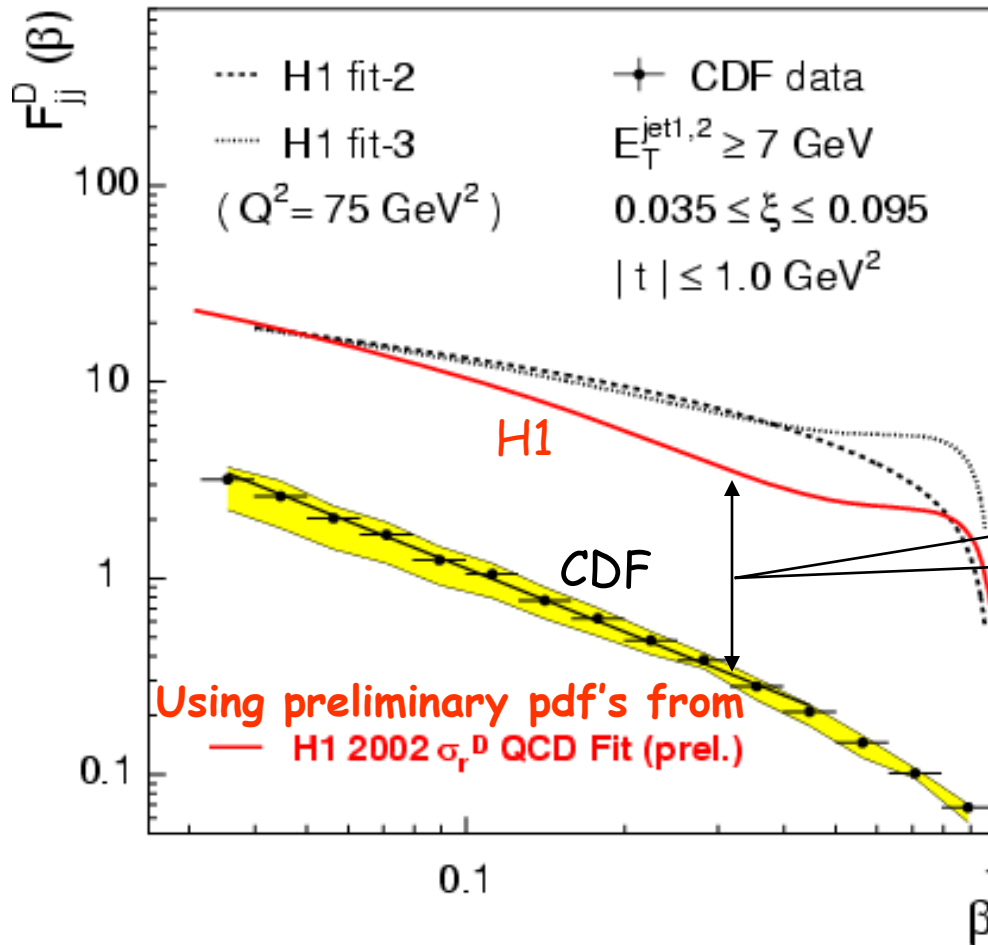


### Renormalization

- $\int_{\xi_{\min} \approx 1/s}^{\xi} \int_{t=-\infty}^0 f_{IP/p}(t, \xi) d\xi dt \approx C \cdot s^{2\epsilon} \cdot s_0^\epsilon \Rightarrow 1$
- Flux integral depends on s and s<sub>0</sub>
- "knee"  $\sqrt{s}$ -position determines s-value where flux becomes unity  $\rightarrow$  get s<sub>0</sub>
- get error in s<sub>0</sub> from error in  $\sqrt{s}$ -knee  
 $\delta s_0 / s_0 = -2 \delta s / s = -4 (\delta \sqrt{s}) / \sqrt{s}$

# Diffraction Structure Function (DSF)

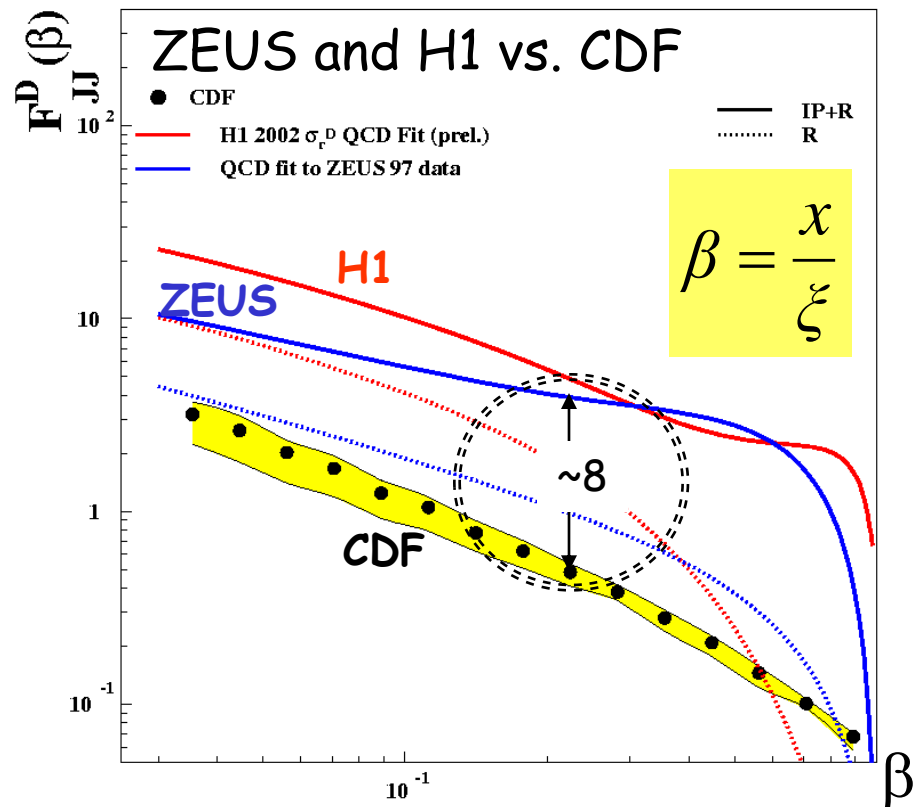
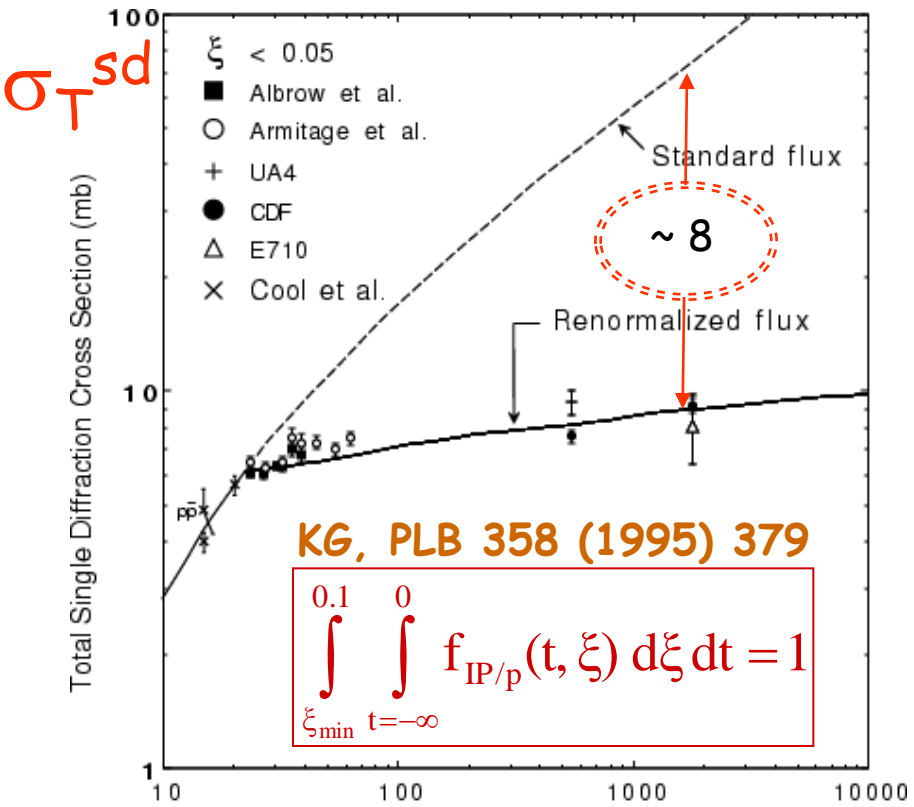
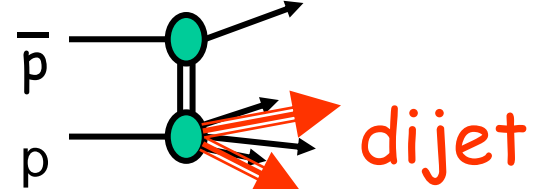
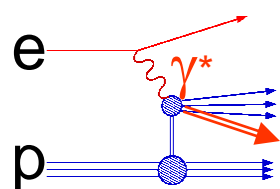
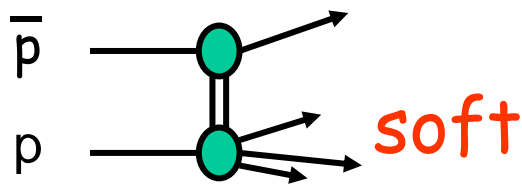
## Breakdown of QCD factorization



$$\bar{p}p \rightarrow \bar{p} + \text{dijet} + X$$



# $\sigma_{SD}^T$ and dijets



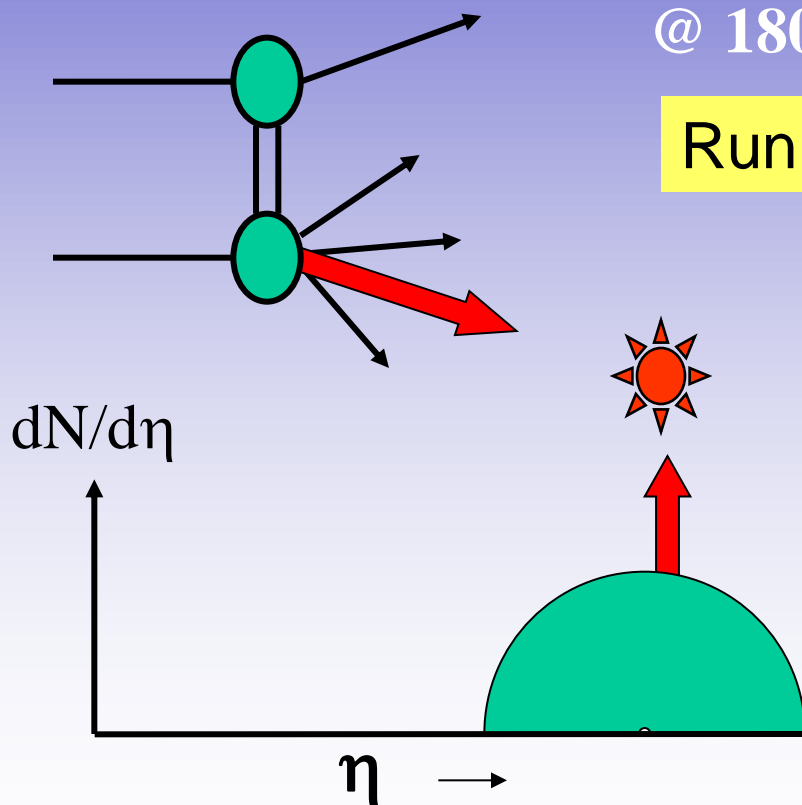
**Magnitude:** same suppression factor in soft and hard diffraction!  
**Shape of  $\beta$  distribution:** ZEUS, H1, and Tevatron - why different slapes?


# Hard diffractive fractions

$$\bar{p}p \rightarrow (\odot + X) + \text{gap}$$

Fraction: SD/ND  
@ 1800 GeV

Run I



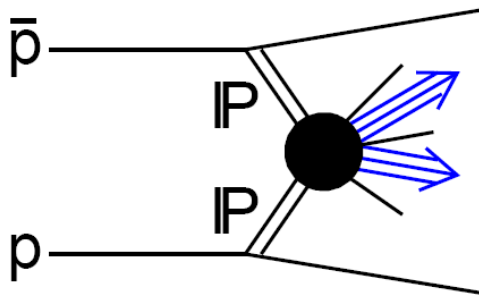
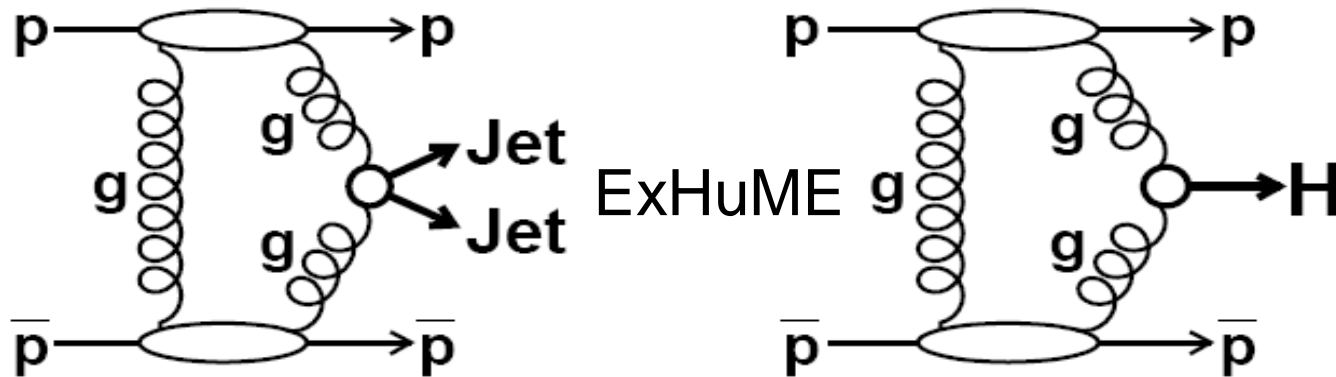
	Fraction (%)
JJ	0.75 +/- 0.10
W	0.115 +/- 0.55
b	0.62 +/- 0.25
J/ψ	1.45 +/- 0.25

All fractions ~ 1%  
(differences due to kinematics)

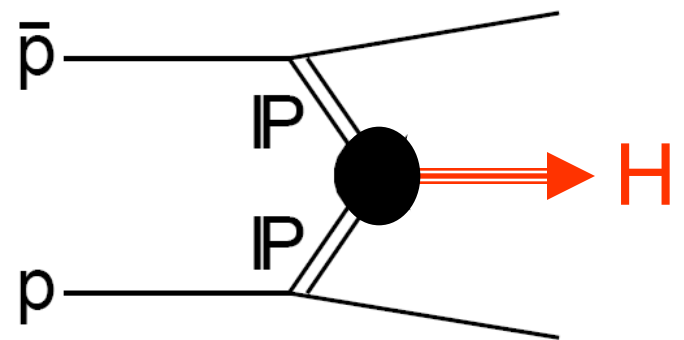
- ~ uniform suppression
- ~ **FACTORIZATION !**

# Exclusive Dijet and Higgs Production

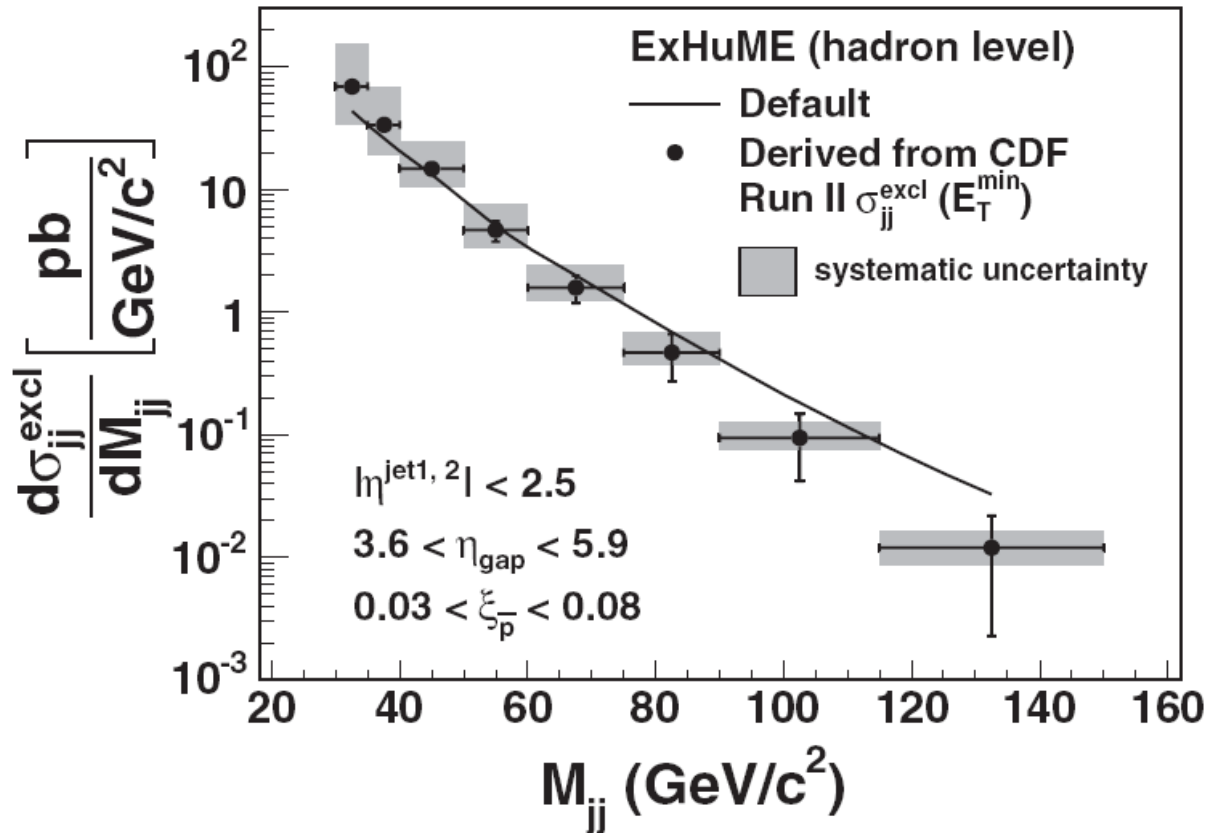
Phys. Rev. D 77, 052004



DPEMC



# Exclusive Dijet x-section vs. $M_{jj}$



line: ExHuME hadron-level exclusive di-jet cross section vs. di-jet mass  
points: derived from CDF excl. di-jet x-sections using ExHuME

Stat. and syst. errors are propagated from measured cross section uncertainties using  $M_{jj}$  distribution shapes of ExHuME generated data.

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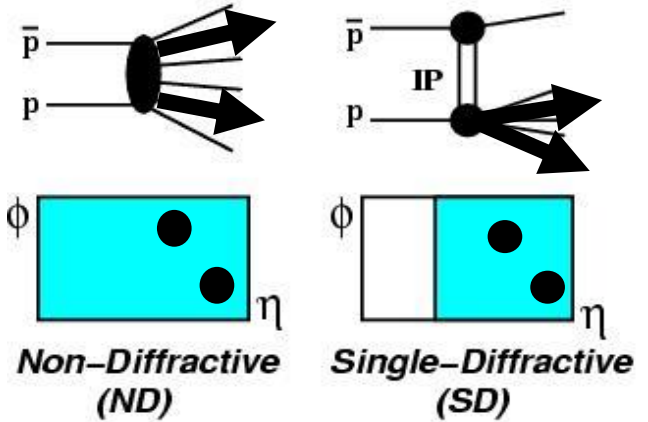
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4 Cross sections at the LHC

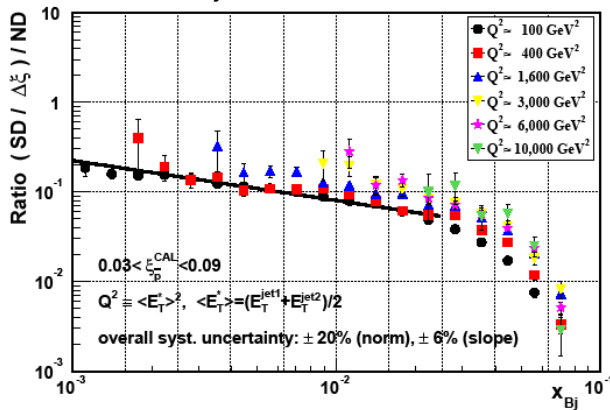


# DSF from Dijets in Run II

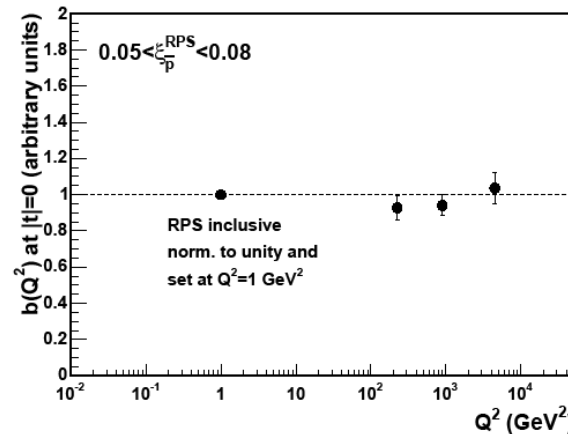


$$R(x_{Bj}) \equiv \frac{\text{Rate}_{jj}^{\text{SD}}(x_{Bj})}{\text{Rate}_{jj}^{\text{ND}}(x_{Bj})} \Rightarrow \frac{F_{jj}^{\text{SD}}(x_{Bj})}{F_{jj}^{\text{ND}}(x_{Bj})}$$

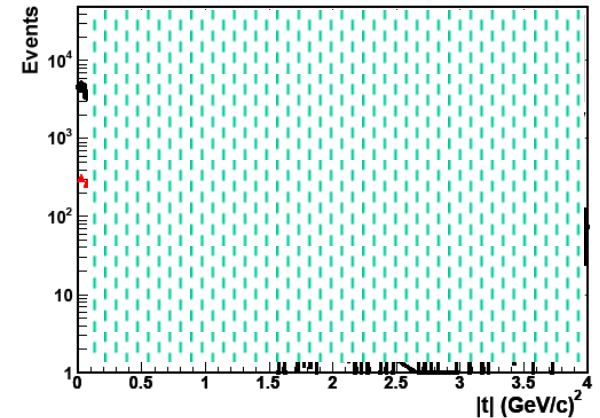
$x_{Bj}$  - distribution



b - slope of t-distribution



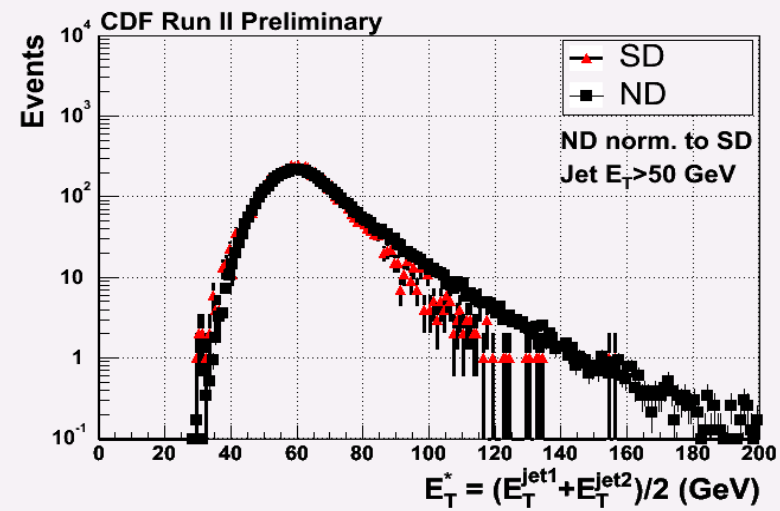
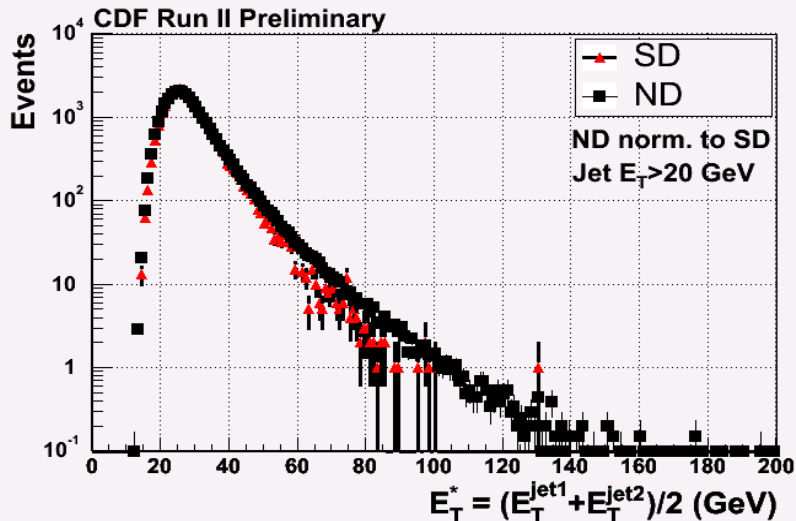
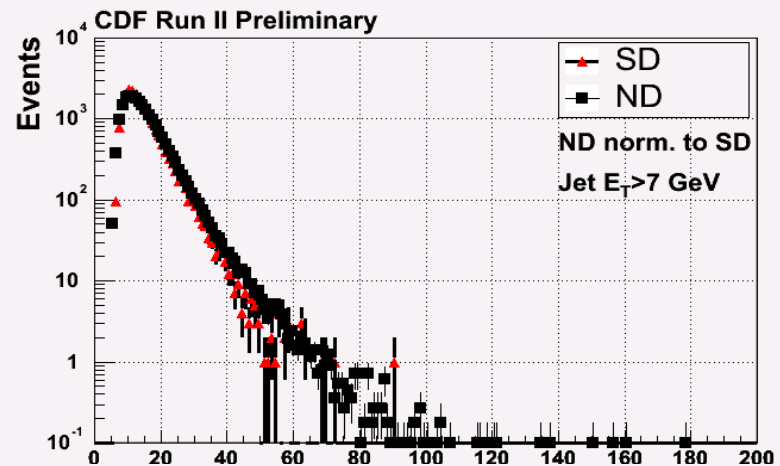
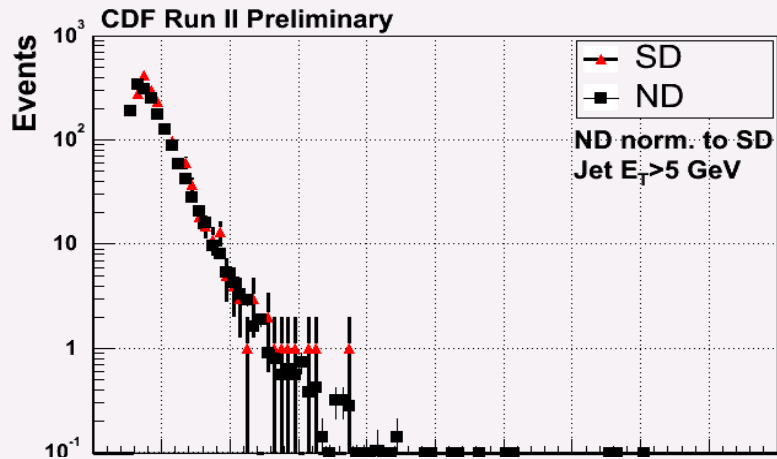
t - distribution



- The  $x_{Bj}$ -distribution of the SD/ND ratio has no strong  $Q^2$  dependence
- the slope of the t-distribution is independent of  $Q^2$
- the t-distribution displays a diffraction minimum

➤ all three results → “**first observation**”

# Dijets - $E_T$ distributions

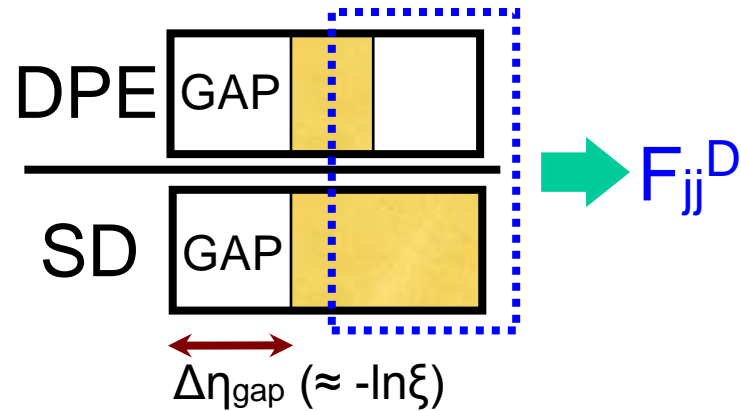


→ similar for SD and ND over 4 orders of magnitude

↑ Kinematics

# DSF from Dijets in DPE

Does QCD factorization hold for the formation of the 2nd gap?

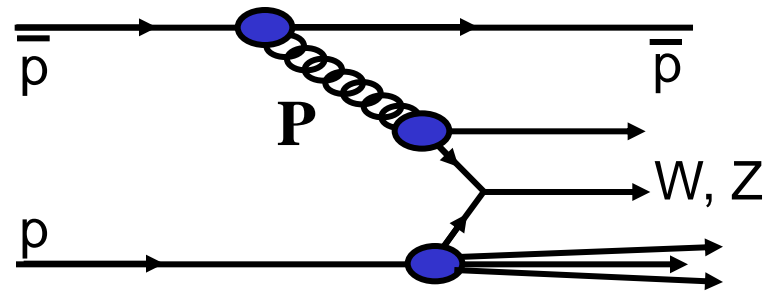


stay tuned...

# Diffractive W/Z Production

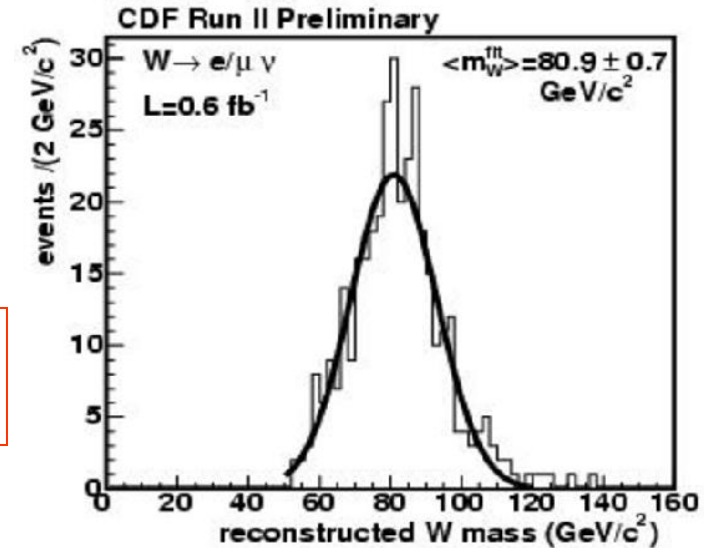
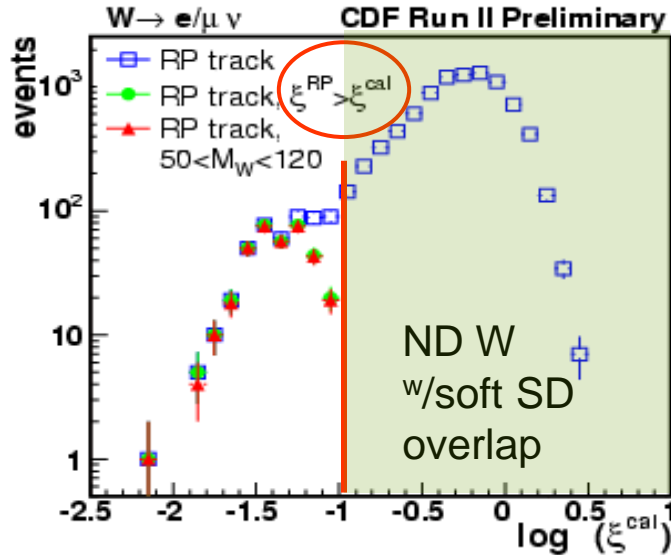
- probes the quark content of the Pomeron

➤ use CAL and Roman pots to get  $\eta_v$



$$\xi^{\text{cal}} = \sum_{\text{towers}} \frac{E_T}{\sqrt{s}} e^{-\eta}$$

$$\xi^{\text{RPS}} - \xi^{\text{cal}} = \frac{E_T}{\sqrt{s}} e^{-\eta_v}$$



CDF (press release 2007):  $80,413 \pm 48 \text{ MeV}/c^2$

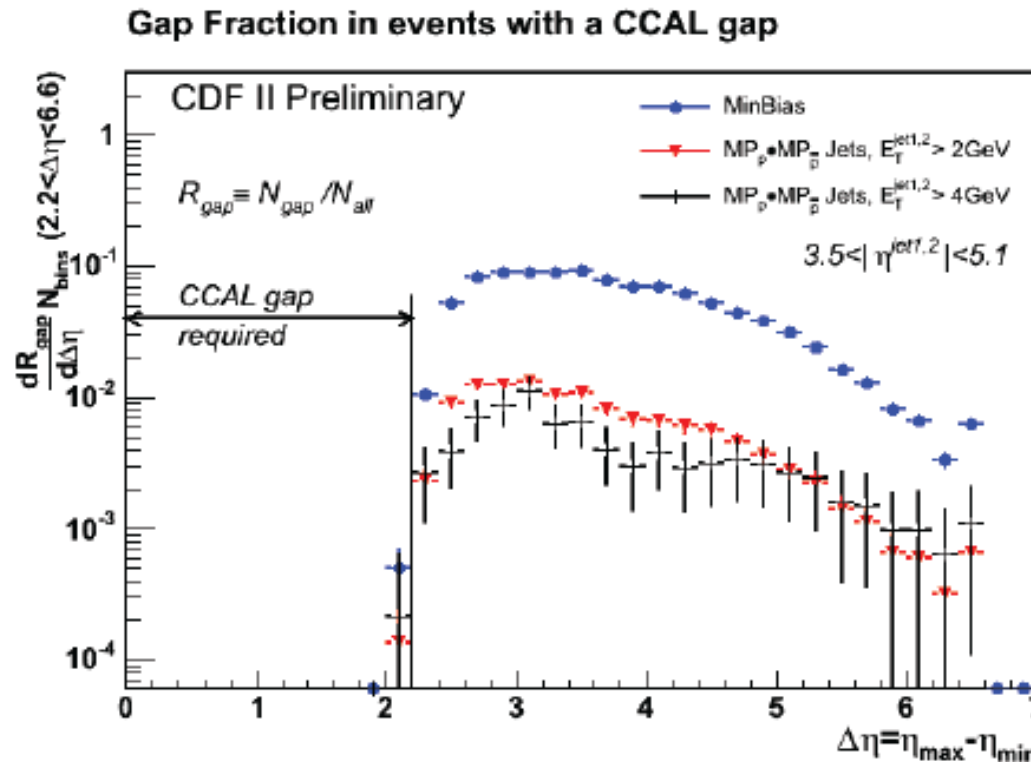
## RESULTS

$$R^W (0.03 < \xi < 0.10, |t| < 1) = [0.97 \pm 0.05(\text{stat}) \pm 0.11(\text{syst})]\%$$

Run I:  $R^W = 1.15 \pm 0.55\%$  ( $\xi < 0.1$ )  $\rightarrow$  estimate  $0.97 \pm 0.47\%$  ( $0.03 < \xi < 0.10$  &  $|t| < 1$ )

$$R^Z (0.03 < \xi < 0.10, |t| < 1) = [0.85 \pm 0.20(\text{stat}) \pm 0.11(\text{syst})]\%$$

# Central gaps



Jet gap Jet

The distribution of the gap fraction  $R_{\text{gap}} = N_{\text{gap}} / N_{\text{all}}$  vs  $\Delta\eta$  for MinBias ( $CLC_p \bullet CLC_{pbar}$ ) and MiniPlug jet events ( $MP_p \bullet MP_{pbar}$ ) of  $E_{T(\text{jet},2)} > 2 \text{ GeV}$  and  $E_{T(\text{jet},2)} > 4 \text{ GeV}$ .

**The distributions are similar in shape within the uncertainties.**



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4 Cross sections at the LHC

# ...some references

<http://physics.rockefeller.edu/dino/my.html>

CDF PRD 50, 5518 (1994)  $\sigma^{\text{el}}$  @ 1800 & 546 GeV

CDF PRD 50, 5535 (1994)  $\sigma^{\text{D}}$  @ 1800 & 546 GeV

CDF PRD 50, 5550 (1994)  $\sigma^{\text{T}}$  @ 1800 & 546 GeV

KG-PR Physics Reports 101, No.3 (1983) 169-219

Diffraction interactions of hadrons at high energies

KG-95 PLB 358, 379 (1995); Erratum: PLB 363, 268 (1995)

Renormalization of hadronic diffraction

CMG-96 PLB 389, 176 (1996)

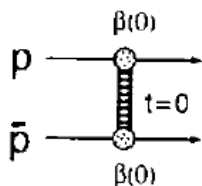
Global fit to  $p^{\pm}p$ ,  $\pi^{\pm}$  and  $K^{\pm}p$  cross sections

KG-09 arXiv:0812.4464v2 [hep-ph] 26 March 2009

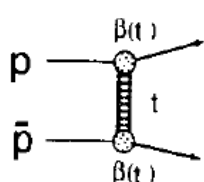
Pomeron intercept and slope: the QCD connection

# Standard Regge Theory

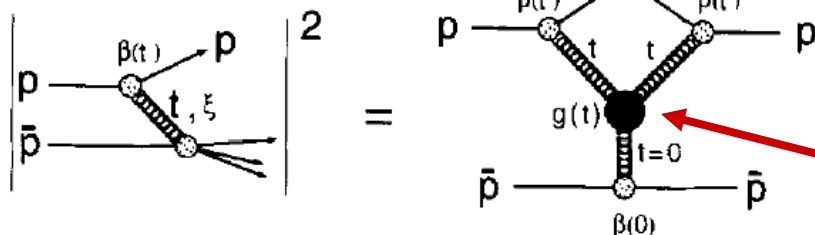
TOTAL CROSS SECTION



ELASTIC SCATTERING



SINGLE DIFFRACTION DISSOCIATION



(KG-95)

$$\sigma_T = \beta_1(0)\beta_2(0) \left(\frac{s}{s_0}\right)^{\alpha(0)-1} = \sigma_0^{p\bar{p}} \left(\frac{s}{s_0}\right)^\epsilon \quad (1)$$

$$\begin{aligned} \frac{d\sigma_{el}}{dt} &= \frac{\beta_1^2(t)\beta_2^2(t)}{16\pi} \left(\frac{s}{s_0}\right)^{2[\alpha(t)-1]} \\ &= \frac{\sigma_T^2}{16\pi} \left(\frac{s}{s_0}\right)^{2\alpha't} F^4(t) \approx \frac{\sigma_T^2}{16\pi} e^{b_{el}(s)t} \end{aligned} \quad (2)$$

$$F^4(t) \approx e^{b_{0,el}t} \Rightarrow b_{el}(s) = b_{0,el} + 2\alpha' \ln \left(\frac{s}{s_0}\right) \quad (3)$$

$$\frac{d^2\sigma_{sd}}{dt d\xi}$$

$$\begin{aligned} &= \frac{\beta_1^2(t)}{16\pi} \xi^{1-2\alpha(t)} \left[ \beta_2(0) g(t) \left(\frac{s'}{s'_0}\right)^{\alpha(0)-1} \right] \\ &= f_{p/p}(\xi, t) \sigma_T^{p\bar{p}}(s', t) \end{aligned} \quad (4)$$

Parameters:

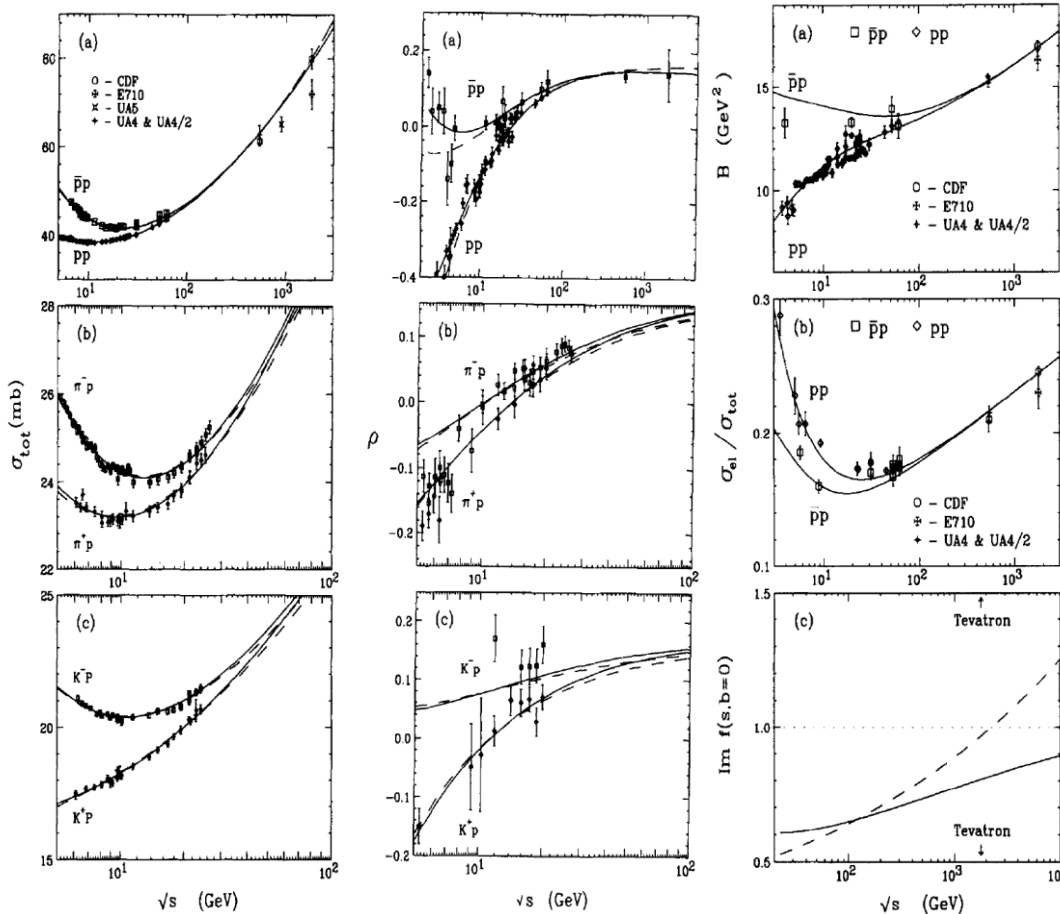
- ❑  $s_0, s'_0$  and  $g(t)$
- ❑ set  $s'_0 = s_0$  (universal IP)
- ❑  $g(t) \rightarrow g(0) \equiv g_{ppp}$  see KG-PR
- ❑ determine  $s_0$  and  $g_{ppp}$  – how?

# Global fit to $p^\pm p$ , $\pi^\pm$ , $K^\pm p$ x-sections

CMG-96 →

A new determination of the soft pomeron intercept

R.J.M. Covolan<sup>1</sup>, J. Montanha<sup>2</sup>, K. Goulios<sup>3</sup>



Use standard Regge theory

INPUT

$$\alpha_{f/a} = 0.68 + 0.82 t$$

$$\alpha_{\omega/\rho} = 0.46 + 0.92 t$$

$$\alpha'_{\mathbf{P}} = 0.25 \text{ GeV}^{-2}$$

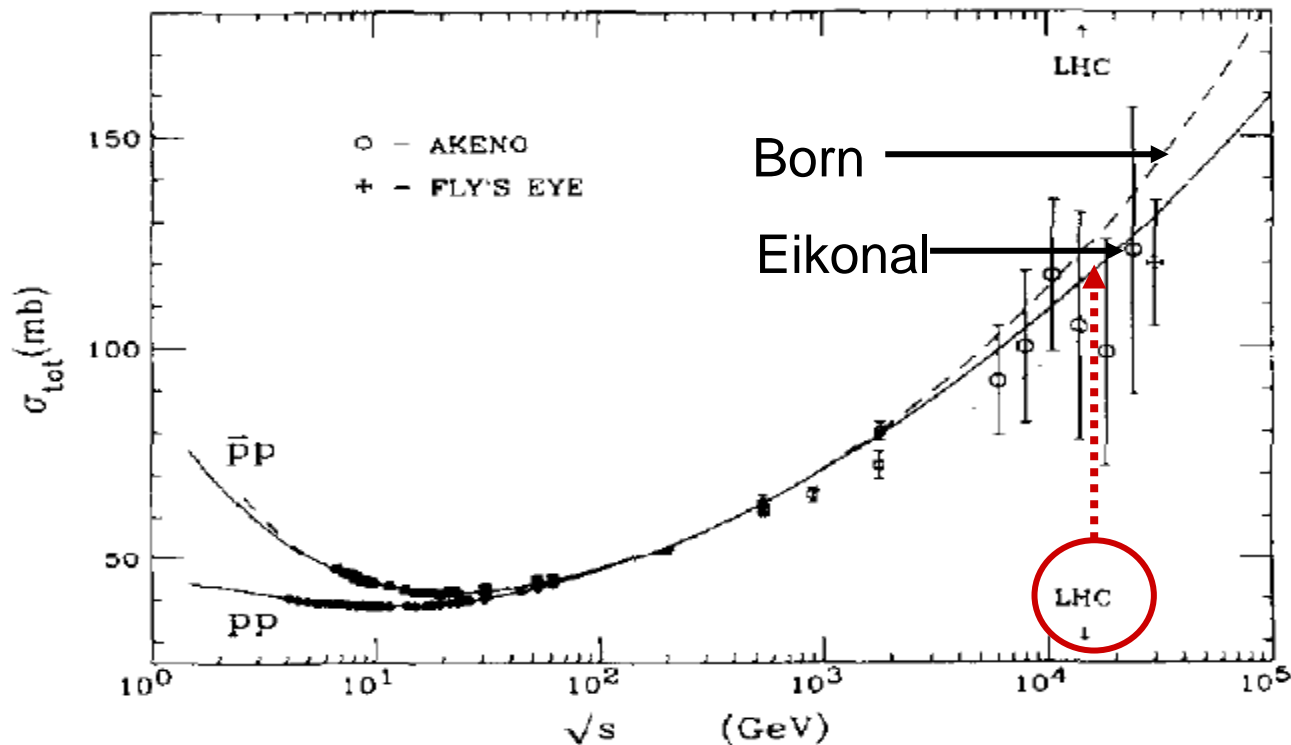
RESULTS

$$\alpha_{0,\mathbf{P}}^{\text{Born}} = 1.104 \pm 0.002, \quad \alpha_{0,\mathbf{P}}^{\text{Eik}} = 1.122 \pm 0.002$$

$$\sigma_{\text{tot}}^{p^\pm p} = 16.79 s^{0.104} + 60.81 s^{-0.32} \mp 31.68 s^{-0.54}$$

negligible

# $\sigma^T$ at LHC from global fit



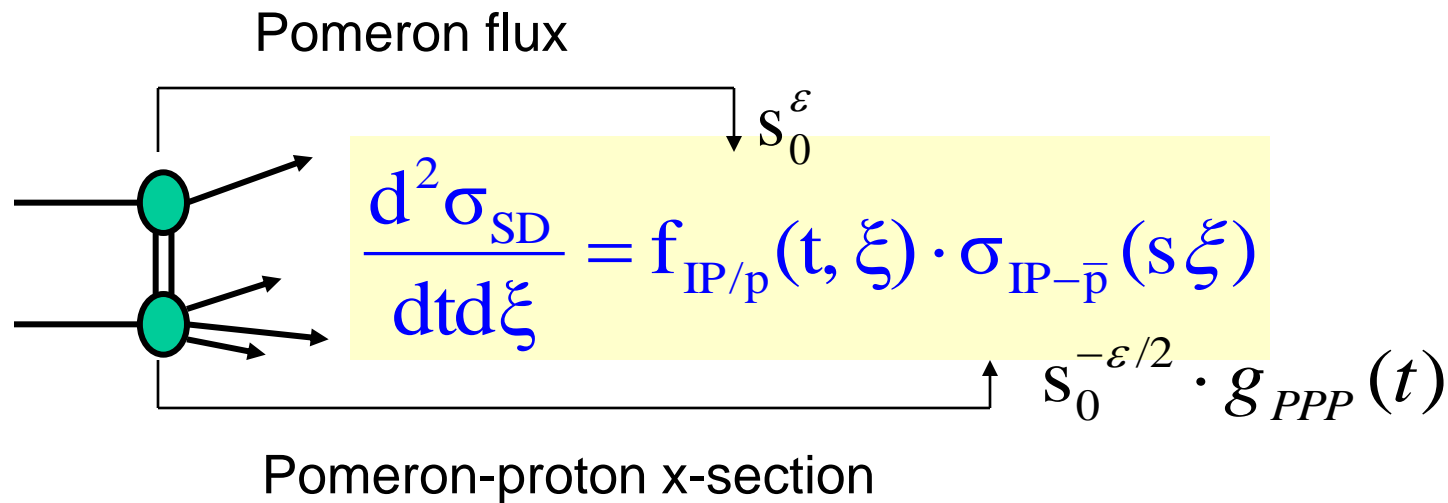
- ✦  $\sigma$  @ LHC  $\sqrt{s}=14$  TeV:  $122 \pm 5$  mb Born,  $114 \pm 5$  mb eikonal  
 → error estimated from the error in  $\epsilon$  given in CMG-96

Compare with **SUPERBALL**  $\sigma(14 \text{ TeV}) = 113 \pm 6$  mb

**caveat:  $s_0=1 \text{ GeV}^2$  was used in global fit!**

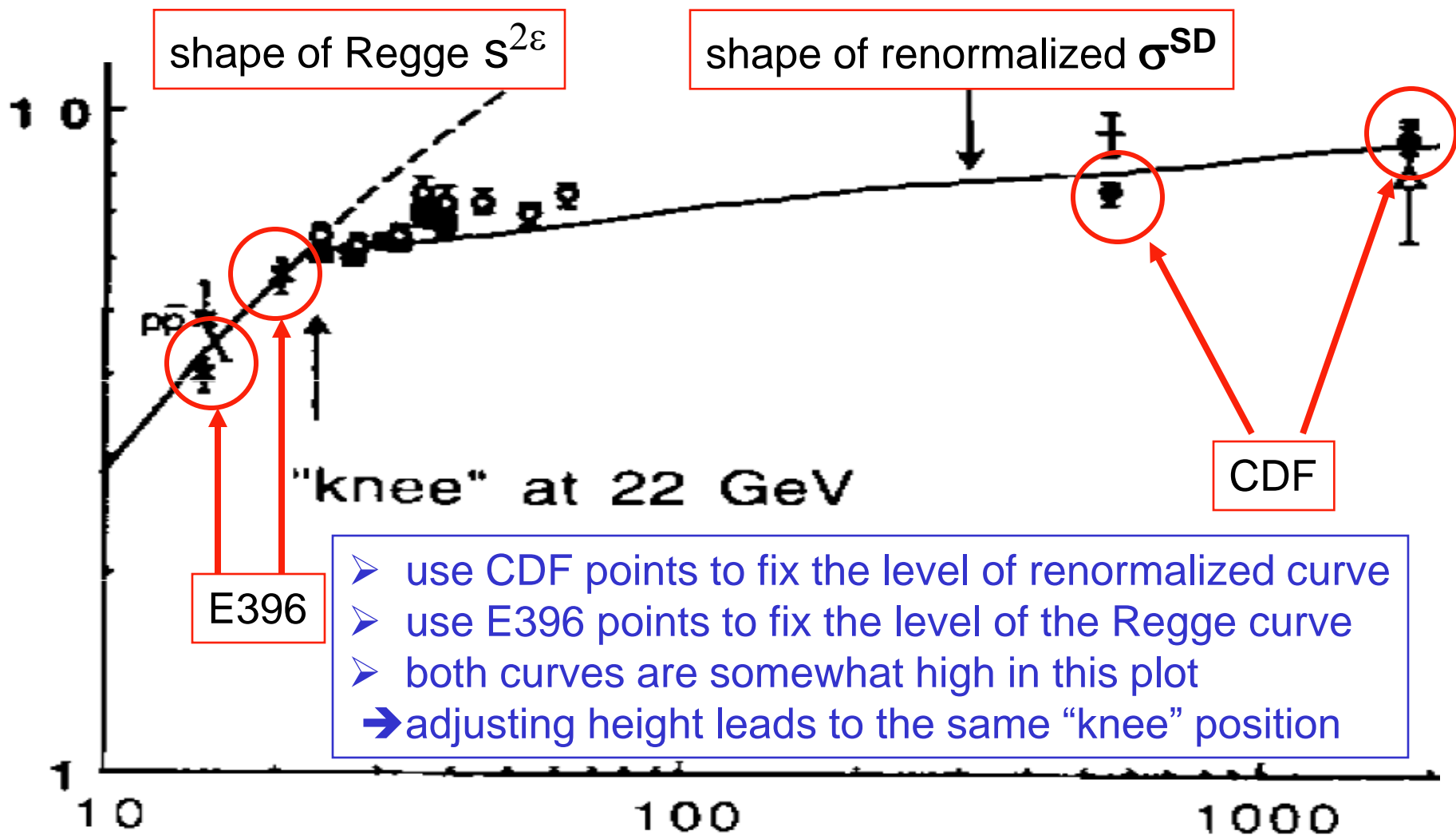


# Unitarity and Renormalization

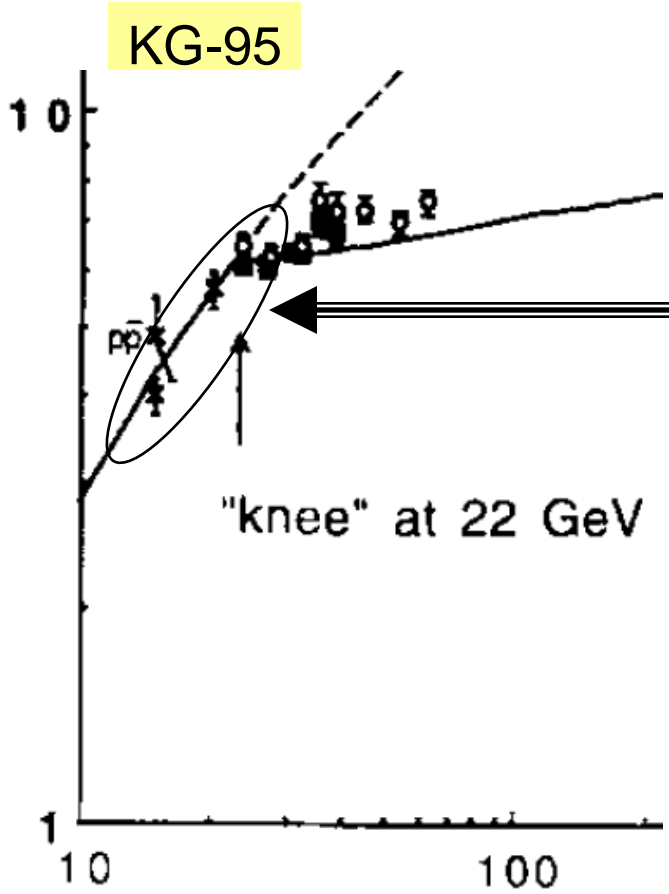


- Two free parameters:  $s_0$  and  $g_{PPP}$
- Obtain product  $g_{PPP} \cdot s_0^{\epsilon/2}$  from  $\sigma_{SD}$
- Renormalized Pomeron flux determines  $s_0$
- Get unique solution for  $g_{PPP}$

# The value of $s_0$ - limited edition



# The value of $s_0$ - a bird's-eye view



			$\sqrt{s}$ (GeV)	
⊠	Cool [KG]	FNAL	14	20
■	Albrow	ISR	23.3	26.9
○	Armitage	ISR	23.3	27.4

→ error in knee position:  $\pm 1$  GeV

"knee" @  $22 \pm 1$  GeV →  $s_0 = 1 \pm 0.2$  GeV

→ triple-Pomeron coupling:  
 $g_{PPP}(t) = 0.69 \text{ mb}^{1/2} = 1.1 \text{ GeV}^{-1}$  **KG-95**

# $\sigma_{SD}^T$ and ratio of $\alpha'/\epsilon$

$$\frac{d^2\sigma(s, M^2, t)}{dM^2 dt} = \left[ \frac{\sigma_0}{16\pi} \sigma_0^{IPp} \right] \frac{s^{2\epsilon}}{N(s)} \frac{1}{(M^2)^{1+\epsilon}} e^{bt}$$

$$s \xrightarrow{\Rightarrow} \infty \left[ 2\alpha' e^{\frac{\epsilon b_0}{\alpha'}} \sigma_0^{IPp} \right] \frac{\ln s^{2\epsilon}}{(M^2)^{1+\epsilon}} e^{bt}, \quad (13)$$

$$\sigma_{sd} \xrightarrow{s \rightarrow \infty} 2 \sigma_0^{IPp} \exp \left[ \frac{\epsilon b_0}{2\alpha'} \right] = \sigma_{sd}^\infty = \text{constant.} \quad (14)$$

$$2\sigma_0^{IPp} \exp \left[ \frac{\epsilon b_0}{2\alpha'} \right] = \sigma_0^{pp},$$

$$\sigma_0^{IPp} = \beta_{IPpp}(0) \cdot g(t) = \kappa \sigma_0^{pp}$$

$$\kappa = \frac{f_g^\infty}{N_c^2 - 1} + \frac{f_q^\infty}{N_c}$$

$$b_0 = R_p^2/2 = 1/(2m_\pi^2).$$

CTEQ5L →

$$f_g^\infty = 0.75$$

$$f_q^\infty = 0.25$$

$$r = \frac{\alpha'}{\epsilon} = -[16 m_\pi^2 \ln(2\kappa)]^{-1}$$

$$r_{pheno} = 3.2 \pm 0.4 \text{ (GeV/c)}^{-2}$$

$$r_{exp} = 0.25 \text{ (GeV/c)}^{-2} / 0.08 = 3.13 \text{ (GeV/c)}^{-2}$$

# Total Cross Section at LHC

- Froissart bound  $\sigma \leq \frac{\pi}{m^2} \cdot \ln^2 s$  (s in GeV<sup>2</sup>)
- For  $m^2 = m_\pi^2 \rightarrow \pi / m^2 \sim 10^4$  mb – large!
- If  $m^2 = s_0 = (\text{mass})^2$  of a large **SUPERglueBALL**, the bound can be reached at a much lower s-value,  $s_F$ ,  
 $\rightarrow \sigma(s > s_F) = \sigma(s_F) + \frac{\pi}{s_0} \cdot \ln^2 \frac{s}{s_F}$
- Determine  $s_F$  and  $s_0$  from  $\sigma_T^{\text{SD}}$
- Show that  $\sqrt{s_F} < 1.8$  TeV
- Show that at  $\sqrt{s} = 1.8$  TeV Reggeon contributions are negligible
- Get cross section at the LHC as  $\sigma^{\text{LHC}} = \sigma_{1800}^{\text{CDF}} + \frac{\pi}{s_0} \cdot \left( \ln^2 \frac{s^{\text{LHC}}}{s_F} - \ln^2 \frac{s^{\text{CDF}}}{s_F} \right)$

# The SUPERBALL cross-section

- ❑ Froissart bound

$$\sigma \leq \frac{\pi}{m^2} \cdot \ln^2 s$$

- ❑ Valid above “knee” at  $\sqrt{s} = 22$  GeV and therefore at  $\sqrt{s} = 1.8$  TeV

- ❑ Use superball mass:

$$\rightarrow m^2 = s_0 = (1 \pm 0.2) \text{ GeV}^2$$

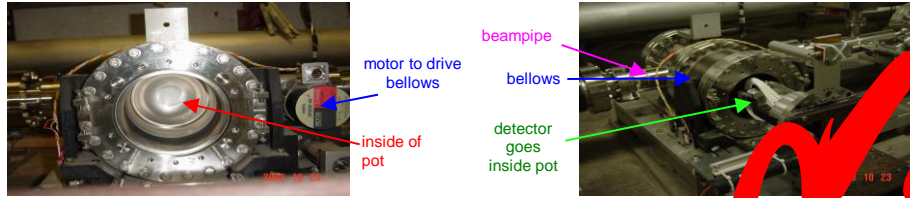
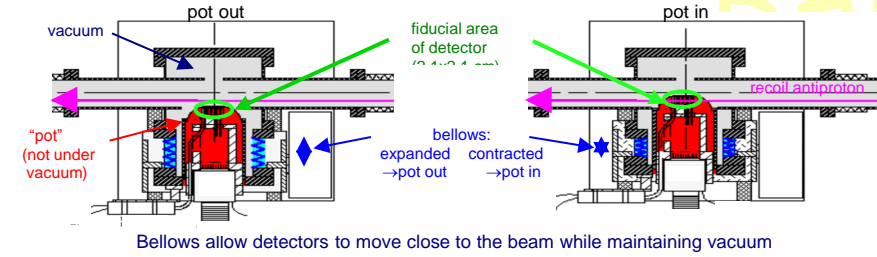
- ❑ At  $\sqrt{s}$  1.8 TeV Reggeon contributions are negligible (see global fit)

$$\sigma_{14000}^{\text{LHC}} = \sigma_{1800}^{\text{CDF}} + \frac{\pi}{s_0} \cdot \left( \ln^2 \frac{s^{\text{LHC}}}{s_F} - \ln^2 \frac{s^{\text{CDF}}}{s_F} \right) = (80.03 \pm 2.24) + (39 \pm 6) = 119 \pm 6 \text{ mb}$$

→ compatible with CGM-96 global fit result of  $114 \pm 5$  mb (see next slides)

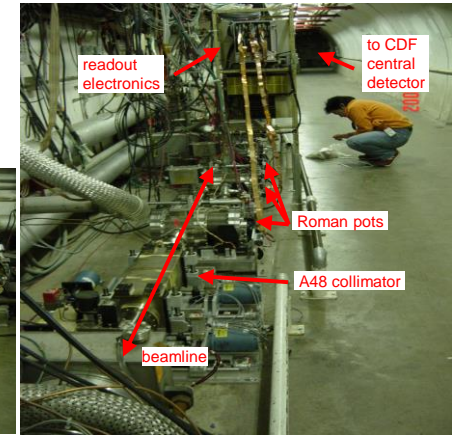


## Concept of a Roman Pot



## In the Tevatron Tunnel

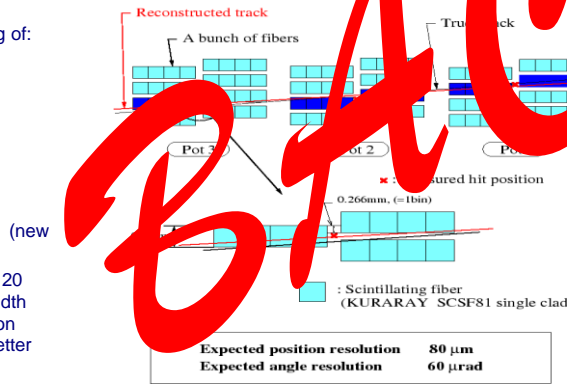
CDF had three Roman pots (RP1, RP2, RP3) located 57m downstream of the interaction point along the antiproton beam direction. They were used to detect antiprotons which underwent a "diffractive" interaction and were scattered in a direction very close to that of the original beam.



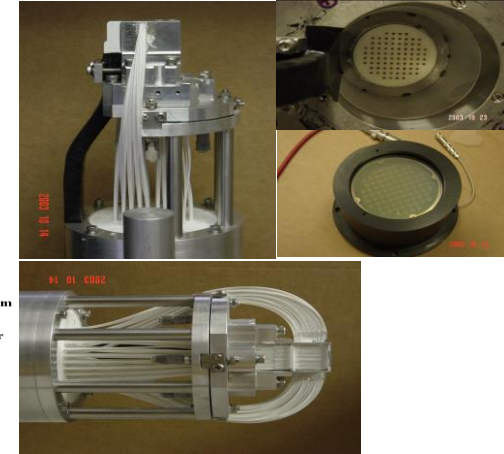
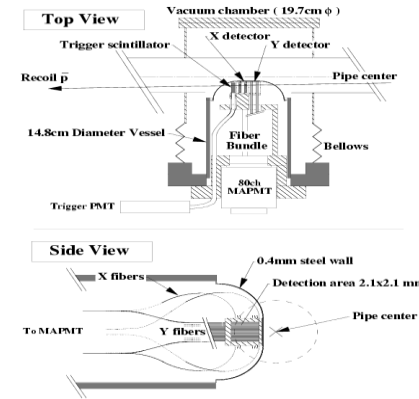
## Roman-Pot Detector Design – by The Rockefeller University

The three Roman pots each contain detectors consisting of:

- Trigger scintillating counter 2.1x2.1x0.8 cm<sup>3</sup>
- 40 X + 40 Y fiber readout channels
  - Each consists of 4 (→ bigger signal) clad scintillating fibers 0.8x0.8 mm<sup>2</sup> technology at the time)
  - X, Y each have 2 rows of 20 fibers spaced 1/3 fiber width apart for improved position resolution (three times better than with a single row)

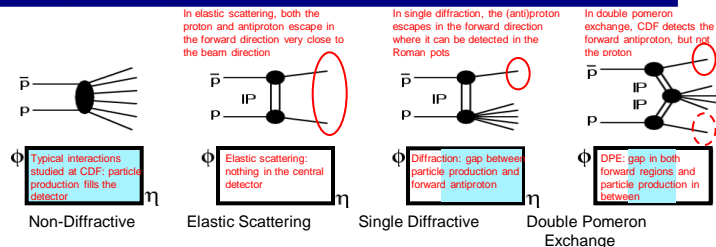


## CDF "Tokyo"-Pot Detectors – Built by the University of Tsukuba, Japan



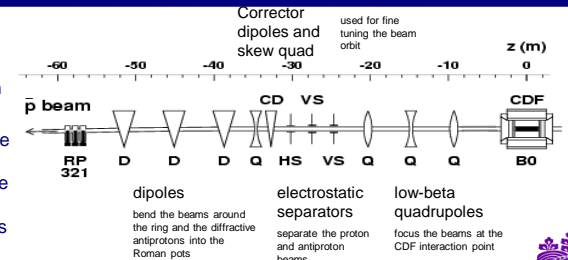
## Physics Using the Roman-Pot Detectors

- The Roman-pot detectors are used to study diffractive interactions
- Elastic scattering was measured by CDF in 1988-1989 using Roman pots (not those described here) in both the proton and antiproton direction

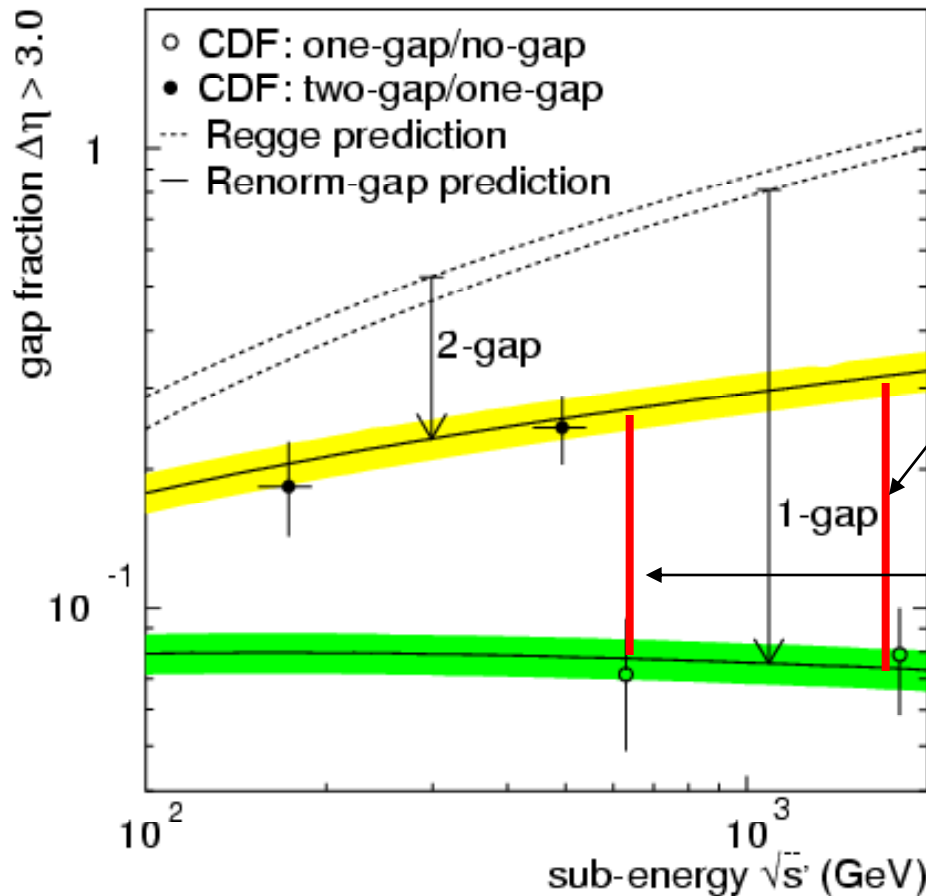


## Path of the Antiproton through the Tevatron Magnets

- Dipole magnets bend recoil antiprotons which have lost momentum towards the inside of the Tevatron ring, into the Roman pots
- Knowledge of the beam optics, the collision vertex position, and the antiproton track position and angle in the Roman-pot detectors are used to reconstruct the kinematics of the diffractive antiproton



# Gap survival probability



$$S = \frac{\phi \left[ \begin{array}{|c|c|c|} \hline \eta & & \eta \\ \hline \end{array} \right] / \phi \left[ \begin{array}{|c|} \hline \eta \\ \hline \end{array} \right]}{\phi \left[ \begin{array}{|c|c|c|} \hline \eta & & \eta \\ \hline \end{array} \right] / \phi \left[ \begin{array}{|c|c|c|} \hline \eta & & \eta \\ \hline \end{array} \right]}$$

$$S_{2\text{-gap}/1\text{-gap}}^{1\text{-gap}/0\text{-gap}} (1800 \text{ GeV}) \approx 0.23$$

$$S_{2\text{-gap}/1\text{-gap}}^{1\text{-gap}/0\text{-gap}} (630 \text{ GeV}) \approx 0.29$$

# CDF and D0 Detectors

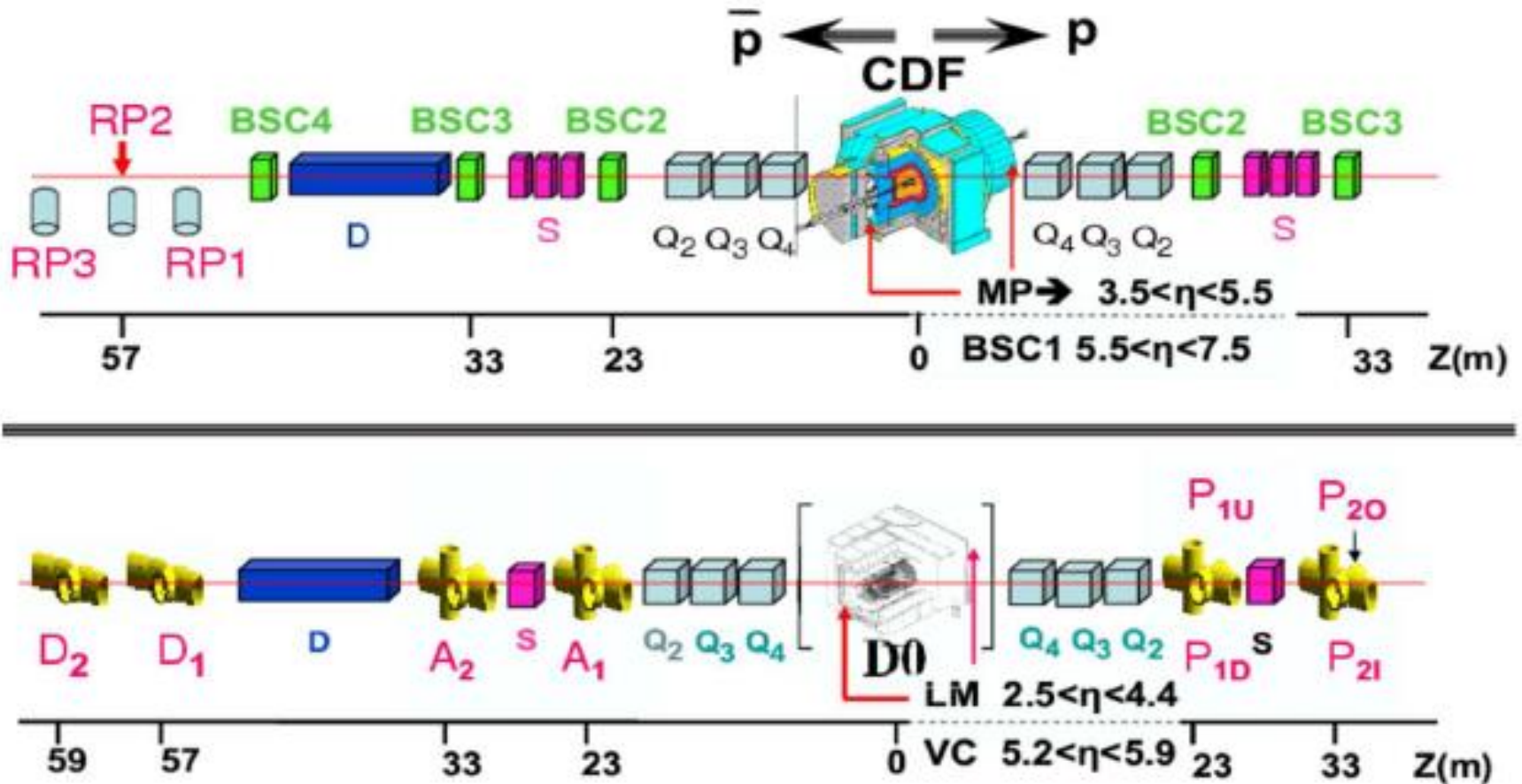


Figure 1: The CDF and D0 detectors in Run II